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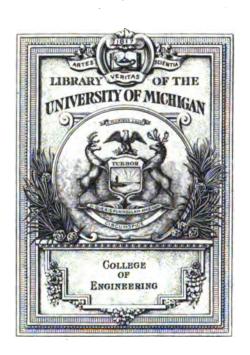
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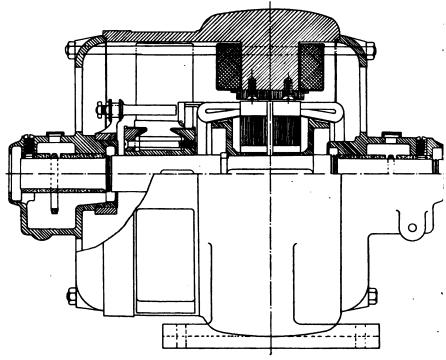
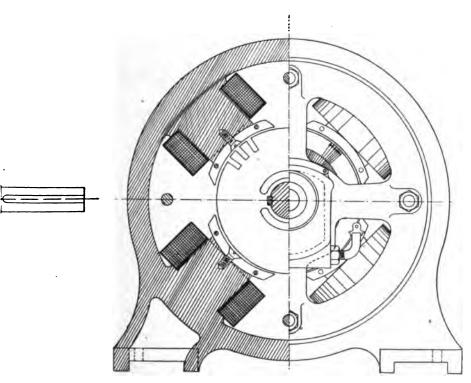


FIG. 232.—15-H.P. 460-volt motor, design



1ed for a speed of 600 R.P.M. Scale, 1:8.

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# PRINCIPLES OF DIRECT-CURRENT ELECTRICAL ENGINEERING

ΒY

# JAMES R. BARR, A.M.I.E.E

LECTURER IN ELECTRICAL ENGINEERING, HERIOT-WATT COLLEGE

WITH 294 ILLUSTRATIONS

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#### PREFACE

In lecturing on Electrical Engineering to Second-Year Students the author has realised the want in recent years of a really suitable text-book—one which he could recommend as adequately bridging the gap between the several elementary manuals and the many excellent works on specialised branches of the subject.

This treatise has been written primarily for the intermediate class-work of Universities and Technical Colleges, the basis being a series of the author's Lectures to Second-Year Students, with a selection of problems systematically arranged in the order of treatment of the subject.

A knowledge of the elementary principles of electrical physics and mathematics has been assumed. In writing the book it has been an aim to give a clear and concise account of the fundamental principles of direct-current electrical engineering. The work deals essentially with Principles, and whenever possible the methods of applying them are illustrated with numerical and descriptive examples. Only those theories and methods of solving problems have been discussed which experience in design and operation has shown to be of practical utility.

The descriptive work has been confined to ap-

paratus and machines associated with the best practice in present-day electrical engineering. Useless catalogue illustrations have been rigidly excluded, the drawings, with a few exceptions, having been specially prepared. In several cases, for the sake of clearness, coloured diagrams have been adopted; the distinct advantages of which in dealing with armature windings, switchboard connections, etc., need no comment.

The author is specially indebted to his friend Charles W. D. Newman, A.M.I.E.E., for the unwearied assistance given in reading over the original MS., and in making numerous and valuable suggestions. His thanks are also due to Dr. W. Mansergh Varley and T. K. Evans, B.A., for looking over proofs; and to John T. Wight, who prepared most of the drawings for Chapters VIII. to XI.

J. R. B.

HERIOT-WATT COLLEGE, EDINBURGH, 1908.

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# PRINCIPLES OF DIRECT-CURRENT ELECTRICAL ENGINEERING

#### CHAPTER I

## UNITS EMPLOYED IN ELECTRICAL ENGINEERING

In commencing a study of the subject of Electrical Engineering it is essential to thoroughly understand how the units employed in practice are derived from the fundamental units. This chapter will be devoted to a brief résumé of the derivations.

A scientific treatment of such a subject as Electrical Engineering is only possible when there is some means of making definite statements as to quantity. This is done by stating how many arbitrarily chosen units are required to make up any quantity in question.

The ideas of length and time are regarded as primary—length, the conception of an interval of space; time, the conception of a duration of a period. Length and time being primary, are the first two fundamental quantities; mass is usually considered third, and is the amount of matter in a body.

The system of units adopted for engineering work is based on those of length, mass, and time. Starting with the fundamental units, it will be shown how (1) the Mechanical, and (2) the Electrical units used in practical engineering are derived, and also the relationship between the two sets.

#### FUNDAMENTAL UNITS

Length.—In Britain the unit of length is the yard, and in France, the metre. Both these units are selected

arbitrarily for their convenience, though the original idea of the metre was derived from a connection with the supposed dimensions of the earth. For scientific purposes the hundredth part of the metre, *i.e.* the centimetre, is taken as the unit of length.

I inch = 2.54 centimetres.
I foot = 30.48 centimetres.
3.28 feet = I metre.
0.621 mile = I kilometre.

Mass.—The unit of mass is fixed arbitrarily, the British and French units being respectively the pound and the kilogramme. The kilogramme originally represented the weight of a cubic decimetre of water at 4° C., i.e. its point of maximum density. More recent investigations have, however, shown that this is not exactly fulfilled. A smaller unit is more convenient in the laboratory, so the thousandth part of the kilogramme, i.e. the gramme, has been chosen as the unit of mass. For all practical purposes the gramme is taken as the mass of a cubic centimetre of water at 4° C.

I lb. = 453 grammes.
I ton ≈ 1000 kilogrammes.

Time.—The unit of time is the  $\frac{1}{86400}$  part of a mean solar day, and is called the second.

The system of units based on the centimetre, the gramme, and the second is in universal use for scientific purposes, and is referred to as the C.G.S. system. All other dynamical units are derived from these three fundamental ones of length, mass, and time. As the dynamical units, so derived, are, with a few exceptions, generally inconveniently small for practical work, the practical units are multiples of the absolute units.

#### MECHANICAL UNITS

Area.—The unit of area is the square centimetre.

I square inch = 6.45 square centimetres.

Volume.—The unit of volume is the cubic centimetre,

I cubic inch = 16.4 cubic centimetres.

Velocity is the rate of change of position. It involves the idea of direction as well as that of magnitude; thus the velocity of a body may be changed by altering the rate at which it moves, or by altering the direction in which it is moving.

The unit of velocity is the velocity of a body which moves through unit distance in unit time, *i.e.* a velocity of 1 centimetre per second.

Velocity in centimetres per second

$$= \frac{\text{space (centimetres) traversed}}{\text{time (seconds)}}.$$

Momentum is the quantity of motion in a body, and is measured by the product of mass and velocity.

The unit of momentum is the momentum of a body I gramme in weight moving at the rate of I centimetre per second.

Acceleration is the rate at which velocity changes, i.e. increases or decreases. Unit acceleration is the change in velocity of a body at the rate of 1 centimetre per second for every second the motion continues, and is usually expressed in centimetres per second per second, or centimetres per second.

The acceleration due to gravity (denoted by "g") is 981 centimetres per second<sup>2</sup> or 32.2 feet per second<sup>2</sup>.

Force is that which tends to alter a body's state of rest or uniform motion in a straight line, and is measured by the rate of change of momentum which it produces.

The unit of force is that force which, acting for I second on a mass of I gramme, gives it a velocity of I centimetre per second. This unit is termed the *dyne*. One gramme weight exerts a force downwards of 981 dynes due to the action of gravity.

I dyne = weight of 
$$\frac{1}{981}$$
 gramme.

I poundal = ,, ,,  $\frac{1}{32.2}$  lb.

I ,, = 13,825 dynes.

I lb. weight = 32.2 poundals = 445,000 dynes.

I kilogramme weight  $\approx$  1,000,000 dynes.

Work is the product of a force and the distance through which it acts. The unit of work is the work done in overcoming unit force through unit distance, i.e. the work done when I dyne acts through a distance of I centimetre. This is called the erg.

Since the weight of 1 gramme is 981 dynes, the work done in raising 1 gramme through a height of 1 centimetre against the force of gravity is 981 ergs. This unit is exceedingly small, and the *joule*, equal to 10<sup>7</sup> ergs, is used as the practical unit of work in the

C.G.S. system.

This unit of work is, however, very seldom used by British engineers, the unit employed being the *foot-pound* (ft.-lb.). The foot-pound is the work done when a body moves through I foot against a force equal to the weight of I pound.

Work = force x distance. I ft.-lb. = 13,825 gramme-centimetres. = 1.356 x 10<sup>7</sup> ergs. 0.7373 ft.-lb. =  $10^7$  ergs = 1 joule. 7.233 ft.-lbs. = 1 kilogramme-metre.

Power is the rate at which work is done. This clearly introduces the idea of work done with reference to the time in which it is accomplished, whereas work itself has no reference to time. It is important to be able to distinguish between power, *i.e.* the rate of doing work, and the amount of work done.

The absolute unit of power is the erg per second, but the practical unit is the foot-pound per minute. The unit of power generally used by engineers is an arbitrary one established by James Watt, namely, a horse-power which is 33,000 ft.-lbs. of work per minute, or 550 ft.-lbs. per second.

Horse-power (written H.P.) =  $\frac{\text{ft.-lbs. of work done}}{\text{time in minutes} \times 33,000}$ 

1 H.P. = 7.46 × 10<sup>9</sup> ergs per second. = 76 kilogramme-metres per second. = 33,000 ft.-lbs. per minute. = 550 ft.-lbs. per second. Energy is the capacity for doing work. There are two kinds of energy—Kinetic Energy and Potential

Energy.

Kinetic energy is possessed by all moving matter, and is the work a body can do in virtue of its motion. If a body of mass m units is moving with a velocity of v units, then the energy or units of work stored up in the mass

$$= \frac{1}{2} mv^2.$$

Potential energy is the work a body can do in virtue of its position in space. Thus when a body of mass m units is raised through a distance s units, the units of work stored up in it

= ms.

#### ELECTRICAL UNITS

The electrical units will now be considered. There are two systems derived from the fundamental units, one set being based upon the force exerted between two quantities of electricity, and the other upon the force exerted between two magnetic poles. The former set are called the electro-static and the latter the electromagnetic units. The commercial units are derived from the latter system.

Unit Magnetic Pole.—Consider two magnet poles of which the strengths are  $m_1$  and  $m_2$ , placed a certain distance apart in air. The mutual attraction or repulsion between the two magnets is proportional to the product of the pole strengths and inversely proportional to the square of their distance apart. This force may be written:

$$f = k \frac{m_1 m_2}{d^2}$$

where k is a constant depending in value upon the units in which f, m, and d are measured. If the poles are equal in strength then  $f = k \frac{m^2}{d^2}$ , and the unit pole is so chosen that m = 1 when f and d are both unity: the

value of k will thus also be unity, and the above formula may be written:

 $f = \frac{m^2}{d^2}.$ 

The unit magnetic pole is that which, when placed at a distance of 1 centimetre from a similar pole, is repelled with a force of 1 dyne (the medium between the poles being air).

Unit Strength of Magnetic Field.—A magnetic pole, situated in a magnetic field, experiences a definite force acting in a definite direction: the magnitude of the force is proportional to the pole strength (m) of the magnet and the strength (H) of the field, or

$$f = kmH$$
.

The units in which f, m, and H are measured are so chosen that k = 1; in which case f = mH. Hence a magnetic field has unit strength when a unit magnetic pole situated in the field is acted on by the force of 1 dyne. Unit magnetic field exists 1 centimetre from unit pole.

Unit Potential-Difference, or Electromotive force (E.M.F.), is set up between the ends of a conductor, which moves through a magnetic field at such a rate that one line of force is cut per second. The practical unit of pressure is 100,000,000 times the absolute unit, and is called the volt.

1 volt = 108 absolute units.

1 micro-volt = 
$$\frac{1}{10000000} = \frac{1}{100}$$
 of a volt.

From the definition of E.M.F. it will be seen that when a conductor of length l centimetres cuts a magnetic field having a density of H lines of force per square centimetre at the rate of v centimetres per second, the electromotive force induced in the conductor is expressed by the equation

E (volts) = 
$$H \times l \times v \times 10^{-8}$$
.

Unit Current is that current which flows in a con-

ductor of unit length bent so as to form an arc of a circle 1 centimetre in radius, and acts upon unit pole at the centre of the circle with a force of 1 dyne. The practical unit of current is  $\frac{1}{10}$  of the absolute unit, and is called the *ampère*.

I ampère = 
$$10^{-1}$$
 absolute units.  
I milliampère =  $\frac{I}{1000}$  ampère.

Unit Resistance is the resistance of a conductor in which unit current is produced by unit potential difference between its ends. By Ohm's law\*, the resistance of a conductor

But 1 volt = 10<sup>8</sup> absolute units of pressure, and 1 ampère = 10<sup>-1</sup> ,, ,, current; therefore the practical unit of resistance, named the *ohm*,  $= \frac{10^8}{10^{-1}} = 10^9 \text{ absolute units.}$  The ohm is often

denoted by the symbol  $\omega$ .

$$I microhm = \frac{I}{IO^6}ohm = IO^{-6} ohm.$$

10<sup>6</sup> ohms = 1 megohm; a term employed in specifying the insulation resistance of cables or electrical machinery, and denoted by the symbol  $\Omega$ .

Unit Quantity of electricity is that which passes round a circuit in 1 second when a current of 1 absolute unit flows. The ampère being  $\frac{1}{10}$  of this current, the practical unit of quantity is likewise a  $\frac{1}{10}$  of the absolute unit, and is called the *coulomb*.

1 ampère-hour = 3600 coulombs.

Unit Force is that force exerted on a conductor of unit length and carrying unit current when it is placed in, but at right angles to, a field of unit intensity.

<sup>\*</sup> See p. 12.

Hence if H denote the strength of field, and i the current in absolute units, then the force acting on a conductor of l centimetres is given by

Force (dynes) = 
$$H \times l \times i$$
.

Unit Power.—Power has been defined as the rate at which work is done, and is measured by the number of units of work done per second. If in t seconds a quantity of electricity Q is conducted against a potential difference E, the work done per second =  $\frac{QE}{t}$ .

But 
$$Q/t = \text{current}$$
, hence Power =  $C \times E$ .

In C.G.S. units power is measured in ergs per second.

The Watt is the practical unit of power and

=  $10^8 \times 10^{-1} = 10^7$  absolute units

=  $10^7$  ergs per second = 1 joule per second.

The product of electromotive force in volts, and current in ampères, gives the power in watts.

$$\dot{W} = E \times C$$
.

As the value of the watt is very small and inconvenient to denote the power of large dynamos, the practical unit of power is 1000 watts, and is called the *Kilowatt*, usually written k.w.

Kilowatts = 
$$\frac{E \times C}{1000}$$
.

Now I H.P. =  $7.46 \times 10^{9}$  ergs per second, and I watt =  $10^{7}$  ergs per second.

Therefore I H.P. =  $\frac{7.46 \times 10^9}{10^7}$  = 746 watts, and I k.w. =  $\frac{1000}{746}$  H.P. = 1.34 H.P.  $\approx 1\frac{1}{3}$  H.P.

This is an important result, as it forms a connecting link between the mechanical and electrical units.

The French horse-power (Force de cheval) = 736 watts.

Unit Energy is expended by I watt in I second, or by a coulomb flowing through a conductor in which there is a difference of potential of I volt. The watthour is a more convenient unit, and is the energy expended in I hour by I ampère flowing along a conductor under I volt pressure.

The Kilowatt-hour or Board of Trade Unit is the legal unit of electrical energy, fixed by the Board of Trade for public supply purposes, and is the quantity of energy supplied in I hour by a current at such a pressure that the product of volts, ampères, and hours equals 1000.

The Board of Trade Unit, written B.T.U., equals

# ampères x volts x hours

IB.T.U. = Ik.w. hour = 1.34 H.P. hours.

Unit Capacity is that of a condenser which will be at unit difference of potential when charged with unit quantity. The practical unit is the Farad, and equals 10-9 absolute units.

In order to thoroughly familiarise the student with the above units a few examples are worked out, showing how the knowledge already acquired may be applied to practical problems. After carefully studying each of these examples there should be no difficulty in working through the problems on this chapter at the end of the book.

Example.—A weight of 2.5 lbs. is raised vertically through a distance of 20 feet in 30 seconds. Calculate

- (1) Force exerted in dynes,
- (2) Work done in joules,
- (3) Power in watts to do this work.
- (1) Force in dynes = weight in grammes × 981
  - $= 2.5 \times 453 \times 981$
  - = 1,112,000.

(2) Work done in joules—
$$= \frac{\text{work in ergs}}{10^7}$$

$$= \frac{\text{force in dynes} \times \text{distance in centimetres}}{10^7}$$

$$= \frac{1,112,000 \times 20 \times 12 \times 2.54}{10^7}$$

$$= 67.8.$$

(3) Power in watts = joules per second  $= \frac{67.8}{30}$ = 2.36.

Example.—A hoist raises 15 cwts. through 400 feet. Calculate the work done.

Work done = weight in lbs. × distance in feet = 15 × 112 × 400 = 672,000 ft.-lbs.

If the work has to be done in 2 minutes find the H.P. of the motor required to drive the hoist, assuming the gearing has an efficiency of 75 per cent.

H.P. to raise the weight-

$$= \frac{\text{ft.-lbs. of work done}}{\text{time in minutes} \times 33,000}$$
$$= \frac{672,000}{2 \times 33000} = 10 \text{ H.P.}$$

Allowing 75 per cent. for efficiency of gearing,

H.P. of motor = 10 
$$\times \frac{100}{75}$$
 = 13.4.

The motor has an efficiency of 87 per cent. and is connected to a 220 volt supply. Calculate the current taken from the mains at full load.

Watts output at motor pulley =  $13.4 \times 746$ . Watt input from electrical supply—

$$= 13.4 \times 746 \times \frac{100}{87}.$$
Current =  $\frac{\text{watts}}{\text{volts}} = \frac{13.4 \times 746 \times 100}{220 \times 87}$ 
= 52 ampères.

Example.—A dynamo gives an output of 100 ampères at 500 volts. Find the H.P. of engine to drive it, assuming the dynamo to have an efficiency of 90 per cent.

Watts output = 
$$100 \times 500 = 500,000$$
.  
Watts input =  $50,000 \times \frac{100}{90} = 55,500$ .  
H.P. of engine =  $\frac{55,500}{746} = 75$ .

If the above dynamo gives the full load for 6 hours, find the number of Board of Trade units generated.

Board of Trade units = 
$$\frac{\text{volts} \times \text{ampères} \times \text{hours}}{1000}$$
  
=  $\frac{500 \times 100 \times 6}{1000}$   
= 300.

#### CHAPTER II

#### FUNDAMENTAL PRINCIPLES

#### RESISTANCE

Ohm's Law.—When a current flows through a conductor a definite resistance is offered by it to the passage of the current, and consequently there must be a drop or loss of pressure in that conductor the value of which depends upon the resistance offered. The relation between the electromotive force E and the current C was first enunciated by Ohm in 1827 and is called Ohm's Law. Ohm found by experiment that the ratio of E to C was constant so long as the physical state (temperature, etc.) of the conductor remained the same. The constant ratio between the electromotive force and the current is called the resistance of the conductor, and representing it by R, Ohm's law may be stated algebraically as follows:

$$E/C = R$$
.

In words, Ohm's law states that the resistance of a given conductor, when its physical state is maintained constant, is the ratio of fall of E.M.F. in a conductor to the current flowing through it. It is of importance to observe that the quantity R defined by the above equation is independent of the strength of the current flowing through the conductor. The value of R will be investigated in this chapter, and depends upon the sectional area, length of the conductor, the material of which it consists, and upon the physical state of the material. The most searching investigations have been made as to the truth of this law when currents are passed through metals or electrolytes; these have all failed to discover

any exceptions to it. The law, however, does not hold when currents are passed through gases.

Example.—A circuit consists of 50 16-c.p. lamps in parallel, each lamp taking 4 watts per candle. If each lead has a resistance of 0.25 of an ohm, find the voltage of the dynamo so that the pressure at the lamps may be 200 volts.

Figure 1 represents the circuit.

Since each lamp gives 16 c.p. and takes 4 watts per candle, the watts absorbed by 50 lamps =  $4 \times 16 \times 50$ .

By definition of power, watts =  $\vec{E} \times \vec{C}$ . Therefore current taken by the lamps

= watts/E  
= 
$$\frac{4 \times 16 \times 50}{200}$$
 = 16 ampères.

This is also the value of the current flowing in the leads. The next part of the problem is to obtain the voltage drop in the leads.

By Ohm's law E = CR, R in this case being the resistance of both leads and  $= 2 \times 0.25 = 0.5$  of an ohm. Therefore the voltage drop in the leads  $= 16 \times 0.5 = 8$  volts. Now the pressure at the lamps = 200 volts, hence the voltage of the dynamo = 200 + 8 = 208 volts.

Specific Resistance.—Materials used in electrical en-

gineering may be divided into two classes—(a) those which are good conductors of electricity, and (b) those which are bad conductors; the former are simply called conductors and the latter insulators. Conductors provide paths

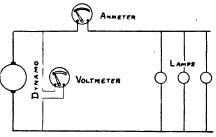


FIG. 1.

along which electricity can flow, and insulators are used for preventing it from flowing along any other path simultaneously. As there are no perfect conductors, all offering some resistance to the flow of electricity, similarly there are no perfect insulators, the best insulators known

having some conductivity.

The resistance of metallic conductors will now be considered. The starting-point in the calculation of resistance is the knowledge of the resistance offered between two opposite faces of a material, having unit length and unit area of cross-section. This is known as Specific Resistance, and varies for different materials. Taking the centimetre as the unit of length and the square centimetre as the unit of area, the specific resistance of a material may be defined as the resistance offered by a wire of that material having a length of one centimetre and a cross-sectional area of one square centimetre, or, as the resistance between the opposite faces of a centimetre cube of the material. Specific resistance is sometimes defined in terms of the inch and square inch, but the former method is the more often used. Table I. gives the specific resistance of some of the conductors employed in electrical engineering, the resistance being given in microhms per centimetre cube. The student is here cautioned against the practice of defining the specific resistance as so many microhms per cubic centimetre or cubic inch. This would imply that the resistance varies as the volume, which, as will be seen directly, is quite erroneous.

From the table it will be seen that silver is the best conductor, being followed closely by copper. The latter substance is in most general use as a conductor of electricity, and its specific resistance should be committed to memory, as it is continually required in calculations. The specific resistance of liquids is very variable, its value depending upon the density. Column 2 gives the relative resistance of conductors, that of annealed copper being taken as unity.

Calculation of Resistance.—For a conductor of a given material under constant conditions of temperature, the resistance is directly proportional to the length and inversely proportional to the area of cross-section. Hence if l be the length, a the area of cross-section, and  $\rho$  the

TABLE I
TABLE OF SPECIFIC AND RELATIVE RESISTANCES OF
CONDUCTORS

Substance.	Specific Resist- ance in microhms per centimetre cube at o° C.	Relative Resistance.		
Metals—				
Silver (annealed)	1.468	0.940		
Copper (annealed)	1.561	0.1		
Copper (hard drawn)	1.592	1.020		
Aluminium (99 per cent. pure) .	2.563	1.642		
Aluminium (97.5 per cent. pure) .	2.665	1.707		
Zinc	5.751	3.684		
Iron (pure)	9.065	5.806		
Iron (Telegraph)	14.910	9.552		
Platinum	10.917	6.995		
Nickel	12.323	7.893		
Tin	13.048	8.358		
Tantàlum	16.000	10.25		
Lead	20.380	13.050		
Mercury	94.070	60.26		
Alloys—				
German silver $(Cu+Zn+Ni)$ .	30.01	19.21		
Manganin (84 $Cu+12$ $Mn+4$ $Ni$ ).	42.92	27.50		
Platinoid (German silver + 1 per		-		
cent. Tungsten)	41.73	26.73		
Carbon (glow lamp)	40 × 10 <sup>2</sup>	2,500		
" (arc lamp)	65 × 10 <sup>9</sup>	4,200		
Liquids (at 15° to 20° C.)—				
Water (ordinary distilled)	72,000 × 10 <sup>3</sup>			
Sulphuric acid (10 per cent.).	850 × 108			
Copper sulphate (saturated)	25,000 × 10 <sup>8</sup>			

specific resistance of the material, the resistance R is given by the equation

$$R = \frac{\rho \times l}{a}.$$

If  $\rho$  be in ohms per centimetre cube, then l and a must be in centimetres and square centimetres respectively, and the resistance R will be in ohms. The same expression will hold good if l be in inches, a in square inches, and  $\rho$  in ohms per inch cube. Since I inch = 2.54 centimetres, and I square inch = 6.45 square centimetres, the specific resistance in ohms per inch cube

\_ specific resistance in ohms per centimetre cube × 2.54.

Therefore the value of  $\rho$  for copper in ohms per inch cube at  $0^{\circ}$  C.

$$= \frac{1.592 \times 10^{-6} \times 2.54}{6.45} = .63 \times 10^{-6}.$$

Electrical conductors are generally made of circular cross-section. This is merely a matter of convenience, as the shape of the cross-section does not affect the conductivity. For a conductor of circular cross-section the area  $a = \frac{\pi a^2}{4}$  where d is the diameter.

Then 
$$R = \frac{\rho \times l \times 4}{\pi d^2}$$
  
or  $d = \sqrt{\frac{\rho \times l \times 4}{\pi R}}$  where R and  $\rho$  are in ohms and

d and l in centimetres.

Example.—Find the resistance of a copper wire 2000 yards long if it has a cross-sectional area of 0.15 square inch.

Whether the specific resistance is expressed in ohms per centimetre cube or in ohms per inch cube is immaterial, the final result in both cases being the same. Thus (1) taking  $\rho = 1.592 \times 10^{-6}$ , say  $1.6 \times 10^{-6}$  ohms per centimetre cube.

$$R = \frac{\rho \times l}{a}$$

 $l = 2000 \text{ yards} = 2000 \times 36 \times 2.54 \text{ centimetres}$   $a = 0.15 \text{ square inch} = 0.15 \times 6.45 \text{ square centimetres}$ Therefore  $R = \frac{1.6 \times 10^{-6} \times 2000 \times 36 \times 2.54}{0.15 \times 6.45}$ = 0.3 of an ohm.

(2) Taking  $\rho = 0.63 \times 10^{-6}$  ohms per inch cube, l and a must be reduced to inches and square inches.

$$l = 2000 \text{ yards} = 2000 \times 36 \text{ inches}$$
  
 $a = 0.15 \text{ square inch}$   
Therefore  $R = \frac{0.63 \times 10^{-6} \times 2000 \times 3}{0.15}$   
 $= 0.3 \text{ of an ohm.}$ 

Example. — Find the area of cross-section and diameter of a copper wire to have a resistance of 0.13 ohms per kilometre.

Since 
$$R = \frac{\rho \times l}{a}$$
.
$$a = \frac{\rho \times l}{R}$$

Taking  $\rho = 1.6 \times 10^{-6}$  ohms per centimetre cube then  $l = 10^5$  centimetres.

Therefore 
$$a = \frac{1.6 \times 10^{-6} \times 10^{5}}{0.13}$$

= 1.22 square centimetres.

Now area = 
$$\frac{\pi d^2}{4}$$
  $\therefore$   $d = \sqrt{\frac{4a}{\pi}}$   
 $d = \sqrt{\frac{4 \times 1.22}{\pi}} = 1.25$  centimetres.

Diameter of wire = 1.25 centimetres.

Example.—Find the area of cross-section of a cable 1000 metres long, to transmit 500 ampères so that the total drop in pressure along the cable may not exceed 25 volts. Take  $\rho = 1.6 \times 10^{-6}$  ohms per centimetre cube.

By Ohm's law the resistance of the cable

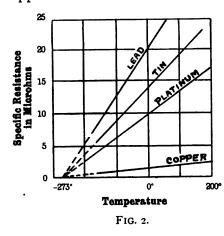
$$= \frac{\text{drop in volts}}{\text{current flowing}} = \frac{25}{500} = 0.05 \text{ ohm.}$$

$$\text{Now R} = \frac{\rho \times l}{a} \quad \therefore \quad a = \frac{\rho \times l}{R}$$

 $l = 10^5$  centimetres.

$$\therefore \text{ area } = \frac{1.6 \times 10^{-6} \times 10^{5}}{0.05} = 3.2 \text{ square centimetres.}$$

Variation of Resistance with Temperature. — In stating the specific resistance of a material the temperature at which it was obtained is also given, the reason for this being that all metals increase in resistance with rise of temperature. The variation in specific resistance with temperature for some metals, as determined by Professors Fleming and Dewar, is shown in Figure 2. The specific resistance was measured for temperatures between - 200°C. and +200°C. If the curves be produced towards the origin, as shown by the dotted lines, they all tend to cut the axis of abscissae at a point corresponding to  $-273^{\circ}$  C. From these curves it would appear that at absolute zero of temperature the resist-



ance of all pure metals would be zero. This leads up to the temperature coefficient of resistance, which is the increase in resistance of a material having an original resistance of 1 ohm when the temperature has increased 1° C. and is denoted by the Greek letter a. If R<sub>0</sub> be the resistance of a metal at o° C., then if the temperature increases to

 $t^{\circ}$  C., the increase in resistance =  $R_0 a t$ . So that the total resistance  $R_t$  is given by the equation

$$R_t = R_0 + R_0 a t$$
$$= R_0 (1 + at).$$

Since the resistance at 0° C. is seldom determined, the last equation may be written in another form. If  $R_1$  be the resistance at some temperature  $t_1$ , and  $R_2$  the resistance at a higher temperature  $t_2$ 

then 
$$R_2 = R_1 \{ 1 + a(t_2 - t_1) \}.$$

For all pure metals, the temperature coefficient a has almost the same value, namely, about 0.004. Table II. gives the temperature coefficient of various conductors, the values holding good when the temperatures are between the limits of o° and 100° C.

It is important to notice that carbon has a negative temperature coefficient. This phenomenon is also shown by most non-metals. In the case of electrolytes the specific resistance falls rapidly with increase of temperature, and the coefficient ranges from 0.2 per cent. to 2 per cent. per degree centigrade. This extremely important effect of temperature on the resistance of

TABLE II

TEMPERATURE COEFFICIENT OF VARIOUS CONDUCTORS

Con	duc	tor.			Temperature coefficient per ° C.
Silver .					0.004
Copper .				.	0.00428
Aluminium				.	0.00423
Zinc .				. \	0.00406
Iron .				.	0.00625
Platinum				.	0.00367
Nickel .				.	0.00622
Tantalum				.	0.003
Mercury					0.00072
German silve	er			.	0.000273
Platinoid					0.000310
Manganin					100000.0
Electrolytes			•	-	Negative temp. coefficient
Carbon .					-0.00052

substances causes some substances to be more suitable for particular purposes than others.

Specific Resistance and Temperature Coefficient of Alloys.—As far as their electrical properties depend on their constituent metals, alloys can be put into two classes. Alloys containing lead, tin, or zinc have a specific resistance which can be calculated from that of the constituent metals, knowing the proportions in which each is present. Thus an alloy having equal quantities of lead and tin, has a specific resistance equal to the mean of the specific resistance of the constituent metals.

In the case of most other metals the specific resistance of the alloy is much greater than that calculated in this manner. Not only is the specific resistance of such an alloy greater than that of the constituents, but the temperature coefficient is less than that of the constituents. For instance, the alloy German silver, having a specific resistance of 30.01 microhms per centimetre cube, and a temperature coefficient 0.000273, consists of the elementary metals copper, zinc, and nickel, the specific resistances of which are respectively 1.592,

5.751, and 12.323 microhms per centimetre cube, and the temperature coefficients 0.00428, 0.00406, and 0.00622

respectively.

This is a very important property of alloys from the point of view of the construction of standard resistances and shunts, for the smaller the temperature coefficient of the material used, the less its susceptibility to temperature variations. It is found that by using manganese as a constituent of an alloy it is possible to prepare a material of which the temperature coefficient at ordinary temperatures is either zero or very nearly so. Manganin is one of these alloys.

Example.—The field magnet coils of a shunt-wound dynamo have a resistance of 160 ohms at 15° C.; what will be their resistance at 35° C.? The temperature coefficient of copper = 0.0043.

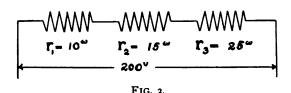
$$R_2 = R_1 \{ 1 + a(t_2 - t_1) \}$$
then substituting
$$R_2 = 160 \{ 1 + 0.0043(35 - 15) \}$$

$$= 160 \{ 1 + 0.0043 \times 20 \}$$

$$= 160 \times 1.086$$

$$= 174 \text{ obsets}$$

= 174 ohms. Resistance at 35° C. = 174 ohms.



Resistance of Systems of Conductors—(1) In Series.—If several conductors be joined in series, as shown in Figure 3, the resistance R of the arrangement is equal to the sum of the resistances of the separate conductors. If  $r_1 r_2 r_3 \dots$  denote the resistance of each conductor, then  $R = r_1 + r_2 + r_3 + \dots$  In Figure 3 there are three conductors, so that  $R = r_1 + r_2 + r_3$ .

(2) In Parallel.—When a number of conductors are connected in parallel, as shown in Figure 4, the reciprocal of the total resistance R is equal to the sum of the

reciprocals of the resistances of the separate conductors. If  $r_1 r_2 r_3 ...$  be the resistance of each conductor respectively, then  $\frac{I}{R} = \frac{I}{r_1} + \frac{I}{r_2} + \frac{I}{r_3} + ...$  In Figure 4 there are three conductors, so that  $\frac{I}{R} = \frac{I}{r_1} + \frac{I}{r_2} + \frac{I}{r_3}$ .

When there are two circuits of resistance,  $r_1$  and  $r_2$  in parallel,  $\frac{I}{R} = \frac{I}{r_1} + \frac{I}{r_2}$  or  $R = \frac{r_1 r_2}{r_1 + r_2}$ .

If there be n circuits in parallel, each of the same resistance, then

$$\frac{I}{R} = \frac{I}{r_1} + \frac{I}{r_2} + \frac{I}{r} + \frac{I}{r} = \frac{n}{r}$$
or  $R = \frac{r}{n}$ .

Example.—Three coils, having a resistance of 10, 15, and 25 ohms respectively, are connected in series across 200 volts. What is the current flowing through the coils, and the voltage drop in each coil?

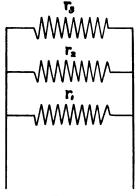


FIG. 4.

Figure 3 gives the diagram of connections for this circuit.

By Ohm's law 
$$C = \frac{E}{R}$$
.

Now E = 200 volts, and R =  $r_1 + r_2 + r_3 = 10 + 15 + 25$ = 50 ohms.

Then the current flowing =  $\frac{200}{50}$  = 4 ampères.

Volts drop in 
$$r_1 = Cr_1 = 4 \times 10 = 40$$
 volts  
,, ,, ,,  $r_2 = Cr_2 = 4 \times 15 = 60$  ,,  
,, ,,  $r_3 = Cr_3 = 4 \times 25 = 100$  ,,  
Total volts = 200.

Example.—In the previous example, if the three coils

be placed in parallel, what will be the combined resistance?

Now 
$$R = \frac{1}{r_1} + \frac{1}{r_2} + \frac{1}{r_3} = \frac{1}{10} + \frac{1}{15} + \frac{1}{25} = \frac{31}{150}$$
  
 $\therefore R = \frac{150}{31} = 4.8 \text{ ohms.}$ 

The resistance of the 3 coils in parallel is 4.8 ohms.

#### EFFECTS OF ELECTRIC CURRENTS

Heating Effect of the Electric Current.—The conversion of energy from an electrical form into that of heat takes place when a current flows through a conductor, the incandescent lamp being a particular example. The power, in watts, absorbed by a circuit is the product of the current in ampères and the fall of pressure in volts in that circuit. This may be expressed by the equation  $W = EC = C^2R$ , since E = CR. The energy in joules absorbed by this circuit in t seconds is equal to  $ECt = C^2Rt$ , since a joule equals a watt per second. If no mechanical work be done then all this energy is transformed into heat, and in doing this a certain amount of energy is expended.

There is a relation between the energy expended and the heat produced. This was first investigated by Joule in 1843. The method consisted in measuring the amount of mechanical work expended in stirring a known weight of water in a calorimeter, and in measuring the rise in temperature of the water. The relation is such that if 4.2×10<sup>7</sup> ergs, i.e. 4.2 joules, of work are done, a quantity of heat is developed sufficient to raise I gramme of water 1° C. This is known as the calorie, or the French unit of heat. (The British heat unit is the quantity of heat required to raise I lb. of water 1° F., and is equivalent to about 780 ft.-lbs. of work.)

Now C<sup>2</sup>Rt is also a measure of joules. Hence the quantity of heat H developed in t seconds in a circuit

of which the resistance is R ohms and current C ampères, is given by

 $H = \frac{C^2Rt}{4.2}$  calories = 0.24 C<sup>2</sup>Rt calories.

This is known as Joule's Law, and the heating effect as the Joule effect. It may be written thus. The heat generated in a simple circuit is proportional to the product of the square of the current into the resistance and the time during which the current continues to flow.

It is important to remember that the heat developed is proportional to C<sup>2</sup>, as this principle is applied to several

pieces of apparatus and measuring instruments used in electrical en-

gineering.

The heating effect of the electric current has now been utilised for heating and cooking purposes. Electric radiators are of the luminous and non-luminous types. A luminous radiator is merely a large lamp, and, as will be seen in the chapter on incandescent lamps, the energy transformed into heat is about 95 or 96 per cent., the remaining energy, be-

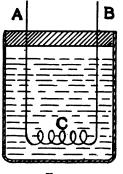


FIG. 5.

tween 4 and 5 per cent., being transformed into light. In the non-luminous radiator the current is passed through resistance wires embedded in cement or other

suitable insulating material.

Figure 5 shows an arrangement for heating a liquid. The ends, A and B, of an open coil C of a high resistance wire are connected to a source of electrical supply, and the coil is immersed in the liquid contained in a vessel. The heat generated raises the temperature of the liquid; some of the heat, however, is radiated from the sides of the vessel to the surrounding air, and consequently the efficiency is reduced to between 65 and 85 per cent. The time taken to raise the temperature to a definite value will depend upon the power

absorbed, and as an exercise in calculation some

examples will be worked.

Example.—An electric heater has an efficiency of 85 per cent., and works on a 230-volt circuit, taking 1.5 ampères. How long will it take to raise the temperature of 906 grammes of water to the boiling point if the initial temperature be 7° C.?

Calories in the water at boiling point

= mass in grammes × temperature rise in ° C.

 $= 906 \times 93.$ 

Power supplied in calories = 0.24 ECt

 $= 0.24 \times 230 \times 1.5 \times t.$ 

Now  $906 \times 93 \times \frac{100}{85} = 0.24 \times 230 \times 1.5 \times t$ 

.: time t taken to boil the water

 $= \frac{906 \times 93 \times 100}{230 \times 1.5 \times 85} = 1200 \text{ seconds}$ 

= 20 minutes.

Example.—If a water-heating vessel absorbs 1.5 ampères at 260 volts for 10 minutes in order to heat 0.5 kilogramme of water from 15° C. to 100° C., what is the efficiency of the apparatus?

Efficiency = calories in water at end of 10 minutes calories input

Calories in water at end of 10 minutes = mass x temp. rise

 $= 500 \times (100 - 15) = 500 \times 85.$ 

Calories input =  $0.24 \text{ È} \times \text{C} \times t$ 

 $= 0.24 \times 260 \times 1.5 \times 10 \times 60$ 

.. efficiency of apparatus

500×8<u>5</u> 0.24×260×1.5×10×60

= 75 per cent.

Chemical Effect of the Electric Current.—It has been shown that, when an electric current passes through a metallic conductor, a certain quantity of heat is developed in the conductor, but, after the conductor has become heated due to the passage of the current, in general there will be no chemical or physical change. Besides

metals, some liquids known as electrolytes conduct electricity, and the phenomena accompanying the passage of a current through these liquids will now be considered. Almost all liquids are compounds of two or more elements. Water, for instance, is a compound of the two elements hydrogen and oxygen in the proportion, by volume, of two of hydrogen to one of oxygen. Water is therefore denoted symbolically H<sub>2</sub>O. Again, copper sulphate, composed of 1 part of copper (Cu), 1 part of sulphur (S), and 4 parts of oxygen (O<sub>4</sub>), is symbolically

expressed by CuSO<sub>4</sub>.

When a current is passed through an electrolyte by inserting two plates into the solution (the plate connected to the positive pole of the supply mains being known as the anode and the other connected to the negative main, the cathode), decomposition of the electrolyte takes place. The products of decomposition, whether they be elements or compounds, will be liberated The elements or either at the anode or at the cathode. groups of elements liberated are called ions: the ion liberated at the anode is termed the anion, and that liberated at the cathode is termed the cation. The ions, such as the elements chlorine, iodine, and a number of acidic groups or salt radicals, such as SO4, which appear at the anode, are negatively electrified or convey negative electricity. The ions, such as hydrogen and the metals which travel to the cathode, are positively electrified or convey positive electricity.

Faraday deduced the laws which govern electrolysis, and hence they are known as Faraday's Laws, and are as

follows:

(1) The mass of any ion liberated is proportional to the quantity of electricity that has passed through.

(2) The mass of any ion liberated by a given quantity of electricity is proportional to the chemical

equivalent of the ion.

The Chemical Equivalent of an element is the weight of it which will combine with or replace I part by weight of hydrogen, and is numerically equal to the ratio of the atomic weight of the element to that of hydrogen divided by the valency: the valency of an element being

the number of hydrogen atoms which will combine with,

or are replaced by, one atom of the element.

The Electro-Chemical equivalent of an element is the weight in grammes which is deposited by the passage of unit quantity of electricity, i.e. one coulomb. Investigations show that, when a current of one ampère passes through a solution of silver nitrate for one second, the weight of silver deposited is 0.001118 grammes. The chemical equivalents of silver and hydrogen are 107.66 and 1 respectively, hence the electro-chemical equivalent of hydrogen is  $0.001118 \times 1/107.66 = 0.00001038$ . As another example, in the case of copper as a cuprous salt, the chemical equivalent of copper is 63.0, hence the electro-chemical equivalent of copper is  $0.00001038 \times \frac{63.0}{1} = 0.0006539$ . In a similar manner the electro-chemical equivalent of any other element may be determined.

Table III. gives for a number of elements their atomic weights, valency, chemical equivalent, and electrochemical equivalent; the latter being the weight in grammes liberated by one coulomb. Some elements, such as mercury, have different chemical equivalents in different compounds, so that the contituents of the compound must be known. The last column gives the approximate grammes deposited in one hour by one ampère.

Now it has been shown that the weight of an element liberated per second by one ampère is given by the electro-chemical equivalent usually denoted by the letter e, so that if C be the current flowing for t seconds, then the total weight W (in grammes) deposited is expressed

by  $W = e \times C \times t$ .

This is a very important relation, as it forms a means of measuring a current in ampères when that current is known to deposit a certain weight in a known time. Thus

$$C = \frac{W}{e t}$$

The apparatus used for this purpose is known as a

TABLE III TABLE OF ELECTRO-CHEMICAL EQIVALENTS

Element.	Symbol.	Atomic weight.	Valency.	Chemical equivalent.	Electro- chemical equivalent (grammes per coulomb).	Approximate grammes deposited in one hour by one ampere.
Electro-positive—	! !					
Copper	ł i		İ	}		
(cuprous) .	Cu	63.0	1	63.0	0.0006539	2.3665
Hydrogen .	H	1.0	1	1.0	0.00001038	0.037368
Mercury					Ū	
(mercurous).	Hg	199.8	I	199.8	0.002075	7.470
Potassium .	K	39.04	I	39.04	0.0004054	1.4594
Silver	Ag	107.66	I	107.66	811100.0	4.0250
Sodium	Na	22.99	1	22.99	0.0002387	0.8593
Copper (cupric)	Cu	63.0	2	31.5	0.0003271	1.1832
Iron (ferrous).	Fe	55.9	2	27.95	0.0002902	1.0436
Lead	Pb	206.4	2	103.2	0.001072	3.857
Mercury				-		
(mercuric) .	Hg	199.8	2	99.9	0.001037	3.733
Nickel	Ni	58.6	2	29.3	0.0003043	1.0993
Zinc	Zn	64.9	2	32.45	0.0003370	1.2113
Aluminium .	Al	27.3	3	9.1	0.00009450	0.3355
Electro-negative-		•	1	1		
Chlorine	Cl	35.37	1	35.37	0.0003673	1.3212
Iodine	I	126.53	I	126.53	0.001314	4.7304
Oxygen	0	15.96	2	7.98	0.00004850	0.29808
l	11			<u> </u>		

voltameter, a sketch of which is shown in Figure 6.

When the electrolyte is copper sulphate the two plates A and B are of copper and form the electrodes. If A be the positive plate, i.e. the plate by which the current enters the electrolyte, then the current flows through in the direction of the arrow, and copper will be deposited on the plate B. The solution used is a 15 per cent. solution of copper sulphate, to which about 2 per cent. of sulphuric acid is added to prevent the formation of basic sulphate.

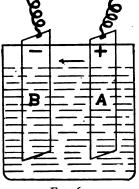


Fig. 6.

The cathode B should be sufficiently large to allow 50 square centimetres of surface per ampère.

The principles of electrolysis are applied to electroplating where the metal to be deposited in the form of a suitable salt in aqueous solution forms the electrolyte. The object to be plated is made the cathode, that is, it is suspended in the liquid and is connected to the negative pole of the dynamo or battery. The anode consists of a strip of the metal to be deposited.

These principles have also been employed in the separation of the elements such as aluminium, sodium,

and potassium.

Example.—What weight of copper will be deposited in a copper voltameter by a current of 10 ampères flowing for 1 hour?

From Table III. the electro-chemical equivalent of

cupric copper = 0.0003271.

The weight deposited =  $e \times C \times t$ = 0.0003271 × 10 × 1 × 3600 = 11.8 grammes.

Example.—Taking the electro-chemical equivalent of silver as 0.001118, calculate the current required to deposit a coating of silver 0.1 millimetre thick to a surface of 1000 square centimetres in one hour.

Density of silver = 10.5.

Volume of silver deposited = 1000 x 0.01 = 10 cubic centimetres.

Mass of silver deposited = 10 × 10.5 = 105 grammes. 1 coulomb deposited 0.001118 grammes

∴ the current required = 
$$\frac{W}{e t}$$
  
=  $\frac{105}{0.001118 \times 3600}$  = 26 ampères.

Example.—An ammeter was connected in series with a silver voltameter and a current sent through: at the end of 30 minutes a weight of 205 grammes was deposited. The current was maintained steady during the test and indicated 99 ampères. Did the ammeter read correctly; if not, what was the error?

The current passing through the ammeter and voltameter

$$=\frac{W}{e \times t} = \frac{205}{0.001118 \times 1800} = 101$$
 ampères.

Ammeter read low by 2 per cent.

#### CHAPTER III

# ELECTRO-MAGNETISM AND MAGNETISATION OF IRON

When a current flows through a circuit, magnetic lines of force are invariably set up around the circuit, causing it to act magnetically on any body in the vicinity. This is known as the magnetic effect of an electric current, but the reason why an electric current is accompanied by a magnetic field is a matter of hypothesis. This phenomenon is known as electromagnetism, and forms the foundation of the science of electrical engineering. It is therefore of great importance, and before progress can be made in the study of electrical engineering the principles of electro-magnetism must be thoroughly understood, As an introduction some of the terms employed will be briefly defined.

Permeability.—As mentioned in the preceding chapter certain substances are better conductors of electricity than others, so, also, there are good and bad conductors of magnetic lines of force. Permeability is the term employed to express the relative magnetic conductance of materials. The permeability of air is taken as unity, and the relative permeability of other substances is usually expressed symbolically by the Greek letter  $\mu$ . The permeability of non-magnetic materials is a little less than 1, but for practical purposes may be taken also as unity. For magnetic materials, e.g. iron, steel, nickel, and cobalt, the value of  $\mu$  is much greater than 1, attaining a value as high as 900 for steel and 3600 in the case of soft iron.

Intensity of Magnetisation.—In a long bar magnet of length l, area of cross-section a, and ends having a pole

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strength *m*, the intensity of magnetisation I is the ratio of the magnetic moment of the magnet to its volume. The magnetic moment of a magnet is the product of its pole strength into the length of the magnet. Therefore the intensity of magnetisation is given by

$$I = \frac{\text{magnetic moment}}{\text{volume of magnet}} = \frac{ml}{al} = \frac{m}{a}.$$

In other words, the intensity of magnetisation is the pole strength per unit area.

Lines of Force per Unit Magnetic Pole.—Suppose a magnetic pole of strength m units be isolated from all magnetic fields, and that the pole is the centre of an infinitely thin spherical surface of radius r, then the number of lines of force cutting unit area of the spherical surface  $=\frac{m}{r^2}$ . Now the area of a sphere  $=4\pi r^2$ , therefore the total number of lines of force cutting the sphere  $=4\pi r^2 \times \frac{m}{r^2} = 4\pi m$ .

If m = 1, the number of lines =  $4\pi$ , that is unit magnetic pole has  $4\pi$  lines of force emanating from it.

Magnetic Induction.—If a long thin rod of iron be placed in a magnetic field of intensity H in air with its length parallel to the lines of force of the field, then the total number of lines of force cutting unit area of the bar is given by

$$B = H + 4\pi \frac{m}{a} = H + 4\pi I$$

where m = the pole strength developed at the end of the iron, a the area of cross-section of the iron, and I the intensity of magnetisation. The ratio  $\frac{B}{H}$  gives the

permeability  $\mu$  of the iron, i.e.  $\frac{B}{H} = \mu$ —one of the fundamental equations of magnetism. H is the magnetising force and may be looked upon as a stress, while B, the number of lines of force passing through unit area is the resultant strain. B is termed the *Induction density* in lines per square centimetre or square inch, and may

be as high as 16,000 per square centimetre in cast steel or wrought iron, but seldom exceeds 9000 per square centimetre for cast iron. The total number of lines of force N passing through a magnet having an area of cross-section  $\alpha$  is given by  $N = B\alpha$ ,

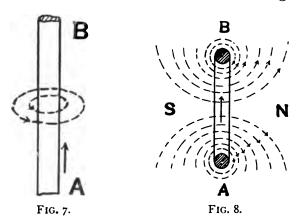
so that 
$$B = \frac{N}{a}$$
,

N being termed the *total magnetic flux*. For instance, if the total number of lines of force passing through a magnet be 70,000, and the area of cross-section 7 square centimetres, then the induction density is given by

B = 
$$\frac{N}{a}$$
 =  $\frac{70,000}{7}$  = 10,000 lines per square centimetre.

MAGNETIC FIELD PRODUCED BY AN ELECTRIC CURRENT

Magnetic Field surrounding a Conductor.—When a direct current traverses a straight conductor, the conductor is surrounded along its entire length by concentric circles of lines of force, as shown in Figure 7, in



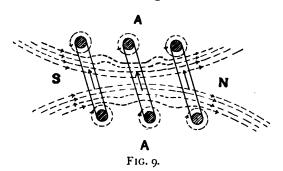
which AB is the conductor. The direction of the lines of force depends upon the direction in which the current flows. Referring to the figure, if the current flow from A to B, the direction of the lines of force is as indicated by the arrow heads, but if the current flow from B to

A, then the direction of the lines of force will also be reversed. This is the starting-point in the theory of electro-magnetism.

The magnetic effect, when a wire carrying current is bent into a circular loop, is shown in Figure 8, which is a vertical section. The direction of the current in the part of the loop shown is indicated by the arrow, and the field by the dotted lines, the direction being indicated by the arrow-heads. At A the lines of force are in a clock-wise direction, but in a counter-clock direction at B. As all the lines of force enter into one face of the loop and leave at the other, the loop may be considered a magnet having north and south poles, as indicated by N and S. If C be the current in ampères flowing in a loop of radius r centimetres, then the magnetic force H at the centre of the loop

$$=\frac{2\pi C}{10r}$$
 C.G.S. units.

Magnetic Field of a Solenoid.—Consider several loops of wire side by side in a straight line carrying current. This is best effected by coiling up a length of insulated wire into a number of turns. Such an arrangement is called a solenoid, and Figure 9 shows a vertical



section through one consisting of 3 turns. The arrows indicate the direction in which the current is flowing, and lines of force are set up around each conductor as shown by the dotted lines. Inside the solenoid all the lines of force due to each coil have a common direction, and the resultant field is in the direction SN; outside

the solenoid the direction is NAS. Thus the lines of force flow through the solenoid from S to N, and emanating from the end N, complete their paths outside the coil and re-enter again at the end S. There is a crowding of the lines of force inside the solenoid and a spreading outside, as indicated in Figures 9 and 10.

Magnetising Force.—Referring to Figure 10, let 1 be the length of the solenoid in centimetres, T the number of turns, and C the current in ampères. If the coil be wound uniformly on a cylinder of non-magnetic material

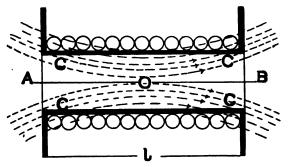


FIG. 10.—Magnetic field due to a solenoid.

the magnetic force inside the cylinder parallel to the axis is given by the equation

$$\ddot{H} = 4\pi ni$$
 C.G.S. units \*

where n is the turns of wire per unit length of the cylinder and i is the current flowing in absolute units.

In this case 
$$i = \frac{C}{10}$$
 and  $n = \frac{T}{l}$  so that
$$H = \frac{4\pi CT}{10 l}$$

but 
$$\frac{4\pi}{10}$$
 = 1.25, therefore H = 1.25  $\frac{CT}{\ell}$ .

CT is usually considered as one term and is referred to as the *ampère-turns*, and for a given solenoid H is a constant for all combinations of C and T which make CT a constant. The magnetising force H will be the

<sup>\*</sup> For proof see J. J. Thomson's *Electricity and Magnetism*, 3rd edition, chap. x. pp. 340-345.

same for two coils having the same dimensions, but one having 100 turns and carrying 10 ampères, while the other has only 50 turns but carries 20 ampères, the product being 1000 in both cases. The above formula is theoretically correct only for solenoids which are very long compared with their diameter, but in practical applications it is sufficiently accurate for any solenoid. The magnetic field inside a solenoid is strongest at its centre O. Since, however, there is no iron to guide the lines of force, they leak out sideways at or near the ends. The field is therefore more dense at the sides CC than near the axis AB, and consequently the field is stronger at the sides CC than at AB. This latter property of the solenoid is made use of to effect the movement of the needle in a class of indicating instrument of the moving soft-iron type.

The interior of the solenoid being of air, the value of  $\mu$  is unity; therefore since  $\frac{B}{H} = \mu$ , B = H. That is, inside a coreless solenoid the value of H is always the number of lines of force per square centimetre.

### THE MAGNETIC CIRCUIT

Lines of force are continuous and unbroken throughout their entire length, and for the sake of convenience are treated as if they have a material existence and flow in definite numbers along definite paths. The paths followed by lines of force are called magnetic circuits, for the same reason that the path taken by an electric current is called the electric circuit. Iron, steel, nickel, and cobalt are, as already stated, the best conductors of magnetic lines of force, but for the magnetic circuits in practical machines and instruments, iron and steel alone are used, being cheaper and more easily worked than the other metals named.

There is a remarkable similarity between the electric and magnetic circuits, although the latter is not so well defined as the former. Leakage from the main circuit takes place in each; in one case there is a leakage of lines of force, and in the other a leakage of current.

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The laws of leakage are the same, namely, that leakage takes place across the paths of least resistance. The

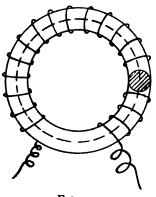


FIG. 11.

total flux generated in a magnetic substance depends both on the magnetising force and the permeability of the material.

The simplest case of the magnetic circuit is an iron ring of circular cross-section, as shown in Figure 11. Suppose the ring to have a mean length of l centimetres, an area of cross-section of a square centimetres, and be wound with a magnetising coil of l turns.

Then, when a current of C ampères flows through the coil, the magnetising force is given by

$$H = 1.25 \frac{CT}{l}.$$

The magnetic flux through the iron = N = Ba, but  $B = \mu H$ , therefore  $N = \mu Ha$ 

$$=\frac{\mu \cdot 1.25 \text{ CT}a}{l} = \frac{1.25 \cdot \text{CT}}{\frac{l}{a} \cdot \frac{1}{\mu}}.$$

This expression is analogous to the expression for Ohm's law in the electric circuit.

By Ohm's law, current =  $\frac{\text{electromotive force (E.M.F.)}}{\text{resistance}}$ and from the previous equation

number of lines of force =  $\frac{\text{magnetomotive force }(M.M.F.)}{\text{reluctance}}$ 

Where magnetomotive force = 1.25 CT Number of lines of force = N Reluctance =  $\frac{l}{a} \cdot \frac{1}{\mu}$ .

The equation for reluctance is also comparable with

the equation for the resistance of a wire. In the case of the resistance of a wire

Resistance = 
$$\frac{\rho \times l}{a}$$
 =  $\frac{\text{specific resistance} \times \text{length}}{\text{area of cross-section}}$ 

In the magnetic circuit

Reluctance = 
$$\frac{l}{a} \cdot \frac{1}{\mu}$$
.

The reciprocal  $\frac{I}{\mu}$  is termed the reluctivity of the magnetic substance

$$\therefore \text{ reluctance} = \frac{\text{reluctivity} \times \text{length}}{\text{area of cross-section}}$$

Reluctivity might, therefore, be defined as the magnetic resistance offered to magnetic flux between

two opposite faces of a unit cube of the substance, but this definition is never employed, as the reluctivity of a substance varies with the flux density B, whereas the specific resistance of a conductor is independent of the current flowing through it.

In practical cases the magnetic circuit generally consists of a number of paths in series, each part having a different reluctance. Figure 12 represents the magnetic circuit of a two-pole dynamo, in which there are indicated the following parts—(1) the armature A; (2) the

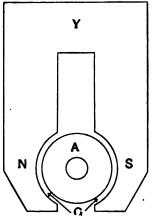


FIG. 12.—Magnetic circuit of a two-pole dynamo.

air-gap G; (3) the poles N and S; and (4) the yoke Y. Since each part of the circuit is in series, the total reluctance is obtained by adding together the reluctances of the different portions. Then if

 $l_1 l_2 l_3$  . . . be the lengths of respective parts,  $a_1 a_2 a_3$  . . . be the areas of respective parts, and  $\mu_1 \mu_2 \mu_3$  . . . be the permeabilities of respective parts,

the general equation for the total reluctance is given by

Reluctance = 
$$\frac{l_1}{a_1\mu_1} + \frac{l_2}{a_2\mu_2} + \frac{l_3}{a_3\mu_3} + \dots$$
Therefore N =  $\frac{1.25 \text{ CT}}{\left(\frac{l_1}{a_1\mu_1} + \frac{l_2}{a_2\mu_2} + \frac{l_3}{a_3\mu_3} + \dots\right)}$ 

This formula was introduced by the late Dr. John Hopkinson, and is applied in a modified form to calculations relating to the magnetic circuit of dynamos and electro-magnetic mechanism. In practical problems the ampère-turns CT is generally the unknown, and for determining its value the equation may be written as follows:

$$CT = N\left(\frac{l_1}{a_1\mu_1} + \frac{l_2}{a_2\mu_2} + \frac{l_3}{a_3\mu_3} + \dots\right)$$
or 
$$CT = 0.8\left(\frac{Nl_1}{a_1\mu_1} + \frac{Nl_2}{a_2\mu_2} + \frac{Nl_3}{l_3\mu_3} + \dots\right)$$
or 
$$CT = 0.8\left(\frac{B_1l_1}{\mu_1} + \frac{B_2l_2}{\mu_2} + \frac{B_3l_3}{\mu_3} + \dots\right)$$
where  $B_1$ ,  $B_2$ ,  $B_3$  . . . are the induction densities of each part. If the symbol  $\Sigma$  denote the sum of all such terms as  $\frac{Bl}{\mu}$ , the above equation may be written in the form

$$CT = 0.8 \Sigma \frac{Bl}{\mu}$$
.

Magnetic Leakage.—In the electric circuit it is comparatively easy to confine the current to a definite path, because some materials have practically infinite resistance. In the magnetic circuit, however, air and the other so-called non-magnetic materials have a permeability which, at the very best, is as high as  $\frac{1}{2500}$  that of iron. There is thus no possibility of magnetically insulating any circuit to anything like the extent attainable in the electric circuit; consequently, leakage lines must be allowed for. This leakage of lines attains to appreciable

dimensions in dynamos and other apparatus where the magnetic circuit is composite in character. Suppose a flux of  $N_a$  lines is required to pass through the armature of a dynamo; since the lines of force have to cross an airgap, a considerable amount of leakage will take place. A flux equal to  $N_m$  lines must therefore be generated in the magnet, so that  $N_m = N_a + \text{leakage lines}$ . Dr. Hopkinson presented this fact by stating that  $N_m$  lines through the magnet were v times the lines through the armature, i.e.  $N_m = vN_a$ . The ratio  $N_m/N_a$  is termed the coefficient of magnetic leakage. Hence

$$v = \frac{\text{total flux generated}}{\text{useful flux}}$$
.

The value of  $\nu$  varies between 1.1 and 1.5, depending

upon the permeability of the leakage paths.

Example. — A solenoid 20.5 centimetres long is wound on a brass former and has an internal diameter of 10 centimetres. It is wound to the depth of 2.5 centimetres with 2500 turns of wire, and carries 1 ampère. Find (1) the magnetising force, and (2) the flux at the centre of the solenoid.

(1) The magnetising force  $H = \frac{1.25}{l} \frac{CT}{l}$ .

Now l = 20.5 centimetres.

C = 1 ampère T = 2500

$$\therefore H = \frac{1.25 \times 1 \times 2500}{20.5} = 153.$$

(2) Since the coil has no iron core

$$B = H$$

and the flux at the centre of the solenoid = N = Ba.

Now  $a = \frac{\pi d^2}{4}$  where d is the mean diameter of the

solenoid and =  $\frac{10+15}{2}$  = 12.5 centimetres;

thus  $a = \frac{\pi \times 12.5^2}{4} = 126$  square centimetres.

 $\therefore N = B \times a = 153 \times 126$ = 19,300 lines.

Example.—A cast-iron ring has a cross-section of 4

square centimetres and a length of 20 centimetres. Calculate the ampère-turns required to drive a flux of 32,000 through the iron, permeability of the iron being 100. Figure 11 shows a diagram of such a circuit.

Starting with the fundamental equation

the ampère-turns = 
$$CT = \frac{Hl}{1.25} = 0.8 Hl$$
  

$$= 0.8 \frac{Bl}{\mu} = 0.8 \frac{Nl}{a\mu}$$

$$= \frac{0.8 \times 32,000 \times 20}{4 \times 100} = 1280.$$

Example.—In the previous example find the additional ampère-turns if an air-gap 0.5 centimetre wide be cut in the iron ring. The coefficient of leakage  $\nu$  may be taken as 1.2.

From the above the ampère-turns = 
$$CT = \frac{0.8N\ell}{a\mu}$$
.

In the air-gap 
$$N = \frac{32,000}{v} = \frac{32,000}{1.2}$$

u=1, l=0.5, and a=4, the same as the iron, this being on the assumption that no spreading of the lines of force takes place in the air-gap. Figure 13 shows the ring with the air-gap introduced, the leakage lines also being indicated.

The additional ampère-turns to drive the flux through the air-gap =  $\frac{0.8 \times 32,000 \times 0.5}{4 \times 1 \times 1.2}$  = 2660.

This example shows very clearly the effect of introducing a small air-gap into the magnetic circuit, namely, that the ampère-turns required to drive the flux through the magnetic circuit must be considerably increased, so that to be economical the air-gap in all magnetic circuits should be as small as possible.

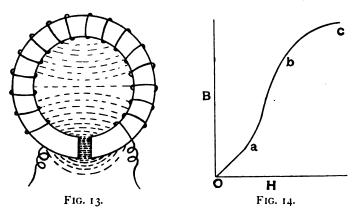
Example.—An iron ring 3 square centimetres in cross-section and 50 centimetres in mean circumference is wound with a coil of 100 turns. It is found that a current of 8 ampères produces a flux of 40,000 lines.

Find the permeability of the iron.

Now (1) H = 1.25 
$$\frac{CT}{l}$$
  
and (2) H =  $\frac{B}{\mu} = \frac{N}{a\mu}$   
therefore  $\frac{N}{a\mu} = 1.25 \frac{CT}{l}$   
then the permeability  $\mu = \frac{N}{a} \cdot \frac{l}{1.25 \text{ CT}}$   
=  $\frac{40,000 \times 50}{3 \times 1.25 \times 8 \times 100}$   
= 660.

#### Magnetisation Curves

The manner in which the induction density B of a magnetic material varies with the magnetising force H



will now be examined. Unfortunately, these quantities are not connected by any simple relation, but the most convenient mode of studying them is to plot corresponding values of B and H on squared paper, taking values of H as abscissæ and values of B as ordinates. The curve obtained by joining up the various points is known as the magnetisation or B-H curve. Methods of measuring B and H are described on pages 46 to 52, but for the present it will be assumed that both quantities have been obtained. Figure 14 represents the

characteristic form of curve obtained with soft iron or steel. In the first part of the curve, between O and a, the induction B gradually increases as the magnetising force increases; between a and b a small increase in H causes B to increase very rapidly. After the point c has been reached the curve becomes almost flat, showing that a large increase in H produces a very small increase

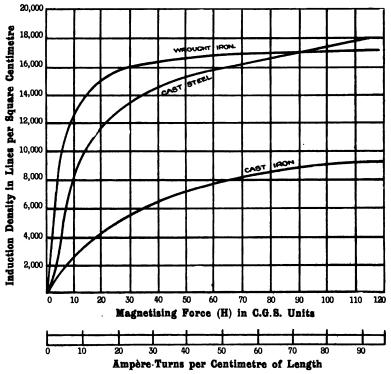


FIG. 15.—Magnetisation curves for iron and steel.

in B. The part bc is known as the knee of the curve, and at the point c the iron is said to be practically saturated. Any further increase in the induction above this is due to the coil alone.

Figure 15 gives the B-H curves for wrought iron, cast steel, and cast iron, these being the magnetic materials invariably employed. It should be noted that wrought iron and cast steel give a much higher induction for a given value of H than cast iron. Reference to these

curves shows that it is not economical to work wrought iron or cast steel at greater inductions than 16,000 lines per square centimetre, whereas the limiting induction for cast iron is about 9000 lines per square centimetre.

Since the magnetising force  $H = 1.25 \frac{CT}{l}$  the ampèreturns per centimetre of length is given by

$$\frac{\text{CT}}{l} = \frac{\text{H}}{1.25} = 0.8 \text{ H} = 0.8 \frac{\text{B}}{\mu}.$$

It is more convenient to express the induction density B of a circuit in terms of the ampère-turns per centimetre of length, and this relation is given for the curves in Figure 15. The ampère-turns per centimetre corresponding to particular values of H have been marked off along the abscissæ.

The makers of different brands of iron usually supply a curve showing this relation, and by making use of it laborious calculations are avoided; in fact these curves are invariably used in calculations relating to magnetic circuits. In order to make the use of these curves perfectly clear an example will be worked.

Example.—The yoke of a two-pole dynamo is of cast steel and carries a flux of 1.12 million lines; the area of cross-section is 80 square centimetres and the length 40 centimetres. What is the value of the ampère-turns necessary to drive this flux through the yoke?

$$B = \frac{N}{a} = \frac{1,120,000}{80} = 14,000.$$

From the curve for cast steel in Figure 15 a value of B = 14,000 requires 28 ampère-turns per centimetre of length. Therefore the total ampère-turns to drive the flux through the yoke =  $28 \times 40 = 1120$ .

At any point on these curves the ratio of B to H gives the value of the permeability  $\mu$ , and the relation between  $\mu$  and B for wrought iron is shown in Figure 16. The permeability rapidly increases to a maximum value of 2400, corresponding to B=6000; with higher values of B the permeability diminishes, and with very high

inductions, such as those occurring in the teeth of armatures, the permeability may be as low as only 10 or 20 times that of air.

The value of the permeability, and, consequently, the shape of the B-H curve, also depends upon the chemical and physical state of the iron. In general all substances mixed with or alloyed with iron lower the permeability. In steel and cast iron it would appear

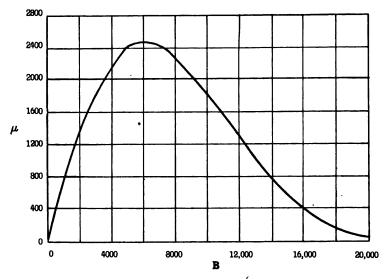


FIG. 16.—Permeability curves for wrought iron.

that the decrease in the permeability is proportional to the amount of carbon present; carbon in the uncombined forms lowers the permeability less than when combined. Figure 17 shows curves for three different grades of cast iron, carbon being present in the following quantities:

Sample.	Per cent. of combined carbon.	Per cent. of uncombined carbon.
Α	0.78	•••
В	0.565	2.98
C	0.198	3.29

These curves clearly show the effect of combined carbon upon the permeability. The cast iron in general use for magnetic purposes would be between the curves B and C.

In cast iron and steel such substances as aluminium and silicon, which tend to give softness and homogeneity to the metal, increase the permeability when present in limited quantities, say from 2 to 2.5 per cent. Figure 18 represents some of the curves from Professor Barrett's paper on "Magnetic Properties of Iron Alloys." A, B, and C are the curves for (i) pure Swedish charcoal iron,

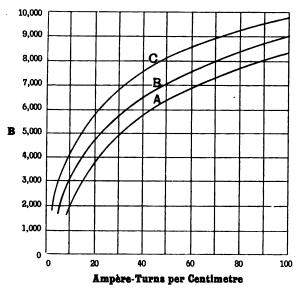


FIG. 17.—Curves for iron containing different percentages of combined and uncombined carbon.

(ii) iron containing 2.5 per cent. silicon, and (iii) iron containing 2.25 per cent. aluminium. Curve C shows the remarkable increase in permeability due to the addition of 2.25 per cent. aluminium to the pure iron.

Rate of cooling also affects the permeability of the iron, the permeability being considerably lowered if cooling takes place too rapidly. On the other hand annealing increases the permeability. Temperature also affects the permeability, but as this effect is hardly

<sup>\*</sup> Journal of Institution of Electrical Engineers, vol. xxxi. pp. 672-721.

noticeable within the range of temperatures that occur in practice, it need not be further considered.

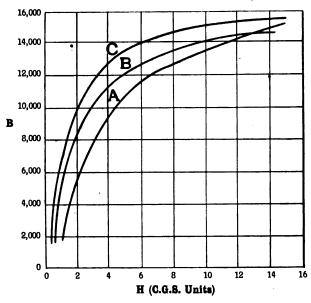


FIG. 18.—Magnetisation curves for—

- A. Pure Swedish charcoal iron.
- B. Iron containing 2.5 per cent. silicon.
- C. Iron containing 2.25 per cent. aluminium.

## METHODS OF MEASURING PERMEABILITY

In order to determine the permeability of a substance, in general, the induction density B corresponding to a given value of H must first be measured and the permeability obtained from the equation  $\mu = \frac{B}{H}$ . Various instruments have been devised with a view to making the permeability tests as simple as possible, but the most accurate, and also the most laborious, is that known as the Absolute or Ballistic method, which will now be described.

Ballistic Method.—In this method, advantage is taken of the fact that if the magnetic flux through any circuit (e.g. a coil of wire) is suddenly altered, a current

is induced in the circuit during the change, the total quantity of electricity induced being proportional to the change in the magnetic flux. By connecting a ballistic galvanometer in series with the conducting circuit the quantity of electricity induced can be measured, and knowing the galvanometer constant the change in the lines of force can be computed. The value of the magnetising force H required to produce the change in the induction can be calculated by knowing the number of the turns per centimetre of length and the current flowing through the magnetising coil.

Referring to Figure 19, the sample of iron to be tested

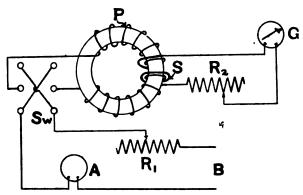


FIG. 19.—Diagram of connections for ballistic method of testing iron.

is made in the form of a ring and wound uniformly with a magnetising coil P, which is connected through a reversing switch Sw, regulating resistance R<sub>1</sub>, and an ammeter A to a battery or other source of E.M.F. B. A search coil S is wound on the ring and is connected in series with a variable resistance R<sub>2</sub> to the ballistic galvanometer G.

The value of the magnetising force H produced by the coil P is obtained directly from the formula  $H = \frac{1.25 \text{ CT}}{l}$ , where C = current in ampères flowing through

the coil, and  $\frac{T}{I}$  = turns per centimetre length of the coil.

The induction density B corresponding to a given

value of H is obtained by suddenly reversing the current in the magnetising coil by means of the switch Sw, and noting the deflection of the galvanometer. Let N= total number of lines of force passing through the ring at the instant of reversal, and A= area of cross-section of the iron, then the induction density  $B=\frac{N}{A}$ . Now the E.M.F.

induced in the search coil is proportional to the rate of cutting of lines of force, and is given by the equation

$$E = \frac{N_1 m}{t} \times 10^{-8} \text{ volts.}$$

Where  $N_1 = \text{total change in lines of force}$ 

t = time in seconds during which the change takes place

m = turns on the search coil.

The current flowing in the search coil circuit is given by

C (ampères) = 
$$\frac{E \text{ (volts)}}{R \text{ (ohms)}}$$
.

Since E = induced E.M.F. =  $\frac{N_1 m}{t}$ . 10<sup>-8</sup>

and R = resistance of galvanometer circuit, the current in ampères =  $C = \frac{N_1 m \cdot 10^{-8}}{t \text{ R}}$ .

The quantity of electricity flowing in the galvanometer  $= Q = Ct = \frac{N_1 m \cdot 10^{-8}}{tR} t = \frac{N_1 m \cdot 10^{-8}}{R}.$ 

When the magnetising current is reversed the total change in the lines of force =  $N_1 = 2N = 2BA$ , therefore  $Q = \frac{2BAm \cdot 10^{-8}}{R}$ .

If  $\theta$  be the deflection of the galvanometer and  $K_1$  the ballistic constant, *i.e.* the quantity of electricity required to give a deflection of one division, then  $Q = K_1\theta$ .

That is, 
$$K_1 \theta = \frac{2BAm \cdot 10^{-8}}{R}$$
  
or  $B = \frac{RK_1 10^8}{2Am} \cdot \theta$ .

But R,  $K_1$ , and m are known quantities, and for a

particular test can remain constant, in which case the equation may be written  $B = K\theta$ ,

where  $K = \frac{R \cdot K_{110}^8}{2Am}$ .

So that by determining H and B as above the permeability  $\mu$  of a specimen of iron is given by B/H.

The magnetising current C can be set to any desired value by means of the variable resistance R<sub>1</sub>. The resistance R<sub>2</sub> in series with the galvanometer should be sufficient to keep the deflections within the scale limits, when the maximum change in the lines of force takes place.

For this test the ring should have a sectional area of about 3 square centimetres and a mean length of 30 centimetres. An inherent disadvantage of this method is that a special ring has to be forged, so that the ballistic test is very seldom used in practical work. It has been described here because it illustrates the application of a number of fundamental principles.

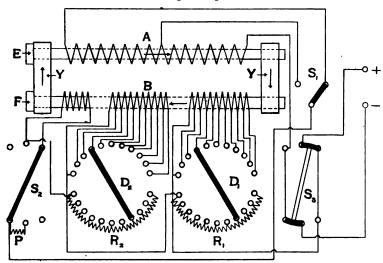


FIG. 20.—Diagram of connections for Ewing's permeability bridge.

Ewing's Permeability Bridge.—This instrument has been devised by Professor Ewing for measuring the permeability of a sample of iron by comparison with a standard test-piece, the B-H curve of which has been determined beforehand. Figure 20 gives a diagram of

connections for the instrument. The bar F to be tested is turned to the same diameter as the standard bar E, and they are then placed inside two parallel magnetising coils, A and B respectively. The ends of the bars fit accurately into two soft-iron yokes Y, which make good magnetic contact between the bars by means of pinching screws. From the soft-iron yokes Y two long soft-iron horns H (Fig. 21) project vertically upwards and are so shaped that they almost meet at the top. In the gap between the ends D is placed a magnetic needle N, the sensibility of which depends on the position of the controlling magnet M. The two magnetising coils A

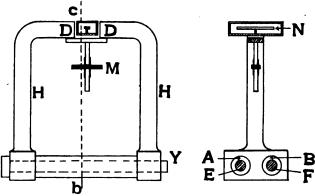


FIG. 21.—Construction of Ewing's permeability bridge.

and B are wound on brass formers and connected in series. The coil A, inside which is placed the standard bar E, consists of either 50 or 100 turns, depending upon the position of the switch S<sub>1</sub>. The second coil B, surrounding the sample of iron to be tested, has 210 turns; of these 10 are controlled by the dial D<sub>1</sub>, 100 by the dial D<sub>2</sub>, and 100 by the switch S<sub>2</sub>. By this arrangement the number of turns constituting the coil B may be varied. The coils A and B are so connected that the resultant magnetism forms a closed magnetic circuit through the two test bars, by way of the soft-iron yokes as shown by the arrows in Figure 20. +and - are the instrument terminals across which 6 or 7 cells are connected, the current taken from the cells being measured

by an ammeter.  $S_3$  is the reversing switch for changing the direction of the magnetising current. To compensate for the variation in resistance when the number of turns forming the coil B are varied, an exactly equal resistance is put into circuit by means of the dial switches. The resistances are shown at  $R_1$  and  $R_2$  on the dials of  $D_1$  and  $D_2$  respectively. The resistance P is likewise introduced when the 100 turns controlled by the switch  $S_2$  is cut out of circuit.

The principle of the instrument is as follows:

When a current is passed through the two magnetising coils A and B a flux is set up in each bar, the fluxes respectively depending upon the permeability of the bars. If the permeability of E and F be equal the flux set up in each bar would be the same, and practically all the lines of force would flow in the path indicated by the arrows. If the permeability of E be greater than that of F, then the flux set up in E will be greater than that in F, and there will be a magnetic difference of potential between the two yokes, and leakage lines of force will pass through the horns and air-gap between DD: this causes the needle N to be deflected, and the amount of deflection is directly proportional to the number of leakage lines. In using the instrument the number of turns forming the coil B are varied until the needle N shows no deflection, in which case the leakage lines are eliminated and the flux through the bar E equals the flux through F. Since the areas of E and F are the same, then the induction density in E equals the induction density in F, i.e.  $B_E = B_F$ . Now  $H_E = \frac{4\pi A T_E}{10l}$ , but the clear length of each bar is 12.56 centimetres  $(4\pi)$ , and the number of turns in the magnetising coil of the standard bar is 100. Hence the magnetising force due to coil A is 10 C.G.S. units for each ampère of current. allows any required magnetising force to be easily applied, with the aid of the ammeter and adjustable resistance in series with the cells. Further, since the relation of B to H is known for the standard bar, a knowledge of the current is enough to show at what value of the induction B the comparison is being made, and B is, of course, the same for both bars, when the condition of

balance is produced. The number of turns on the bar F divided by 100 gives the ratio of the magnetising force required for that bar, to the known force applied to the standard. Because  $H_F = \frac{4\pi A T_F}{10l} = \frac{4\pi A T_F}{10 \times 12.56} = \frac{AT_F}{10}$ , and from above  $H_E = \frac{AT_E}{10} = \frac{A}{10}$ . 100

Therefore  $\frac{H_F}{H_F} = \frac{T_F}{100}$ , or  $H_F = \frac{T_F}{100}$ .

Knowing  $H_E$ ,  $B_E$  can be computed from the B-H curve of the standard, and therefore  $B_F$ , since  $B_F = B_E$ . Hence a point on the B-H curve of the iron under test is determined, and by changing the current, as many points as are desired may be found.

In order to get rid of residual magnetism effects in the test-pieces, yokes, and horns, the direction of the magnetising current is frequently reversed by means of the switch S<sub>3</sub>. In testing iron of poor magnetic quality it is necessary, in order to obtain a balance, to use only 50 turns around the standard.

## MAGNETIC HYSTERESIS

When a magnetic substance has been magnetised in a strong magnetic field it will be found to retain a considerable proportion of magnetism after the magnetising force has been removed. This, as will be shown, is a very important phenomenon. Take a sample of annealed wrought iron which has been previously demagnetised, then, when the magnetising force is first applied the induction B varies with H in a manner represented by the curve OA in Figure 22, which is similar in form to the curve for wrought iron in Figure 15. After having reached the point A on the ascending curve let the magnetising force be gradually reduced from A to O again. It will be found that the descending curve is not, by any means, identical with the ascending curve, but is considerably higher, as shown by the part AR. It will further be noticed that when the magnetising force is zero the

or of the current through the magnetising force is reversed, by reversing the direction of the iron, i.e. the lines of force per square centimetre passing through the iron when the magnetising force has been entirely withdrawn. When the magnetising force is reversed, by reversing the direction of the current through the magnetising coil, the iron rapidly loses its magnetism, and a negative force,

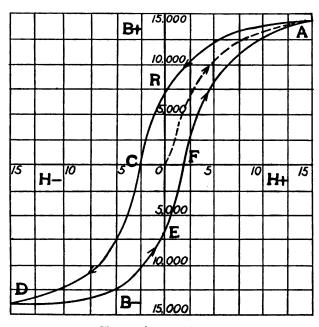


FIG. 22.—Hysteresis curve for wrought iron.

represented by OC, is sufficient to deprive the iron of all its magnetism. When the negative magnetising force is increased beyond OC the iron becomes negatively magnetised and reaches a maximum at the point D. At this point the induction B is of the same numerical value as at the point A, but of the opposite sign. After the magnetising force is again reversed it requires a positive force equal to OF to deprive the iron of its negative magnetism. Lastly, by increasing the magnetising force from O to the same positive maximum as at

first, the curve EFA is obtained. A loop ARCDEFA has then been described, and is known as a complete magnetic cycle. If the cycle of operations be repeated a curve identical with ARCDEFA will be obtained.

Professor Ewing was the first to point out this lagging of the induction behind the magnetising force. The phenomenon is known as magnetic hysteresis, and the curves enclosing the area ARCDEFA is known as the B-H curve of hysteresis. On examining this curve it will be seen that when H is reduced to O, B still has a considerable value, OR; this is termed the retentivity. To reduce the induction to zero a negative or demagnetising force, represented by OC, has to be applied; this is called the coercive force. The return half DEFA of the curve is a repetition of the first half ARCD, and OE = OR, and OF = OC.

If a similar test be performed on a ring of sheet iron for armature cores, a loop such as is represented by ARCDEF in Figure 25 will be obtained. Every kind of magnetisable substance shows this phenomenon in

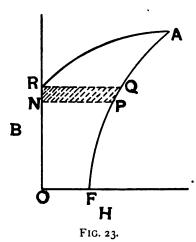
varying degrees.

Dissipation of Energy through Magnetic Hysteresis.— One very important consequence of magnetic hysteresis is that changes of magnetisation involve a dissipation of energy. When, for instance, a piece of iron is magnetised, a certain amount of work is done in overcoming the molecular friction of the iron, i.e. work is done in the process of magnetisation, and if there were no energy retained by the iron it would return to its original state on withdrawing the magnetising force. This is known not to be the case; in fact, in order to demagnetise the iron a reverse force has to be applied, that is, work has to be done in demagnetising the iron. The law of the conservation of energy states that no energy can be lost, but is convertible from one form to another. Experiment shows that the energy retained by the iron is converted into heat, and the iron, or any other magnetisable substance which goes through magnetising and demagnetising cycles, becomes heated. Hence, whenever the phenomenon of magnetic hysteresis occurs, energy

is expended and work done, and it will be shown that the work done is proportional to the area of the hysteresis loop.

The problem now is to find the work done when a sample of iron, having a length  $\ell$  and area of cross-

section a, is subjected to a complete magnetic cycle. Let the magnetising coil consist of n turns per centimetre, so that the whole number of turns is In. Suppose that the magnetic induction of the iron is increased by an infinitely B small amount, dB, in an infinitely small interval of time, dt, by increasing the magnetising force by an infinitely small amount. Then the total lines of force through the iron are



increased by adB, and the time rate of change of this increase is  $a\frac{dB}{dt}$ . This change in the lines of

force will set up an opposing electromotive force in the coil, the value of which will be equal to the product of the total number of turns constituting the coil and the time rate of change in the lines of force, *i.e.* the total opposing E.M.F. =  $ln \cdot a \cdot \frac{dB}{dt}$ .

The work done in overcoming this opposing E.M.F. = C. dt. lna.  $\frac{dB}{dt} = nC$ . la. dB,

but  $H = 4\pi nC$ , and la is the volume of the iron, so that the work done per unit volume  $=\frac{I}{4\pi}$ . HdB. In Figure 23 the product HdB is represented graphically as the area NPQR, and the work done per cubic centimetre of iron when B is changed by any finite amount by changing the magnetising force from a value  $H_1$  to

 $H_2$  is =  $\frac{I}{4\pi} \int_{H_1}^{H_2} H dB$ . Or the total work done by the

cycle OFAR =  $\frac{I}{4\pi}$  area OFAR. In a complete hysteresis

loop, as is given in Figure 22,  $\int HdB$  is given by the area of the loop. The work done per cycle per cubic centimetre of a substance is then given by the area of the hysteresis loop divided by  $4\pi$ , i.e.  $\frac{1}{4\pi}\int HdB$ , and if

H and B be in absolute units, the work done is expressed in ergs. The energy expended in doing this work is therefore derived from the magnetising current. The area of the hysteresis loop may be obtained accurately by means of a planimeter, but as an approximation may be taken as the value of the product of twice the retentivity into twice the coercive force. Referring to Figure 25, this would make the area ARCDEF approximately equal to  $2OR \times 2OC = RE \times CF$ .

The form and area of a hysteresis curve depend upon the kind of material, and the harder the physical state of the material the larger will be the area of the loop, and consequently the greater will be the hysteresis loss. In subsequent calculations of commercial apparatus it is more convenient to have the loss of energy due to hysteresis expressed in watts per kilogramme of material, and the relation between the two quantities may be obtained as follows:

Ergs per cubic centimetre per cycle

= area of hysteresis loop

Watts per cubic centimetre per cycle per second

$$= \frac{\text{area}}{4\pi} \times 10^{-7}.$$

Since I cubic centimetre of sheet iron weighs 7.8 grammes, the watts absorbed per kilogramme per cycle per second

$$= \frac{\text{area}}{4\pi} \times 10^{-7} \times \frac{1}{7.8} \times 1000$$

= 0.000001 x ergs per cubic centimetre per cycle.

The ergs per cycle per cubic centimetre will depend upon the degree to which the iron is magnetised, so that for each specimen of iron a series of tests must be performed in order to determine the hysteresis loss at various inductions. This would be rather a tedious procedure, and Steinmetz has suggested the use of an empirical formula, in which the hysteresis loss is expressed in terms of the maximum induction B, and a constant  $\eta$  depending upon the kind of material.

The specific loss in ergs per cubic centimetre per cycle is given by  $h = \eta B^{1.6}$ . This formula is sufficiently correct for all practical purposes where B varies between 1000 and 14000. The values of  $\eta$  for different magnetic materials are given in Table IV. These values hold for inductions up to and just over the knee of the magnetisation curve. From the table it will be observed that for sheet iron employed in the construction of armature cores,  $\eta$  may be taken as = 0.0025 or 0.003, while for good transformer iron it may be as low as 0.0015.

TABLE IV
HYSTERESIS CONSTANT 7 FOR DIFFERENT MATERIALS

Material.	Hysteresis Constant η.			
Sheet iron for transformer con	es			0.0015 to 0.0025
" " armature cores			.	0.0025 to 0.003
Ordinary soft wrought iron				0.0032
Soft annealed cast iron .			. 1	0.0045 to 0.0085
Tool steel (annealed) .			. !	0.009
Grey cast iron			.	0.015

Since I erg per second =  $10^{-7}$  watts, the watts lost per cubic centimetre per cycle per second =  $10^{-7}$ .  $\eta$ .  $B^{1.6}$ . The watts per kilogramme per cycle per second

= 
$$10^{-7} \times \eta \times B^{1.6} \times \frac{I}{7.8} \times 1000$$
  
=  $0.000013\eta \cdot B^{1.6}$ .

So that when K kilogrammes of iron are subjected to N magnetic cycles per second the total loss in watts

= 0.0000 I 
$$3\eta \times B^{1.6} \times K \times N$$
.

In Figure 24 is shown a curve connecting the watts expended per kilogramme per complete cycle per second with the maximum induction for iron used for armature stampings in which  $\eta = 0.003$ .

Hysteresis loss in iron may be produced in two ways: one when the magnetic force acting upon the iron passes through zero when changing from a positive to a negative, and the other when the magnetic force

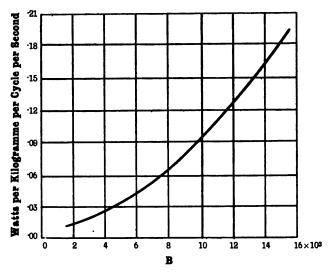


FIG. 24.—Hysteresis loss in watts per kilogramme for armature iron.

remains constant in value but varies in direction. The former is known as an alternating field, and takes place in the core of transformers; the latter is termed a revolving field, and it is the field an armature is subjected to when it revolves between the pole-pieces. The resultant hysteresis loss from these two causes is not by any means the same. Professor Baily has found that for low inductions an alternating field produces lower hysteresis loss than that of a rotating field, but at an induction of about 15,000 lines per square centimetre the loss due to a rotating field reaches a maximum, and then rapidly diminishes if the induction be further increased. On the other hand, the loss due

to an alternating field increases with the induction until the latter reaches about 22,000 lines per square centimetre. If the induction be increased beyond this the hysteresis loss ceases to increase, but shows no signs of diminishing, as in the case of the revolving field.

Example.—The ascending and descending values of B and H in half the hysteresis curve for a sample of armature iron are as follows:

Ascen	iding—				
B H	1.7	2500 2.0	5000 2.6	6000 3. I	7500 4.0
Desce	nding—				
В	7000	6000	5400	3000	0
H	2.3	0.5	0	<b>-</b> I.2	- 1.7

From the above data find the watts absorbed by an

armature having a volume of 5000 cubic centimetres of iron, revolving in a magnetic field, the induction density of which is 7500 lines per square centimetre, and the iron goes through 20 magnetic cycles per second.

Plotting the above values of B and H; the curve Figure 25 is obtained, the two halves of the curve being identical. Using a planimeter, it will be

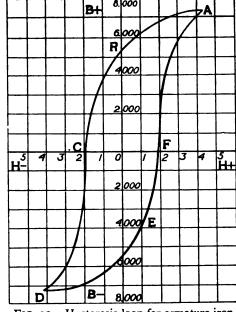


FIG. 25.—Hysteresis loop for armature iron.

found that the curve has an area of 44,000 units.

Now, the ergs wasted per cubic centimetre per cycle

$$= \frac{1}{4\pi} \int \mathbf{H} d\mathbf{B} = \frac{\text{area of curve}}{4\pi}$$
$$= \frac{44,000}{4\pi} = 3500.$$

Watts per cubic centimetre per cycle per second =  $\frac{3500}{10^7}$ .

Total watts absorbed =  $\frac{3500}{10^7} \times \text{volume} \times \text{cycles per second}$ =  $\frac{3500}{10^7} \times 5000 \times 20 = 35$ .

Example. — Find the increase of temperature in degrees centigrade of a mass of iron having a volume of 8000 cubic centimetres. The iron revolves for 30 minutes in a magnetic field, the induction density of which is 8500 lines per square centimetre, and goes through 50 complete cycles per second. Assume 25 per cent. of the heat to be lost by radiation. When B = 8500, the ergs lost per cycle per cubic centimetre equals 9000.

Specific heat of iron = 0.11.

1 cubic centimetre of iron weighs 7.8 grammes.

1 calorie =  $4.2 \times 10^7$  ergs.

The total work done against hysteresis

= 9000 x volume x cycles per second x time

 $= 9000 \times 8000 \times 50 \times 30 \times 60 \text{ ergs.}$ 

The work done in heating the iron

= weight × temperature rise × specific heat ×  $4.2 \times 10^7$ .

75 per cent. of work done against hysteresis

= work done in heating the iron.

That is

$$\frac{75}{100} \times 9000 \times 8000 \times 50 \times 30 \times 60$$

$$= 7.8 \times 8000 \times T \times 0.11 \times 4.2 \times 10^{7}.$$
Therefore the temperature rise of the iron =

$$T = \frac{75 \times 9000 \times 50 \times 30 \times 60}{100 \times 7.8 \times 0.11 \times 4.2 \times 10^{7}}$$
  
= 17° C.

### Hysteresis Testing

Within recent years a number of instruments have been devised for rapidly measuring the hysteresis loss in specimens of iron. Some of them indicate the loss when iron is revolved in a magnetic field, as in the case of the armature core of a dynamo or motor. Others again indicate the loss when the magnetism passes through zero in changing from positive to negative, as is the case of iron forming the magnetic circuit of a transformer. The Ewing hysteresis tester shown in Figure 26 is an example of the former type.

Ewing's Hysteresis Tester.—This instrument consists

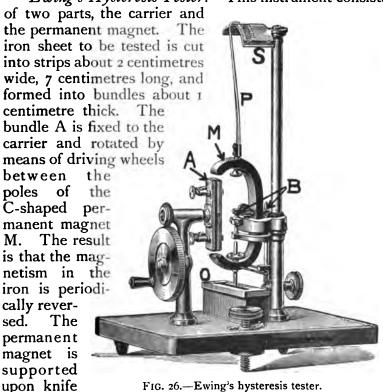


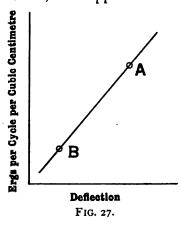
FIG. 26.—Ewing's hysteresis tester.

B, and carries a pointer P which moves over a graduated scale S; to the lower end of the magnet is attached a vane which dips into an oil bath O

edges

at

and so serves to damp the vibrations. The work done in reversing the magnetism due to the hysteresis loss causes a mechanical force to be exerted by the revolving iron upon the magnet; consequently the latter, along with the pointer P, is deflected through an angle which is proportional to the work expended per cycle. Since a certain amount of work is done for each reversal, whatever the frequency, the deflection is independent of the speed, provided the latter is not sufficiently high to create eddy current effects. Two pieces of iron, having different but known hysteresis losses, are supplied with the instrument; these are used



as standards of reference. The deflections produced by both these samples are plotted as a function of the hysteresis loss in ergs per cycle per cubic centimetre, and a straight line drawn through the two points A and B, as in Figure 27. By observing the deflection produced by a given specimen the corresponding value of the hysteresis loss can be obtained from the calibration

curve. To eliminate any zero error the iron should be rotated in both directions, and the mean of the two deflections may be considered the correct value. The standard hysteresis loss is based upon the assumption that B = 4000 lines per square centimetre in the iron. The loss at any other value of B is easily obtained from the law, hysteresis loss =  $\eta B^{1.6}$ .

In practical work the hysteresis loss is expressed in so many watts per kilogramme weight at 50 cycles per second, and at a value of B = 10,000. A fair average hysteresis loss for armature laminations is about 2 watts per kilogramme.

# CHAPTER IV

#### ELECTRICAL MEASURING INSTRUMENTS

#### Indicating Instruments

THERE are four distinct types of instruments intended for the measurement of current, pressure, and power. They are classified as follows, according to the principles upon which they work.

- A. Electro-magnetic instruments for measuring current and pressure, which may be subdivided into
  - (a) Moving soft-iron instruments;
  - (b) Moving-coil permanent-magnet instruments.
- B. Hot-wire instruments for measuring current and pressure.
  - C. Electrostatic instruments for measuring pressure.
- D. Electro-dynamic instruments for measuring current, pressure, and power.

Every instrument has some moving part which, when actuated by the current to be measured, takes up a temporary position of equilibrium between two positions of rest,—one when there is no deflecting force and the other when the moving system can move no further.

Controlling Force.—In all instruments it is necessary to provide a controlling force which opposes and controls the deflecting force so that the deflection may be proportional to the deflecting force. In any position of equilibrium the controlling and deflecting forces are equal, the former force tending to bring the moving system back to the zero position, while the latter tends to further deflect the moving system.

The controlling forces employed in the majority of present-day instruments are:

- (a) Force of gravitation.
- (b) Torsion of a spiral spring.

The force of gravitation, as a controlling force, has the great advantage that it is absolutely constant. Gravitation controls the movement of all instruments of the moving soft-iron type, hence they are often referred to as gravity instruments.

In the second form of control the force exerted by the spring is proportional to the angle of torsion. The spring is, in most cases, made of some hard and non-magnetic material, such as phosphor-bronze, and its strength varies directly as the sectional area of the material and inversely as the number of turns. It is essential that the turns be uniformly spaced, and do not touch one another at any stage of their action.

Damping.—The moving part of an instrument on receiving an impulse, due to a sudden change in the current flowing, tends to oscillate about its mean position. This is often undesirable, and a damping device is introduced so that, if the dimensions of the moving parts be suitably designed, the pointer of an instrument will move up to its reading without passing beyond it or oscillating about it. The instrument is then said to be deadbeat.

The methods of damping now in most general use depend on

- 1. Viscosity of liquids.
- 2. Electrical eddy currents.
- 3. Air friction.

Of these, that depending on the viscosity of liquids is the easiest to apply, and has therefore been largely employed. This arrangement consists of a light disc (attached to the moving system) immersed in a liquid (usually oil), so that the resistance offered by the liquid to the plunging of the disc damps out any vibration. This form of damping has been successfully applied to Kelvin's electrostatic voltmeters.

In the second method, damping is effected by causing a conductor, usually in the form of an aluminium disc attached to the moving system, to rotate in a magnetic field produced by a permanent magnet. Such an arrangement is depicted in Figure 28, in which the disc D rotates between the poles N and S of the permanent magnet M. As the disc moves across the magnetic field electric currents are induced in it, and assume the form of little whirls or eddies, as shown by the dotted lines. These currents, according to Lenz's law, oppose the

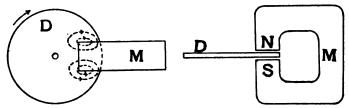


FIG. 28.—Principle of Eddy current damping.

cause producing them, thus the motion of the disc and consequently the moving system is retarded, and any tendency to oscillate is effectively damped.

This damping device is suitable for hot-wire and electrostatic instruments, but cannot be applied to moving soft-iron instruments. In the latter instruments the

presence of a permanent magnet close to the working coil would have a considerable effect on the readings. The instruments would of course be calibrated with the magnet in position, but the small magnets with comparatively large air-gaps have a great tendency to lose their strength, so that the effect on the readings would be a variable one.

Air damping, although used before any other system for galvanometers and other laboratory instruments, has only within recent years been applied to commercial

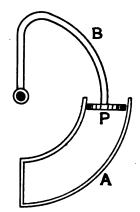


FIG. 29.—Principle of air damping.

Figure 29 illustrates a typical form of airinstruments. damping arrangement. It consists of an air chamber A closed at one end, in which works a loosely fitted aluminium piston P. The piston is connected by means

5

of a crank B to the moving system, so that any oscillation is damped by the cushioning action of the air on the

piston.

The mechanical difficulties of manufacture of this type of damping are great, since the clearance between the piston and the air chamber should not exceed 0.04 centimetre.

Ammeters and Voltmeters.—The essential difference between an ammeter and a voltmeter of the same type is in the resistance of the coil which carries the current to actuate the moving parts. The same movement does for either. An ammeter is connected in series with the circuit whose current is to be measured, and consequently must have a low resistance, otherwise the insertion of an ammeter in a circuit might alter the value of the current; moreover, the power absorbed by any part of the circuit is equal to C<sup>2</sup>R, so that if R be large an appreciable amount of power might be absorbed by the ammeter.

A voltmeter is connected in parallel across the points where the difference of potential is to be measured. The current taken by a voltmeter should be small, and in order to fulfil this condition the resistance must be very high, in some cases being as high as 50 ohms per volt. If the resistance be low then an appreciably large current will flow through the instrument, altering the pressure across the points connected to the instrument and preventing a reading of the true difference of potential being obtained. Figure 1 shows how to connect an ammeter and voltmeter to indicate the current and pressure respectively of a dynamo supplying current to a number of lamps in parallel.

# Moving Soft-Iron Ammeters and Voltmeters

This type of instrument includes those in which a piece of soft iron is constrained to move from one part of a magnetic field to another; the field being set up by a suitably wound solenoid energised by the current or pressure to be measured. The solenoid for these instruments, in general, is similar to that shown in Figure 10, the outside diameter being about 5.5 centimetres and

the length 5 centimetres. The magnetic force H inside the solenoid is equal to  $\frac{1.25}{l}$ ; that is, for the same size

of solenoid the strength of magnetic field H is directly

proportional to the ampère-turns CT.

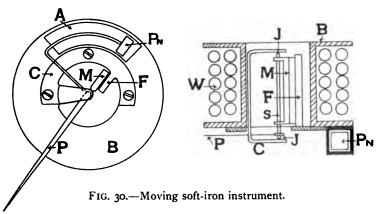
The same movement serving for both ammeters and voltmeters, it is essential to provide the same strength of magnetic field for both when giving a full scale deflection. Also it is immaterial whether the product CT be given by a large current flowing through a few turns of thick wire or a small current flowing through many turns of fine wire. In an ammeter the working coil is wound with a few turns of thick wire capable of carrying the maximum current to be indicated, while a voltmeter has its working coil wound with many turns of fine wire.

Thus the only difference between an ammeter and a voltmeter of this type is in the turns and size of wire constituting the winding of the working coil.

It will be of advantage, before investigating the theory of this type of instrument, to describe a few

representatives.

Examples of Moving Soft-Iron Instruments.—Figure 30 shows an end elevation and plan of the internal parts of



one form of moving soft-iron instrument. The coil W, of cable or fine wire according as the instrument is to be used as an ammeter or a voltmeter, is wound on a

suitably insulated brass bobbin B. Inside this bobbin is placed a brass frame C which carries the jewelled centres J between which is pivoted, concentric with the bobbin B, the steel spindle S. Inside the coil are two pieces of soft iron M and F, set axially with the coil. F is fixed to the frame C, and extends nearly the entire length of the solenoid. M is attached to the spindle, and is therefore free to move. To one end of the spindle is attached

a pointer P which passes over a graduated scale.

The working of the instrument is as follows. When no current flows through the solenoid the action of gravity causes the moving iron M to lie parallel to and almost touching the fixed iron F, the pointer being set to zero on the scale. When the coil is energised by a current, lines of force are set up inside, and M and F become magnetised, developing similar polarity at the same ends, consequently repulsion ensues and the moving iron M is repelled against the controlling force of gravity from its zero position; the pointer P at the same time moves over the scale. The movement of M, and hence the deflection of the pointer P, is very nearly proportional to the current energising the coil W.

In order to render the instrument dead-beat a small aluminium piston P<sub>N</sub> which is carried at the end of a crank attached to the spindle S, moves to and fro in the

air chamber A.

In the instrument illustrated in Figure 31 advantage is taken of the fact that the magnetic field set up inside a solenoid is stronger near the inner circumference CC (Fig. 10) than along the axis AB. The moving system consists of a piece of very thin soft iron M shaped as shown, and attached to a steel spindle S. The latter also carries an aluminium pointer P and balance arm A. The spindle is set eccentric with, but parallel to, the coil in jewelled bearings carried by the bridge piece D attached to the bobbin B, and a similar bridge piece at the other end. By the control of gravity, in the zero position, the iron M lies near to the centre of the coil. When the coil is energised, the field set up being stronger at the inner circumference C, the part M is

attracted towards it. As the iron is attracted, causing the spindle to rotate, the pointer P moves over a

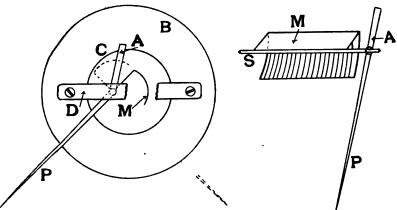


FIG. 31.—Moving soft-iron instrument.

graduated scale. The position of the moving system when the pointer indicates its maximum reading is shown in the figure by the dotted lines. The zero may be adjusted by altering the position of the balance arm A.

Figure 32 shows an elevation and plan of a third form of moving soft-iron instrument. The working coil C is wound on an insulated bobbin B, and set with its magnetic axis parallel to the base of the instrument. The coil is of a flat shape, in order to give as concentrated a field as possible with the minimum expenditure of energy. The moving soft iron M, of the shape shown, is built up of three thin pieces and carried by a steel spindle S set in jewelled centres J; the latter are supported by two lugs L projecting from the frame of the instrument. To the spindle is fixed an aluminium pointer P, and balance arms carrying the adjusting weights W<sub>1</sub> and W<sub>2</sub>.

The figures show the position of the moving system when no current passes through the coil C. On the coil becoming energised the moving iron is attracted against the controlling force of gravity towards the centre by an amount proportional to the strength of the current, the pointer at the same time moving over the scale.

Damping is effected by the movement of the piston  $P_N$  inside the curved air chamber A, the piston being attached by the crank D to the spindle.

Design of Moving Soft-Iron Instruments.—The force

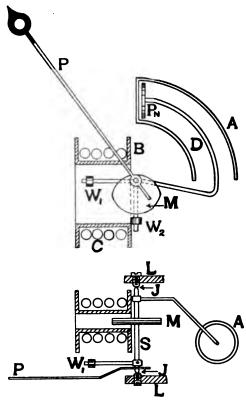


FIG. 32.—Moving soft-iron instrument.

required to deflect the moving system of an instrument so that the pointer moves over the scale is proportional to the weight of the moving parts. Consequently, order to reduce the power absorbed by the working coil, the weight of the moving system and friction at the pivots must be reduced to a mini-This mum. effected by (1) makthe moving as small possible,(2) making the pointer of aluminium, and setting the spindle in jewelled bearings.

In well-designed instruments the ampère-turns required to give a full scale deflection range from 200 to 400; so that from a knowledge of the ampère-turns required to deflect the moving system of a particular type of instrument over the scale the number of turns constituting the working coil of an ammeter can be easily determined. For a voltmeter the calculation is not so simple, for not only must the coil give the requisite magnetising force, but its resistance must be sufficiently high.

Size of Wire required for a Voltmeter Coil.—The ampère-turns CT required to deflect the needle of a particular instrument over the scale can be determined experimentally, and the voltage E impressed on the working coil is also a known factor.

Let C = current flowing through the coil.

R = resistance of the coil.

 $l_m$  = length of a mean turn on the coil.

l = total length of wire forming the coil.

a =area of cross-section of wire.

d = diameter of wire.

 $\rho$  = specific resistance of wire.

T = turns constituting the coil.

Then 
$$\frac{E}{C} = R = \frac{\rho \times l}{a}$$

but 
$$l = l_m \times T$$
 and  $a = \frac{\pi d^2}{4}$ 

Therefore 
$$\frac{E}{C} = \frac{\rho \times l_m \times T \times 4}{\pi d^2}$$

or 
$$d^2 = \frac{\rho \times l_m \times 4 \times TC}{\pi E}$$
.

From the above the diameter of the wire is given by  $d = \sqrt{\frac{4 \times \hat{\rho} \times l_m \times CT}{\pi F}}.$ 

$$d = \sqrt{\frac{4 \times \hat{\rho} \times l_m \times CT}{\pi E}}.$$

Example.—The working coil of a moving soft-iron voltmeter reading up to 100 volts requires 300 ampèreturns to give a full scale deflection. Find the diameter of wire for the coil if the wire be of copper having a specific resistance of 1.6 × 10<sup>-6</sup> ohms per centimetre cube; the mean length of one turn = 13.5 centimetres.

By the above formula

$$d = \sqrt{\frac{4 \times \rho \times l_m \times CT}{\pi E}}$$

 $\rho = 1.6 \times 10^{-6}$  $l_m = 13.5$  centimetres

$$CT = 300$$
  
 $E = 100$ .

The diameter of the wire

$$= \sqrt{\frac{4 \times 1.6 \times 10^{-6} \times 13.5 \times 300}{\pi \times 100}} = 0.009 \text{ cms.} = 0.09 \text{ mm.}$$

To obtain a uniform scale with these instruments it is necessary to have the moving soft iron saturated, the reason for this being as follows:

When the solenoid is energised the moving soft iron becomes a magnet, and the force deflecting the moving system is proportional to the product of the strength of the field and the strength of this temporary magnet. From the curves in Figure 15 it will be seen that when the iron is saturated its magnetic strength remains practically constant, in which case the deflecting force would be directly proportional to the current flowing in the coil, the field strength being proportional to the current. These instruments, when the iron is saturated, will have a perfectly uniform scale, equal increments of current producing equal increments in the deflection.

Below saturation value the variation of B with H is irregular, consequently the scale of an instrument in which the iron is not saturated cannot be evenly divided. For this reason moving soft-iron instruments are not calibrated for currents or voltages which do not produce a magnetic field strong enough to saturate the iron, and the lower part of the scale of these instruments is generally left blank.

Errors in moving Soft-Iron Instruments.—The chief errors occurring in this type of instrument are due to the following causes:

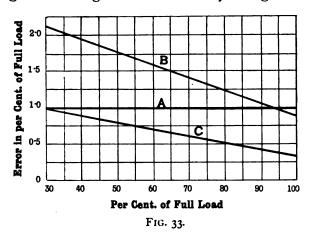
- 1. Hysteresis effect.
- 2. Effect of stray magnetic fields.
- 3. Change in resistance of working coil due to temperature.

The hysteresis effect causes the readings taken with a rising current to be lower than those obtained with a falling current, due to the property of retentivity explained in Chapter III.

In order to reduce the hysteresis error to a minimum, it is essential that the moving iron should be very soft, and further, that the mass be as small as possible. By working the iron near saturation point and observing the above conditions the hysteresis effect is practically eliminated.

Stray magnetic fields affect the accuracy of all electro-magnetic instruments. This is particularly the case with instruments used for switchboard work. The effect is somewhat difficult to predetermine owing to the complicated nature of resultant fields, but other things being equal an instrument which in itself utilises the strongest field will be least affected. In Figure 33 curves are given showing the error introduced into three types of moving soft-iron instruments when subjected to stray magnetic fields near a switchboard.

These curves are reproduced from a paper on directreading measuring instruments by Edgcumbe and



Punga.\* The abscissæ show the readings as a percentage of the maximum current, while the ordinates represent the error as a percentage of the maximum readings of the instruments. Curve A shows the effect on a 30-ampère moving soft-iron ammeter, having 450 ampère-turns and enclosed in a brass case. The movement consisted of a fixed mass of iron repelling a moving mass. It will be observed that the percentage error is practically constant. Curve B refers to a 10-ampère instrument having 400 ampère-turns and with its castiron case removed. It will be seen that the error falls off very rapidly as the load increases. Curve C refers

<sup>\*</sup> Journal of Institution of Electrical Engineers, vol. xxxiii. pp. 620-693, March 1904.

to the same instrument after replacing the cast-iron case.

From these curves it would appear that by placing the moving system in a cast-iron cover the instrument is shielded from stray magnetic fields and errors considerably reduced. The shielding action of the iron case is shown diagrammatically in Figure 34. The stray lines, say, coming from the magnet M, enter the case C, and if it be of appreciable thickness the lines of force follow the paths in the case as shown. Thus the stray field in no way influences the working of the moving parts.

The iron case may screen the working parts from

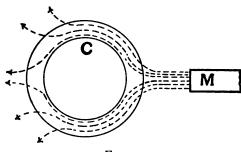


FIG. 34.

stray magnetic fields, but on the other hand the lines of force emanating from the moving iron pass into the case, and consequently the hysteresis error is greatly increased. Again, the case is

liable to become magnetised and cause a possible error far outweighing the reduced error due to magnetic shielding. In general, moving soft-iron instruments are enclosed in non-magnetic cases.

The error due to change of temperature occurs in all types of instruments having a high resistance coil carrying potential currents. Let C denote the current passing through the coil of a voltmeter, R the resistance of the coil, and E the potential across the voltmeter. The scale of the instrument is graduated in terms of E = CR; so that the reading on the instrument is proportional to C. If E remain constant but R vary, due to change of temperature, then C will alter, and consequently the reading. This is best illustrated by a concrete case.

Example.—The working coil of a moving iron voltmeter has a resistance of 4000 ohms at 20° C., at

which temperature it was calibrated and read correctly when connected across a potential of 200 volts. coil is wound with copper wire having a temperature coefficient equal to 0.0043. Find the percentage error in the reading when the temperature of the working coil increases to 60° C.

At 20° C. the current flowing in the coil

$$=\frac{E}{R_{20}}=\frac{200}{4000}=0.05$$
 ampère.

This current gives a full scale deflection corresponding to 200 volts.

At 60° C. the current flowing in the coil

= 
$$\frac{E}{R_{60}}$$
; but  $R_{60} = R_{20}(1 + at)$   
=  $4000(1 + 0.0043 \times 40)$   
=  $4000 \times 1.17 = 4680$  ohms.

Therefore the current flowing in the coil when it is at  $60^{\circ}$  C. =  $\frac{200}{4680}$  = 0.043 ampère.

The current energising the solenoid is thus reduced, so also will be the voltmeter reading. With 0.05 ampère through the coil the needle indicated 200 volts, therefore, if the iron be saturated, 0.043 ampère will indicate

$$\frac{200 \times 0.043}{0.05}$$
 = 172 volts.

The error introduced due to change of temperature  $= -28 \times \frac{100}{200} = -14$  per cent. That is, the voltmeter indicates 14 per cent. low.

A voltmeter so constructed would be unreliable, and the method of reducing the temperature error will now be considered.

Alterations in the temperature of an instrument are caused in two ways-first, by change in atmospheric temperature; and second, by the expenditure of energy in the coil itself, the latter being proportional to C<sup>2</sup>R. The employment of a material such as manganin, which

has a negligible temperature coefficient, would practically eliminate any temperature error; but a voltmeter coil wound with manganin wire would have a much less radiating surface than a coil of copper wire of the same resistance. This would result in a considerable increase in the actual heating, the radiating surface being insufficient. A compromise has therefore to be made between the two. The working coil of a voltmeter is wound with copper wire so as to obtain as large a

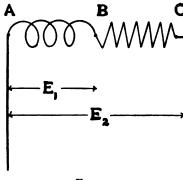


FIG. 35.

magnetising force as possible with the least expenditure of energy, and connected in series with it is another coil, made of a material such as manganin, having a negligible temperature coefficient.

In Figure 35 AB is the working coil, and BC the resistance in series with it. Let E<sub>1</sub> denote the voltage required to produce a

certain deflection when applied to the working coil AB, and  $E_2$  the voltage to produce the same deflection when applied to AC. If  $R_1$  and  $R_2$  denote the resistance of the coils AB and BC respectively,

then 
$$\frac{E_1}{E_2} = \frac{R_1}{R_1 + R_2}$$
.

With this arrangement if  $R_1$  vary it is so small a fraction of  $(R_1 + R_2)$  that the latter remains practically constant. The resistance BC is wound on one or more porcelain bobbins. In low-reading voltmeters the bobbins are fixed to the base of the instrument, but for high-voltage instruments several are required, so they are placed in a separate case. The working coil is generally designed so that it produces a full scale deflection with about 20 volts, the remaining voltage being absorbed by the extra resistance. In this way the same size of working coil will do for any voltmeter reading

up to say 600 volts; the resistance coils being wound for each particular voltage.

Example.—If in the previous example the resistance of the working coil be reduced to 400 ohms at 20° C. by winding it with the same number of turns of copper wire having a larger sectional area, determine the error in the voltmeter reading when the temperature of the working coil increases to 60° C. In series with the working coil is a resistance of 3600 ohms, having a negligible tempera-

Current flowing through the coils at 20° C. = 0.05 ampère.

Resistance of working coil at 60° C. is equal to

 $R_{20}(1+at)$ 

ture coefficient.

= 
$$400 (I + 0.0043 \times 40) = 400 \times I.17$$
  
=  $468$  ohms.

Total resistance in voltmeter circuit at 60° C.

= 468 + 3600 = 4068 ohms.

Current flowing through the coils at 60° C.

$$=\frac{E}{R_{00}}=\frac{200}{4068}=0.0492$$
 ampère.

Voltmeter reading at 60° C.

$$= 200 \times \frac{0.049^2}{0.05} = 197.$$

Error in voltmeter =  $-1\frac{1}{2}$  per cent. The voltmeter now reads only  $1\frac{1}{2}$  per cent. low, clearly showing the effect of introducing a resistance in series with the working coil.

# Moving-Coil Permanent-Magnet Ammeters and Voltmeters

Instruments belonging to this type, though differing in the details of construction, all work on the d'Arsonval principle. Such instruments depend for their action on the rotative force experienced by a coil of wire carrying current when the latter is pivoted so as to lie across a magnetic field. The amount of movement is indicated by a pointer, attached to the moving system, passing over a graduated scale.

The principal parts of these instruments are:

(1) A permanent magnet provided with soft-iron pole pieces.

(2) A moving coil of fine wire mounted on pivots

and fitted with controlling springs.

Figure 36 shows a plan and elevation of the working parts. PM is a permanent magnet which has been specially "aged" so that its strength will remain constant over a long period of time. The soft-iron pole pieces P are fixed to the ends of the permanent magnet and bored

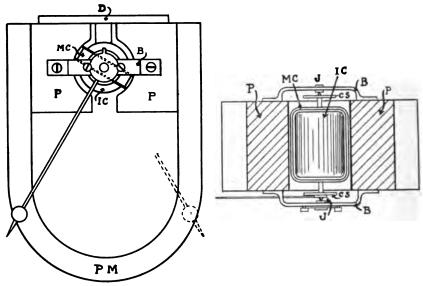


FIG. 36.—Principle of moving-coil permanent-magnet instrument.

out so as to be truly cylindrical. Concentric with the two pole pieces P is placed a soft-iron core IC. This iron core has a diameter of about 2.5 centimetres, and is screwed to a brass bridge piece D. Capable of turning in the narrow air-gap formed between the poles P and the iron core IC, is a rectangular-shaped coil MC, composed of a number of turns of fine insulated wire wound on a copper or aluminium frame. The frame is carried by two pivots running in jewelled bearings J, the latter being supported from two brass brackets B attached to the pole pieces. The pivots are insulated from the frame, but

each is in electrical connection with an end of the moving coil.

The current is led into and out of the moving coil by means of two copper phosphor-bronze hair-springs CS, one end of each being connected to the top and bottom pivots respectively, and the other ends to two insulated contacts fixed either to the brackets B or to two metal pillars fixed to the base of the instrument. Connection is made between these insulated contacts and the terminals of the instrument. The springs are set in opposite directions, so that as one coils up the other uncoils. This arrangement of the springs neutralises the effect on the

position of the coil due to expansion or contraction

The action of the instrument is as follows: When a current passes through the moving coil, lines of force are set up, and they tend to set themselves parallel to the lines of force from the permanent magnet, consequently the coil experiences a rotative force and moves against the spiral springs which act as a controlling force. When equilibrium is obtained the controlling force equals the deflecting force, and the pointer takes up a definite position on the scale, that position depending upon the value of the current flowing in the moving coil.

The deflecting force is proportional to the product C.B.

where C = current in the moving coil,

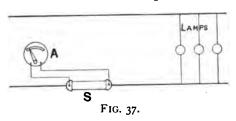
through temperature variation.

and  $B_a$  = induction density in the air-gap, and varies between 600 and 2000 lines per square centimetre, depending on the make of instrument. Throughout the entire movement of the coil MC, the strength of the magnetic field  $B_a$  is maintained uniform by having a very narrow air-gap about 0.18 centimetre, and setting the coil MC at such an angle that the two positions of rest are within the polar arc. Under these conditions the deflecting force is directly proportional to the current, and as the controlling force due to the hair-springs is proportional to the angle turned through, an evenly divided scale is obtained throughout the entire range.

These instruments are rendered dead-beat by the damping action of eddy currents induced in the aluminium

or copper frame as the coil moves from one position to another. The moving coil is wound with different sizes of wire, depending upon the use for which the instrument is intended, i.e. ammeter or voltmeter.

Ammeters of this type measure current indirectly by indicating the difference of potential between the ends of a low-resistance shunt made of a material having a negligible temperature coefficient. The shunt is connected in series with the main circuit, and carries the current to be measured. The voltage drop in the shunt is proportional to the current flowing through it, so that moving-coil ammeters are in reality milli-voltmeters. Figure 37 illustrates how a shunt S is connected in series with a circuit of lamps, the measuring instrument A



being connected across the terminals of the shunt. fall of potential in the shunt should small. consequently an ammeter coil wound with a small

number of turns, and is then actuated by a small electromotive force across its terminals.

In a particular make of ammeter of this type the moving coil consists of 15 turns, having an approximate resistance of 0.15 ohm. In series with this coil is a resistance having a negligible temperature coefficient, which reduces the error caused by temperature variation, as explained on page 76.

Ammeter Shunts.—These are made of strips of manganin, and are so designed that with the maximum current flowing, the drop of E.M.F. is sufficient to give a

full scale deflection on the instrument.

Suppose the current to be measured to flow through the shunt and be denoted by C, then if R, be the resistance of the shunt the volts drop is given by  $E_r = C_r R_r$ . R, remains constant, as the shunt is made of manganin, having a negligible temperature coefficient, so that  $E_r \propto C_r$ . Now the current C flowing in the moving coil and producing the deflection is proportional to  $E_n$  so that

the deflection of the instrument is directly proportional to the current flowing through the shunt.

In order that the student may thoroughly understand the function of a shunt, the following example is given:

Example.—In a particular moving-coil instrument 0.08 of a volt is sufficient to produce a full scale deflection. It is proposed to use the instrument to indicate a maximum current of 200 ampères. If the shunt be made from manganin strip 0.5 millimetre thick, calculate the dimensions of the shunt. Specific resistance of manganin = 43 microhms per centimetre cube.

Since 0.08 of a volt is required to produce a full scale deflection, the voltage drop in the shunt must equal this value when the maximum current the instrument has to indicate passes through the shunt. So that the resistance of the shunt is given by

$$R_s = \frac{E_s}{C_c} = \frac{0.08}{200} = 0.0004$$
 of an ohm.

Shunts are generally designed for a temperature rise of about 30° C. when carrying continuously their full load, and in order that the temperature increase may not exceed this limit the shunt must have a radiating surface of 12 square centimetres per watt absorbed.

In this case the watts absorbed

$$= E_s \times C_s = 0.08 \times 200 = 16$$
 watts.

Therefore the total radiating surface must be

=  $12 \times 16 = 192$  square centimetres; but there are two sides of the shunt strip exposed to the atmosphere, so that the surface per side =  $\frac{192}{2}$  = 96 square centimetres.

Referring to Figure 38, l = length of strip, b = breath, and t = thickness; therefore  $l \times b = 96$ .

The resistance of the shunt is also given by the equation

$$R_s = \frac{\rho \times l}{a} = 0.0004$$
 of an ohm

where a = area of cross-section of the strip.

From this equation 
$$\frac{l}{a} = \frac{0.0004}{\rho} = \frac{0.0004}{0.000043} = \frac{9.3}{1}$$
.  
Now  $a = b \times t = b \times \frac{1}{20} = \frac{b}{20}$  sq. centimetres that is  $\frac{l}{b} \times \frac{20}{1} = \frac{9.3}{1}$  or  $l = \frac{9.3 \times b}{20}$ .

Substituting for l,  $\frac{9.3 b^2}{20} = 96$  or b = 14.4 centimetres.

Now  $l \times b = 96$ 

therefore  $l = \frac{96}{14.4} = 6.65$  centimetres.

Length of shunt strip = 6.65 centimetres. Breadth of shunt strip = 14.4 centimetres.

Referring to Figure 38, the shunt strip is brazed into

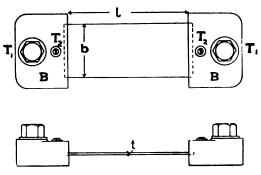


FIG. 38.—Ammeter shunt.

saw-cuts made in two terminal blocks B; to the latter are attached main terminals  $T_1$  and potential terminals  $T_2$ . If the breadth be greater than the length (as in the above example) the shunt is made up with a number of strips, the length remaining the same as that calculated, but the breadth of each part is  $\frac{1}{n}$ th the calculated breadth, n being the number of parts into which it is found

convenient to divide the strip. Figure 39 illustrates the shunt calculated above; it is divided into 4 strips as shown, the breadth of each strip being  $\frac{14.4}{4} = 3.6$  centimetres.

For instruments reading up to 75 or 100 ampères the shunt usually is fixed to the instrument base; for

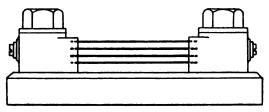


Fig. 39.—Ammeter shunt for large currents.

higher reading instruments the shunt is separate and can be fixed at any convenient place on the switchboard, and leads run from the potential terminals to the instrument, as indicated in Figure 37.

These instruments are calibrated in ampères, and should only be used with the shunt for which each one is calibrated.

In voltmeters the moving coil is wound with 130 to 250 turns of copper wire having a resistance of from 30 to 100 ohms. In series with the moving coil is connected a resistance of manganin having a negligible temperature coefficient and is adjusted to such a value that 0.015 of an ampère passes through the voltmeter when giving a full scale deflection. The resistance of a voltmeter may therefore amount to many thousands of ohms, so that any error due to temperature variation is practically eliminated. The actual temperature coefficient of a 100-volt instrument is often less than one one-hundredth per cent. per degree centigrade.

Example.—A moving-coil voltmeter reading up to 150 volts requires a current of 0.015 of an ampère to produce a full scale deflection. If the error due to temperature change must not exceed 0.05 per cent. of the maximum reading, with a rise in temperature of 20° C., and the moving coil is wound with copper wire having a temperature coefficient of 0.43 per cent. per

degree centigrade, calculate the value of the manganin resistance in series with the moving coil. Manganin has a zero temperature coefficient.

Total resistance of voltmeter circuit at ordinary

temperature

$$=\frac{E}{C}=\frac{150}{0.015}=10,000 \text{ ohms};$$

when the temperature increases by 20° C. the current in the moving coil is reduced by 0.05 per cent. and

$$=\frac{99.95}{100} \times 0.015 = 0.01499$$

Therefore the resistance of the voltmeter when the temperature rises 20° C. above normal must not exceed

$$\frac{150}{0.01499}$$
 = 10,007 ohms.

Increase in resistance = 10,007 - 10,000 = 7 ohms. The copper increases  $0.43 \times 20 = 8.6$  per cent. per 20° C. So that the normal resistance of moving coil

$$=\frac{100\times7}{8.6}=81$$
 ohms.

The manganin resistance must therefore have a value of 10,000 - 81 = 9919 ohms.

The resistance of the moving coil is quite low

compared with that of the manganin resistance.

Example.—The control of a particular moving-coil instrument is such that it requires a force of 1.5 gramme-centimetres to produce a full scale deflection, and the current flowing in the moving coil when giving this deflection is 0.015 of an ampère. From the following data calculate the number of turns required for the moving coil:

Diameter of moving coil (d) = 3 centimetres. Length of active conductor (l) = 3 centimetres. Flux density in air-gap  $(B_a) = 800$  lines per square centimetre. The force acting on one conductor =  $B_a \times l \times 0.0015$  dynes.

If t denote the turns required for the moving coil, then the force acting on one side of the coil

= 
$$B_{\alpha} \times l \times t \times 0.0015$$
 dynes  
=  $\frac{B_{\alpha} \times l \times t \times 0.0015}{981}$  grammes.

The total moment producing rotation is given by  $\frac{B_a \times l \times t \times 0.0015}{981} \times d = 1.5 \text{ gramme-centimetres,}$ 

so that 
$$t = \frac{1.5 \times 981}{0.0015 \times B_{\alpha} \times l \times d}$$
  
=  $\frac{1.5 \times 981}{0.0015 \times 800 \times 3 \times 3} = 136$ .  
Turns required for moving coil = 136.

Sources of Error in Moving-Coil Instruments.— Hysteresis is of course absent, as the magnetic flux is practically constant, although theoretically the ampèreturns of the moving coil (in practice less than one ampère-turn is required) slightly affect the permanent magnetic field, weakening it over the lower half of the scale and strengthening it throughout the upper half.

The chief source of error in moving-coil instruments was formerly the variation with time of the springs. A great amount of attention has been devoted to the preparation of non-magnetic springs with as small a permanent set as possible; these can now be obtained, and if properly fixed they introduce practically no error.

Instruments of the moving-coil type are the most accurate for the measurement of direct currents. They are the least liable to derangement, have no hysteresis loss, and when enclosed in a cast-iron case are unaffected by stray magnetic fields. The cast-iron case, however, diverts some of the lines of force from the air-gap and so lowers the induction density in the latter, affecting at the same time the accuracy of the instrument.

In order to avoid this error instruments of this type must be calibrated with the cast-iron case in position, otherwise an error amounting to as much as 4 or 5 per

cent. may be introduced.

The current in the moving coil must always flow in the one direction, otherwise the needle would be deflected in the wrong direction. For convenience the terminals of these instruments are marked + and respectively, so that the proper connections may be made. The zero is adjusted by altering the tension of the controlling springs. For this purpose they are generally provided with an adjusting screw, so that the operation may be performed without the removal of the case.

## HOT-WIRE AMMETERS AND VOLTMETERS

In these instruments the heating effect of an electric current in a wire of suitable resistance is by special mechanism made to indicate current or potential in a circuit. The rate of generation of heat when a current of C ampères flows through a wire having a resistance of R ohms =  $C^2R \times 0.24$  calories per second.

If E be the fall of potential along the wire, then

$$C^2R \times 0.24 = E \times C \times 0.24$$
.

If the wire be at a temperature  $t_1^{\circ}$  C. before the current or potential is applied, then let  $t_2^{\circ}$  C. denote the temperature to which the wire is raised when a constant current of C ampères flows through it.

Denoting the emissivity by  $\sigma$ ,—emissivity being the rate of loss of heat by radiation per unit area of the wire per degree centigrade difference in temperature between the wire and the surrounding air,—then when the maximum temperature, due to the current flowing in the wire has been attained, the rate of loss of heat by radiation

$$= 2\pi r_2 l_2 \sigma (l_2 - l_1) \text{ calories per second}$$
the rate of generation of heat
$$= C^2 R \times 0.24 \text{ calories per second}$$

$$= C^2 \cdot \frac{\rho \times l_2}{\pi r_2^2} \times 0.24 \qquad , \qquad , \qquad ,$$

Now the rate of generation of heat must equal the rate of loss of heat by radiation, so that

$$2\pi r_2 l_2$$
.  $\sigma$ .  $(t_2 - t_1) = \frac{C^2 \rho l_2}{\pi r_2^2} \times 0.24$   
or  $(t_2 - t_1) = \frac{\rho}{\sigma} \times \frac{C^2}{\pi^2 r_2^3} \times 0.12$ .

Let x = the elongation of the wire when its temperature rises from  $t_1^{\circ}$  to  $t_2^{\circ}$ , then

$$x = l_1 \times \kappa \times (t_2 - t_1)$$

$$= l_1 \times \kappa \times \frac{\rho}{\sigma} \times \frac{C^2}{\pi^2 r_2^3} \times \text{ o. I 2.}$$

 $\sigma$  and  $\rho$  are practically constant within the limits of temperature that occur in hot-wire instruments.

 $l_1$  and  $r_2$  are also constants for a given temperature,

so that 
$$x = K_1 C^2$$
  
or  $C = K\sqrt{x}$ 

where K<sub>1</sub> and K are both constants.

Thus the elongation of a wire is proportional to the square of the current flowing in it. The elongation of the wire is transmitted to a pointer which moves over a graduated scale. The chief difficulty in the design of hot-wire instruments is that the expansions dealt with are so small that when the necessary multiplication has to be taken into account the available power is very small. With ammeters it is necessary to reduce the size of wire employed to a minimum, so as to avoid excessive sluggishness. Shunts are therefore employed, as with moving-coil instruments.

The first instrument of this type was the well-known but now obsolete Cardew voltmeter.

Figure 40 illustrates a more modern voltmeter of this type. The measuring or hot-wire W is of platinum silver—16 centimetres in length—and is stretched between the fixed point A and a tension adjusting arrangement B. A little to the right of the centre of the wire W is attached another wire W<sub>1</sub>, of phosphor-bronze, at right angles, and is held taut to a fixed terminal D.

Near the centre of the wire W<sub>1</sub> a cocoon fibre C is attached, and passes round a grooved metal pully E

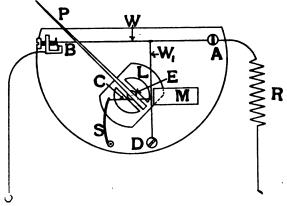


FIG. 40.—Hot-wire voltmeter.

fixed on a pivoted steel spindle mounted in jewelled bearings, and terminates in a small eyelet attachment to a flat steel spring S. The whole arrangement of the fibre and wires is thus subjected to tension, and any slackening or sag of the wire W is immediately taken up by the steel spring, and is transmitted by the wire W<sub>1</sub> and the fibre C to the spindle which carries the pointer P. By this method the smallest extension of the wire W is greatly magnified and conveyed to the pointer, thus rendering the readings easily perceptible. A magnetic damping arrangement is provided, which consists of a light disc L of aluminium, which is mounted on the spindle carrying the pulley E and the pointer P. This disc, which is about 5 centimetres in diameter, moves between the poles of the permanent magnet M, and the eddy currents induced damp the oscillations of the moving system, thus rendering the instrument dead - beat. The working of the instrument is as follows:

When the wire W becomes heated, due to the passage of a current, it expands, the corresponding sag being taken up by the spring S and transmitted by the wire W, and fibre C to the pointer P, as already explained. The whole of the hot-wire movement is mounted on a metal compensating plate, made from an alloy whose temperature coefficient is the same as the hot wire W. For high pressures the whole internal mechanism is mounted on ebonite. In all these voltmeters a fuse is introduced to protect the measuring wire in case an excessive voltage should be accidentally applied. deflect the pointer of such a voltmeter over the scale a current of 0.2 ampère is required. For instruments up to 400 volts a series resistance R, made of constantan, is placed in the back of the instrument and connected in series with the hot wire. For higher voltages than 400, the resistance R is placed in a separate case. When the resistance is placed in the same case as the movement, means must be provided for efficient ventilation.

Hot-wire ammeters of this make are, with the excep-

tion of a slight modification in the arrangement of the measuring wire, exactly similar to the voltmeter just described. The arrangement of the measuring wire of an ammeter is shown in The hot Figure 41. wire is divided into four equal parts by thin silver foil, strips  $F_1$ ,  $F_2$ , and  $F_3$ . The object of these strips

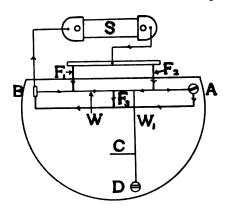


FIG. 41.—Hot-wire ammeter.

is to divide the current passing through the measuring wire. Referring to the figure, the current enters the wire W at two points situated at a quarter of its length from either end, while it leaves the wire from three

points, one being situated in the middle and the other two at the ends. The arrows in the diagram indicate the direction in which the current flows through the working wire. By suitably arranging the number of the contacts four or five ampères may be passed through the wire with a drop of potential not exceeding 0.25 of a volt.

All ammeters are provided with a shunt S, so that this type of instrument can measure currents of almost any magnitude provided the shunt is designed to give a fall of potential of 0.25 of a volt at full load.

The means provided for re-setting the pointer to zero when necessary, consists of a very fine pitched screw passing through the support B of the measuring wire. This screw, which is accessible through a small aperture in the case, moves very slightly the arm of the stud to which the wire is attached. The arm is forced back against the set-screw by means of steel springs.

Characteristics of Hot-Wire Instruments.—The main advantage of hot-wire instruments is that they are unaffected by stray magnetic fields and have no hysteresis Their disadvantages, however, far outweigh their advantages, and are as follows:

1. Large consumption of power, the drop in an ammeter varying from 0.1 to 0.5 of a volt, and the current taken by voltmeters being from 0.1 to 0.4 of an ampère.

2. Uncertainty of zero, and very sluggish action, as the final temperature of a wire for a particular current

is only gradually reached.

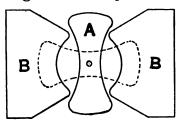
3. Liability in an ammeter of the working wire to These wires are usually raised to a high temperature in order to get the maximum possible elongation, hence a momentary increase of current might destroy Further, these instruments, in common with all others giving deflections proportional to the square of the quantity measured, have very unevenly divided scales, being excessively open at the maximum readings and cramped at the lower readings. Consequently they are never calibrated below one-fifth of the maximum reading.

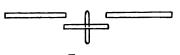
# Electrostatic Voltmeters

The principle on which electrostatic voltmeters work is that of an air condenser, in which one metal part is movable about an axis so as to increase or diminish the capacity. If two sets of insulated metal plates, one of which is movable about an axis, as shown in Figure 42, be connected to two points at different potentials, they will become charged to the potentials of the respective points. The moving and fixed plates being at different potentials

a force of attraction ensues, and the moving plate tends to set itself alongside the fixed plates B, and may take up the position shown by the dotted lines.

The capacity of the system will then have changed by a definite amount C, and the change in energy is equal to  $\frac{1}{2}$  CV<sup>2</sup>, V being the difference of potential between the two plates. If the moving plate be pro-





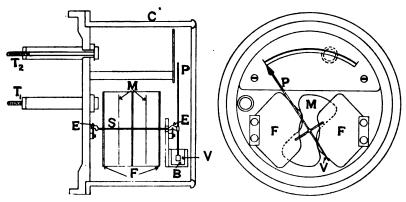
vided with a controlling force any movement will produce a couple tending to bring the moving system back to its original position. For a given form of control, this controlling force will depend solely upon the angle of rotation and may be denoted by  $K\theta$ , where  $\theta$  = the angle of rotation, and K a constant. When the moving system comes into a position of equilibrium the deflecting and controlling forces must be equal, that is, the gain in energy of the system must equal the work done against the controlling force,

i.e. 
$$\frac{1}{2}$$
 CV<sup>2</sup> = K $\theta$  and  $\theta = \frac{\text{CV}^2}{2}$  K.

Hence there will be a definite relation between the pressure and the resultant angular movement; this movement may be taken as a measure of the pressure. Instruments constructed on the above principle will therefore give deflections proportional to the square of the difference of potential between the two plates, thus causing the scale to be irregular, as in hot-wire instruments.

Kelvin's Electrostatic Voltmeters.—A type of voltmeter in which the foregoing principles are applied has been devised by the late Lord Kelvin. These instruments are made in two forms—(1) high-tension dial form, for measuring pressures above 1000 volts, and (2) multicellular form, for pressures up to 1000.

(i) High-Tension Dial Form.—This instrument is illustrated in Figures 43 and 44. It consists of two



FIGS. 43 and 44.—High-tension electrostatic voltmeter.

aluminium vanes M attached to a steel spindle S, and capable of moving between the fixed plates F. The spindle S is supported on knife-edges E and carries a light pointer P, moving over a graduated scale. The fixed plates F are insulated from the brass case C by vulcanite supports and connected to an insulated terminal T<sub>2</sub>; the moving system is connected to terminal T<sub>1</sub> through the case C. The controlling force is furnished by gravity. When a difference of potential exists between the plates M and F, the moving vanes M are attracted in between the fixed plates. The moving system thus rotates against the controlling force, and when the forces balance the position of the pointer

P on the scale indicates the pressure. Damping is effected by a small vane V, attached to the lower end of P, moving in an oil bath B. The case is surrounded by tin-foil, to screen the movement from external electrostatic effects.

(2) Multicellular Form.—For accurately measuring potentials below 1000 volts the dial form is not suitable.

since, with only two moving vanes, difficulty is experienced in obtaining a sufficient deflecting force. This force can, however, be augmented by employing a greater number of vanes. each moving between a pair of fixed plates. Such an arrangement is referred to as a multicellular electrostatic voltmeter.

Figure 45 illustrates this instrument. The fixed F. of triplates angular shape, consist of two sets, as shown, and are fixed to brass supports B.

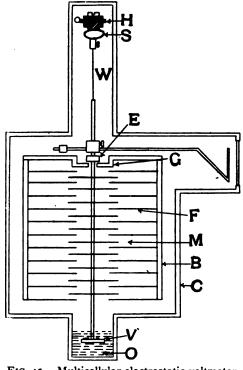


FIG. 45.—Multicellular electrostatic voltmeter.

C is the outside case to which two insulated terminals are fixed; one of these terminals is in connection with B, the other one being connected to the moving system.

The moving system consists of a number of aluminium vanes M of the form shown in Figure 42. These vanes are mounted on a spindle and suspended by a fine phosphor-bronze wire W, so that the vanes are free to move, each between a pair of fixed plates. upper end of the suspension wire is attached through

a carriage spring S to a torsion head H, provided with a tangent screw for adjusting the zero. The function of the carriage spring between the torsion head and the suspension wire is to prevent the latter from breaking when accidentally jerked. Should the vanes be jerked downwards, then the carriage spring yields sufficiently to allow the safety-sleeve E to come into contact with the guide stop G before the suspension wire is overstrained.

The working of this instrument is similar to the

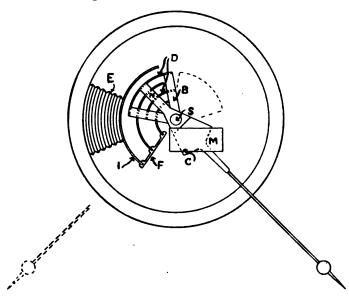


FIG. 46.—Electrostatic voltmeter.

dial form, except that the controlling force is furnished by the torsion of the suspension wire as the moving system rotates. The controlling force thus differs from that generally employed in indicating instruments. At the lower end of the moving system is a disc V, dipping into an oil bath O, which acts as a damper on the moving system.

Ayrton and Mather's Electrostatic Voltmeter.—This instrument is used for the measurement of potentials between 1000 and 3000 volts. The construction will be understood by referring to Figure 46. The plates, both

fixed and moving, are curved. The fixed plates consist of three metallic inductors I fixed to a metallic endpiece F and mounted on a corrugated ebonite block E, the latter being fixed to the instrument case. The moving system N consists of two aluminium sheets D, concentric with each other and the axis about which they turn, carried by light arms B on a horizontal spindle S set in jewelled bearings. The arm B at one end of the spindle terminates in a light copper plate C, which moves between the poles of a permanent magnet M.

The fixed and moving plates are in connection with two terminals fixed outside the case; the terminal connected to the fixed plates is highly insulated, and the other is connected to the moving system through the case; when the plates are at different potentials the moving system is attracted against the force of gravity inside the fixed plates, and takes up a position of rest when the two forces balance. Damping is effected by eddy currents induced in the plate C, as it moves between the poles of the magnet M.

Instruments working on the electrostatic principle are of all instruments the least liable to change with time. Since there is no circuit through the instrument, they consume no power and are also unaffected by temperature changes. They are unaffected by stray magnetic fields, although electrostatic fields (set up, for instance, by such a simple process as rubbing the glass of the case to clean it) may cause considerable errors. This error may, however, be minimised by covering the glass with a transparent conducting varnish.

The great difficulty met with in the design of electrostatic voltmeters is that the forces dealt with are so small that frictional errors are difficult to avoid. In order to increase the deflecting force the distance between the fixed and moving plates has to be reduced to a minimum, with the result that sparking may occur across the plates should there be an abnormal rise of voltage.

In order to increase the range of electrostatic voltmeters, and at the same time to avoid sparking difficulties, a system of condensers may be made use

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Figure 47 shows the arrangement diagrammatically. An electrostatic voltmeter V, reading up to say

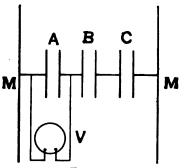


FIG. 47.

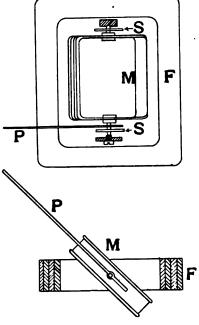
one-third of the maximum voltage, is connected across one of the three condensers A, B, and C, the condensers being connected in series across the points M and M, whose potential difference is to be found. The voltage at the terminals of each condenser is inversely proportional to the capacity. the condensers have each the same capacity, and that of the voltmeter V be very

small, then the voltmeter will indicate one-third of the

difference of potential between M and M. Should the voltmeter capacity not be small compared with the condensers, then the capacity of A and V in parallel will much exceed that of A alone, and so upset the simple voltage ratio mentioned above. Voltmeters on this principle are constructed reading up to 40,000 volts.

# ELECTRO-DYNAMIC Instruments

The construction of electro - dynamic instruments is based upon the mutual forces between movable and fixed por- Fig. 48.—Electro-dynamic instrument. tions of a circuit convey-



ing current. The fixed portion of the circuit often consists of a rectangular coil F (Fig. 48) of one or more turns of insulated copper strip, and is fixed with its plane horizontal. The moving coil M is mounted on pivots and set in jewelled bearings, so as to lie inside the fixed coil.

The current is led into and out of the moving coil by means of phosphor-bronze hair-springs S S, which also act as the controlling force. When no current flows through the coils, the moving system takes up the position shown in the figure. On the coils becoming energised a magnetic field is set up by each coil, and they tend to arrange themselves so that their fields are coincident. The moving coil therefore experiences a rotative force, and moves against the controlling force of the hair-springs into a new position, where it is in equilibrium. To the moving system is fixed a pointer P, which moves over a graduated scale.

The force of attraction or repulsion exerted between the fixed and moving coils is proportional to the product of the ampère-turns of the fixed coil and the ampèreturns of the moving coil,

# i.e. deflecting force $\propto C_f N_f \times C_m N_m$ .

The number of turns  $N_f$  and  $N_m$  on the fixed and moving coils respectively are constant, so that the deflecting force  $\propto C_f C_m$ .

In an ammeter the current in the moving coil is either equal to or proportional to the current in the fixed coil, in which case the deflecting force is proportional to C<sub>2</sub>.

A voltmeter has its moving and fixed coil connected in series, so that the deflecting force is proportional to  $E^2$ .

Electro-dynamic ammeters and voltmeters give, therefore, deflections proportional to the square of the quantity being measured.

Figure 49 shows the movement of an electro-dynamic instrument. In this form the moving coil M swings outside the fixed coil F; the latter being wound in the form of a ball. The moving coil is mounted on pivots B<sub>1</sub> B<sub>2</sub> set in jewelled bearings, and the current is

led into and out of the coil by means of the phosphorbronze hair-springs H. To the top pivot B<sub>1</sub> is attached a pointer P, which moves over a graduated scale. Eddy-current damping is effected by causing an aluminium disc D attached to the moving system to rotate between the poles of four permanent magnets PM.

The field of these instruments is so weak that considerable errors may be introduced due to stray magnetic fields, and in order to protect them, they

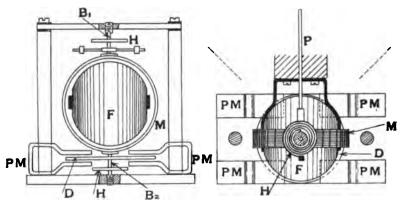


Fig. 49.—Electro-dynamic instrument.

must be shielded with cast-iron cases. Not more than 1 ampère can conveniently be passed through the moving coil, so that a shunt becomes necessary in the case of ammeters.

Owing to the weak fields employed (usually not more than one-tenth of that of a permanent-magnet moving-coil instrument) the ampère-turns of the moving coil must be relatively high, so that a much greater fall of potential is required over the shunt. Again, the power necessary to overcome friction is usually greater than that required by a moving-coil instrument, owing to the greater weight of the moving parts. As a rule 20 to 30 ampère-turns are employed in the moving coils, and in order to keep down the temperature coefficient of the moving system a drop of nearly half a volt is required.

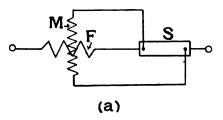
Figure 50 (a) shows diagrammatically the electrical connections for an ammeter indicating large currents. The fixed coil F carries the main current, and the

moving coil M is connected across a shunt S; the shunt is series with the main circuit, and is designed to give a fall of potential of 0.5 volt at full load.

In a voltmeter the moving and fixed coils M and F respectively in Figure 50 (b) are arranged in series, together with the necessary resistance R having a negligible temperature coefficient.

Watimeters.-Wattmeters work on the

electro-dynamic principle. the circuit whose power is to be measured, is passed through the fixed coil in Figure 48, and the moving coil



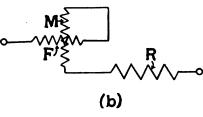
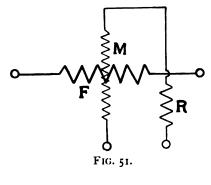


FIG. 50.

The main current taken by

is energised by the potential current. The deflecting force is proportional to  $C_m \times C_f$ , but  $C_m$ is proportional to the voltage of the circuit, and C, is the main current; therefore the deflecting force is proportional to the product EC, where E is the pressure, and C the cur-



rent in the circuit to which the wattmeter is connected.

Figure 51 indicates the connections of a wattmeter: the moving coil M, carrying the potential current, together with the resistence R, is connected across the mains, while the fixed coil F is connected in series with the main circuit.

Wattmeters are seldom used on direct current circuits, being mainly employed for the measurement of alternating current power. For a fuller treatment of electro-dynamic instruments, the student is referred to text-books on alternating currents.

# RECORDING INSTRUMENTS

The ammeters, voltmeters, and wattmeters which have, so far, been described, indicate the momentary value of the current, pressure, or power. It may, however, in some cases be necessary to obtain a permanent record of the variation in the value of the quantity measured during a certain period, say for twenty-four hours or more. Instruments for fulfilling this purpose are known as "recording instruments." Their electrical parts are constructed on the same principles as indicating instruments, and they are made recording by fitting them with a light cylinder or drum, which is rotated, by clock-work, at some definite speed. Long bands of paper, about 12 centimetres wide, are unwound from the drum at a rate ranging from 2.5 to 21 centimetres per hour. Holes are usually punched down one edge of the paper at a uniform distance of 1 centimetre apart; they engage in pins in a wheel driven by the clock, so that the movement of the paper is very definite and accurate.

Attached to the end of the pointer of the electrical part of the instrument, is an ink pen which presses against the paper chart as it unwinds from the drum. The chart paper is ruled longitudinally and cross-wise, the former being calibrated in time and the latter in terms of the quantity being recorded. The scale of the ruling will of course depend upon the rate of movement of the chart and the range of the instrument. The clock for such instruments is generally made to go for eight days, and is wound by means of a lever movement outside the case.

## STANDARD INSTRUMENTS

Kelvin's Standard Balances. — These instruments, devised by Kelvin, work on the electro-dynamic principle. They are among the most accurate and reliable electrical instruments constructed, and are therefore used as standards. There are several forms, all alike in principle but differing in the details of construction, depending on whether the instrument has to measure current, pressure, or power.

Current Balance.—In this instrument there are two movable coils or rings, each actuated by two fixed coils, all the coils being set with their planes horizontal. Figures 52 and 53 are respectively a diagram of the

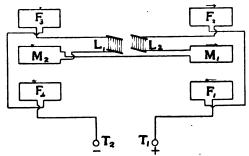
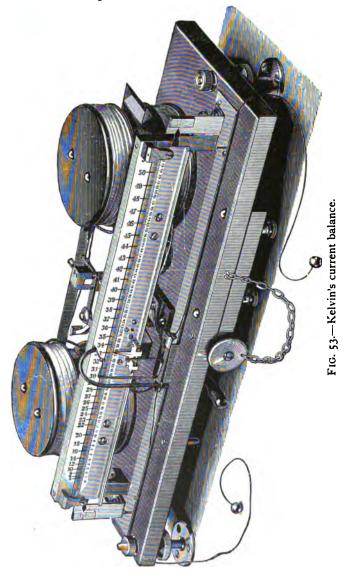


FIG. 52.—Diagram of connections for the Kelvin current balance.

connections, and a general view of the instrument. Referring to the former, the two movable rings  $M_1$  and  $M_2$  are attached to the ends of a horizontal balance arm, which is supported by two trunnions, each hung by elastic ligament, represented by  $L_1$  and  $L_2$ . These consist of a number of fine copper wires laid side by side and soldered to suitably insulated contact pieces; the ligaments also serve to lead the current into and out of the movable coils. Above and below each movable coil is a fixed coil, indicated by  $F_1$ ,  $F_2$ ,  $F_3$ , and  $F_4$ ; the fixed and movable coils are connected in series between the terminals  $T_1$  and  $T_2$ . The current flows in opposite directions through each two adjacent fixed coils, so that the movable coil is attracted by one

#### 102 ELECTRICAL MEASURING INSTRUMENTS

fixed coil and repelled by the other. The balance arm is in the zero position when the movable coils are



midway between the respective pairs of fixed coils. When the current to be measured is passed through the instrument the balance arm is tilted, and the

deflecting couple acting on the movable system is proportional to the square of the current. The deflecting couple is balanced by a weight, which brings the movable system back to the zero position. weight is made to move along a horizontal, finelygraduated scale attached to the balance-arm; the moving of the weight into its proper position is performed by means of a self-releasing pendant hanging from a hook carried by a sliding platform, which is pulled in either direction by two silk threads shown in

Since the balancing couple is proportional to the displacement of the weight, the current is proportional to the square root of the displacement; so that from the scale reading the value of the current can be. obtained by taking the square root and multiplying by a certain constant.

In addition to the finely-divided scale referred to, there is a fixed inspectional scale shown above the other in the figure; the reading on which gives an approximation to the value of the current. For fine adjustment of the zero a small metal flag is provided, as in an ordinary weighing balance. This flag is actuated by a fork having a handle outside the case, as shown protruding just below the base of the instrument in Figure 53. At the right-hand end of the balance there is a trough into which a counterpoise weight is placed. The latter is for balancing the weight of the carriage and its contained weight. Several pairs of weights (moving and counterpoise) are supplied with each instrument; these weights are adjusted in the ratios of 1, 4, 16, and 64.

Composite Balance.—This instrument is in principle similar to the ampère balance, and can be used for the measurement of power, pressure, or current. It is represented diagrammatically in Figure 54. The left-hand pair of fixed coils are made of copper cable capable of carrying 500 ampères, and connected to two terminals at the back of the instrument. The other pair of fixed coils are wound with the same size of wire as the movable coils, and connected to the terminal T<sub>2</sub>

and contact S. The movable coils are in series, one end being connected to the terminal  $T_1$  and the other to the switch lever L. The switch allows the movable fine wire coils either to be included in the circuit by themselves when the lever is in contact with  $T_2$ , or in series with the fixed fine wire coils when in contact

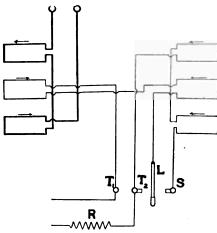


FIG. 54.—Diagram of connections for Kelvin's composite balance.

with S. The fixed and movable coils have a resistance of about 18 and 12 ohms respectively.

To enable the composite balance to be used as a direct reading wattmeter or voltmeter, a separate non-inductive resistance R, having four tappings, is connected as shown: The balance is provided with four pairs of weights, which, together with

the extra resistance, can be adjusted to give a round number of watts or volts per division.

To use the balance as a voltmeter the switch is turned to S. When being used as a wattmeter the fixed fine wire coils are cut out of circuit by moving the switch to T<sub>2</sub>, and the thick wire coils are connected in series with the main circuit. When using the balance as a centi-ampère meter the switch is turned to S. To use as a hecto-ampère balance the main current is sent through the thick wire coils, and a pre-determined constant current through the two movable coils.

Potentiometer.—The potentiometer is one of the most reliable instruments to use as a standard for the measurement of current, electromotive-force, and resistance. Measurements are made by opposing an unknown E.M.F. or P.D. by a known P.D., which exists between two points of a suitable resistance, frequently in the form of a wire.

The principle is illustrated in Figure 55. The potentiometer itself consists of a long wire AB of uniform cross-section fixed between two terminals at A and B. In series with AB is a cell E to provide a constant E.M.F., and a variable resistance R, the positive terminal of E being joined to A. If the positive terminal of a second cell  $E_1$  be connected to A, the former will be at the same potential as the latter, and the difference of potential between A and the free end D will be the same as the

E.M. F. of E<sub>1</sub>. By means of the variable resistance R the P.D. across AB is adjusted, so that there will be a point on AB at the same potential as D, and if D be connected to this point C no current will flow. The P.D. be-

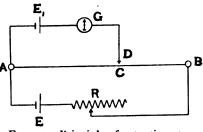


FIG. 55.—Principle of potentiometer.

tween A and C is then equal to the E.M.F. of  $E_1$ , and since the wire AB is uniform the length AC is a measure of the E.M.F. of  $E_1$ . If contact be made to the right of C, current will flow from D through  $E_1$  to A, and if contact be made to the left of C, current will flow in the reverse direction. So that by inserting a galvanometer G in series with  $E_1$  the point C can be located.

There are several forms of potentiometers, but they all work on the above principle, so that a description of one form will be sufficient to illustrate the application of the principle.

The instrument illustrated in Figure 56 works entirely by adjusted resistances, so that there is no slide wire liable to injury. A secondary cell is joined to the terminals F, and sends a current through the dials C and D and the adjusting resistances K and H, the latter all being connected in series. In the dial C are 150 exactly equal resistances. The dial D is also divided into 100 equal resistances, the sum of which is equal to one of the resistances in dial C. The two together are therefore equivalent to a slide wire with 15,000 fixed contacts at equal distances. The adjusting resistances K and H are

provided, so that when working with one accumulator the instrument can read volts direct with a Clark cell.

To calibrate the potentiometer a Clark cell giving 1.4340 volts at 15° C. is connected to A + and A -.

The switch L is moved into the position AA, and a suitable galvanometer is connected to the galvanometer terminals G. Assuming the voltage of the Clark cell to be 1.4340, the arm of the dial C is set to 143 and that of dial D to 40. The galvanometer key is then closed, and the resistances K and H adjusted until there is no

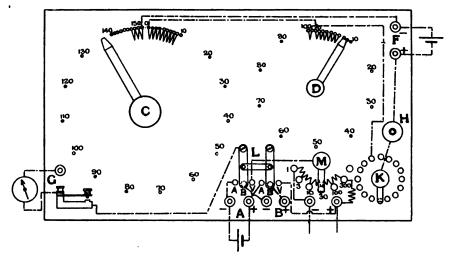


FIG. 56.—Potentiometer.

deflection of the galvanometer. The instrument is thus calibrated, so that one division on C equals 0.01 of a volt, and one division of D equals 0.0001 of a volt.

An E.M.F. lower than 1.5 volts is joined to the terminals B+ and B-, and the switch is set to the position BB. The dials D and C are adjusted until the galvanometer gives no deflection, when the dial readings give the value of the E.M.F. being measured.

Any voltage higher than 1.5 has to be measured on the terminals marked + and -, and with the switch L turned to V V. The switch M is then turned to a convenient multiplying power, either 3, 10, 30, 100, or 300, and the readings obtained by the dials C and D multiplied

by this multiplying power. For example, suppose the voltage to be measured is approximately 460, the switch M is set to 300 and the dials C and D adjusted. Suppose that when a balance is obtained, the former is at 150 and the latter at 4, then the voltage being measured =  $1.504 \times$ 300 = 451.2 volts.

For the measurement of current a known resistance is connected in series with the circuit whose current it is required to know, and by measuring the fall of potential in the resistance the current can be calculated.

# ELECTRICITY SUPPLY METERS

An electricity supply meter has to measure the rate of using power, and therefore should record the product of ampères, volts, and time in Board of Trade units.

The meter should be so designed that it satisfies the following conditions:

- 1. Simple construction, and not liable to derangement.
- 2. Low-power consumption.
- 3. Insusceptibility to temperature changes and stray magnetic fields, and sensibility to the smallest load.
- 4. Permanent accuracy at all loads.

Condition 2 is of great importance, as a supply meter should be designed to absorb the minimum amount of power. In a good instrument the power wasted should not exceed 0.5 of a watt in the coils carrying the main current, and if there be a fine wire coil the loss in it should never exceed 2 watts.

The author has known the fine wire coil to absorb as much as 5 watts, and as these fine wire coils are always connected to the supply circuit, the energy lost per annum may assume a considerable amount. instance, in the above case where the fine wire coil absorbed 5 watts, suppose one Board of Trade unit cost 3d., then in one year the meter would absorb, due to this cause alone,  $\frac{5 \times 24 \times 365}{1000} = 44$  Board of Trade

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units, and this would mean an annual loss of 11 shillings. In a large supply system, where there may be hundreds of such meters, the loss might amount to hundreds of pounds per annum.

By applying the same precautions as in ammeters and voltmeters, the first part of condition 3 can be easily secured, and the second part of the same condition may be observed by so reducing the coefficient of friction of the moving parts that the meter will start when the smallest power-consuming apparatus is switched on to the supply mains.

Condition 4 is of importance to both the consumer and the supply company. If the meter read low then power is supplied for which no return is received. On the other hand, if the meter read high the consumer is paying for more than he receives.

Modern supply meters may be divided into two classes. First, those in which the Board of Trade units are recorded by simply integrating current and time, the supply voltage remaining constant. The ampère-hours can then be multiplied by a constant to give watt-hours, though even this is not necessary, as the instruments can be calibrated to record directly in Board of Trade units. Those meters which do not take into account the difference of pressure, are known as ampère-hour or coulomb meters. To this class the majority of supply meters belong.

Second, those in which the Board of Trade units are recorded by integrating current, pressure, and time. They measure the true energy absorbed by a circuit, and are known as watt-hour meters.

Again, according to the principles upon which they work, electricity supply meters may be divided into three distinct types, each of which comprises both of the classes referred to.

- 1. Chemical or electrolytic type.
- 2. Motor type, which may be sub-divided into-
  - (a) Meters in which the rotating part is a wound armature;
  - (b) Meters in which the rotating part is mercury.
- 3. Clock type.

In order to demonstrate the application of the principles involved, a meter belonging to each of the types will now be explained.

Chemical or Electrolytic Meter.—The principle on which these meters work is that when a current is passed through an electrolyte the deposition is proportional to the quantity of electricity. Figures 57 and 58 indicate

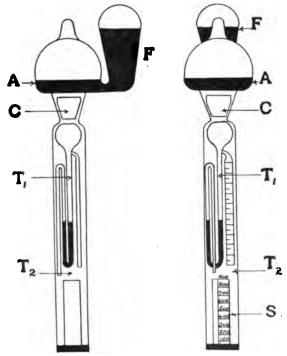


FIG. 57.—Electrolytic meter.

the arrangement and electrical connections of a meter of this type.

F is a reservoir filled with mercury and connected by a narrow neck to a flat glass vessel, the lower part of which is provided with an annular groove containing the mercury A. This circle of mercury forms the anode. The cathode C is in the form of a bowl and made of iridium, a metal which is not amalgamated by the electrolyte. The electrolyte consists of a solution of

mercuric iodide in excess of potassium iodide, which forms the salt  $K_2HgI_4$ . The entire vertical tube  $T_2$  is filled with the latter and then hermetically sealed.

In series with the electrolyte is placed a high resistance H, and both are connected in parallel with a low resistance shunt K made of manganin strip. The

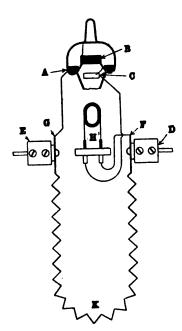


Fig. 58.—Diagram of connections for electrolytic meter.

relation between the resistance of the shunt and the electrolyte is such that only 100 of the current to be metered is passed through the electrolyte. Referring to Figure 58, the current enters at the terminal E, and the greater part passes round the low resistance K to the terminal D. The operating current passes from E to the anode A, through the electrolyte to the cathode C: hence it goes by way of the resistance H to the terminal D.

When current is passed through the meter the electrolyte is decomposed, and the mercury along with the iodine travels to the anode, while the potassium travels to the cathode: but the potassium

never appears as such, for it acts on the surrounding liquid, forming iodide of potassium and liberating mercury, which falls in minute globules into the first graduated tube T<sub>1</sub>. At the anode, mercury dissolves to mercuric iodide, and a large excess of potassium iodide keeps this in solution by forming constantly K<sub>2</sub>HgI<sub>4</sub>.

The tube T<sub>1</sub> is graduated to read direct in B.T.U., and is made in the form of a syphon, so that when it is filled by a quantity of mercury equal to 100 units it automatically and completely empties itself into a lower

tube  $T_2$ , which is provided with a scale S, of which each division is equal to 100 units. There are nine of these divisions, bringing the total capacity of the meter up to 1000 units.

The mercury as it is dissolved from the anode is simultaneously replaced by fresh mercury drawn from the anode feeder F. The mercury in the latter forces its way past the narrow neck connecting the two vessels, when the level of the mercury A falls slightly. After 1000 units have been registered the meter has to be re-set to zero. This is done by inverting the tube, so that the mercury is returned to the anode and feeder.

The point at which the mercury syphons over is first determined by experiment, and the distance between this point and zero is made equal to 100 units. The volume of the measuring tubes varies according to the voltage of supply. For example, if an instrument which reads up to 1000 B.T.U. be placed in a circuit taking 100 ampères at 500 volts, then the mercury should fill

the tubes in 20 hours, recording  $\frac{20 \times 100 \times 500}{1000} = 1000$ 

B.T.U. Now suppose the same meter is placed in a circuit taking the same current, but this time at 250 volts, since the amount of mercury liberated is proportional to the current and independent of the voltage, the measuring tubes would become filled in 20 hours as before, and 1000 B.T.U. would be indicated, when only 500 had been used. To remedy this the measuring tubes would have to be replaced by ones having double the volume, and thus taking 40 hours to fill. Each meter will only read correctly when used in a circuit having the same voltage as that for which the meter was calibrated. In the meter described the tube  $T_1$  is so graduated that 2 millimetres represent 1 B.T.U.

Example.—In the above meter the electro-chemical equivalent of the electrolyte is 0.001037. The first graduated tube T<sub>1</sub> has a length of 20 centimetres, and syphons over when 100 B.T.U. are recorded. Find the internal bore of this tube for two meters, one to be used on 230 volts and the other on 460 volts. A cubic

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centimetre of mercury weighs 13.6 grammes, and 100 of the main current goes through the electrolyte.

Weight of mercury deposited

 $=e \times \text{coulombs}$  passed through the electrolyte.

Ampère-hours passed through the main circuit when pressure is 230 volts

$$=\frac{100 \times 1000}{230} = \frac{10,000}{23}.$$

Therefore coulombs passed through the electrolyte

$$= \frac{10,000}{23} \times 3600 \times \frac{1}{100} = 15600.$$

Weight of mercury deposited

 $= 0.001037 \times 15600 = 16.3$  grammes.

Volume of mercury deposited

$$= \frac{16.3}{13.6} = 1.2 \text{ cubic centimetre.}$$

Area of cross-section of tube

total length of tube containing mercury

$$=\frac{1.2}{2\times20}$$
 = 0.03 square centimetre.

If d denote the internal bore of the tube, then

$$0.03 = \frac{\pi d^2}{4}$$
  
or  $d = \sqrt{\frac{0.03 \times 4}{\pi}} = 0.19$  centimetre.

Therefore a meter used on a 230-volt circuit will be provided with a tube having an internal bore of 1.9 millimetre. By a similar calculation it will be found that for a 460-volt circuit the internal bore of the tube should be 1.4 millimetre.

The relation between the resistance of H and K is calculated in the first instance. The consideration which determines the resistance of the shunt K is the all-important one of the fall of potential across the meter terminals, which ought to be as low as possible to prevent undue loss of energy, yet high enough to give an appreci-

able reading for 1 B.T.U. The potential drop in these instruments varies between 0.5 and 1 volt.

The current in the main circuit when the demand is one unit per hour =  ${}^{1000}_{E}$ , E being the pressure of supply. From the formula  $W = e \times C \times t$  the following equation is obtained:

Grammes of mercury per millimetre on scale

$$=e \times \frac{1000}{E} \cdot \frac{R}{r}$$

Where R is the resistance of K and is calculated from a knowledge of the permissible volts drop at full load, r = total shunt resistance and e = the electro-chemical equivalent of the electrolyte. The resistance between the electrodes is measured, and knowing this the value of the additional resistance H to be placed in the shunt can be found, so that the total shunt resistance = r.

The exact final adjustment is made during calibration by sliding the wires G and F up or down in the terminals E and D, and so varying the value of K. When the final adjustment has been effected the ends are brazed to the shunt as shown.

In the early forms of shunted electrolytic meters great difficulty was experienced in overcoming the back E.M.F. set up between parts of the electrolyte of differing densities. This back E.M.F. should be reduced to a minimum, as the impressed E.M.F. sending the current through the electrolyte never exceeds 1 volt. The back E.M.F. in the meter described is almost eliminated by suitably stirring the solution; this is done by gravity and is entirely automatic. Referring to Figure 59, the heavy solution formed at the anode falls, while the less dense solution at the cathode rises, the interchange of the solution being assisted by the curved surface of the mercury anode. This process is illustrated in the figure, the stream lines in the solution being shown.

Changes in temperature may also affect the accuracy

of electrolytic meters if they are badly designed.

The resistance of an electrolyte diminishes with increase of temperature, while the reverse takes place

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in a copper wire. If, therefore, the shunt resistance H, in Figure 58, be wound with a sufficient proportion of copper, within given temperature limits, the variation in its resistance will counterbalance that of the electrolyte. The resistance between the electrodes having been measured for this purpose, the requisite amount of copper wire is first wound, and the remainder of the total calculated resistance in the shunt circuit is made up of a material having a negligible temperature coefficient.

Motor Meters: (a) With wound armature.—The meter to be described registers watt-hours, and has

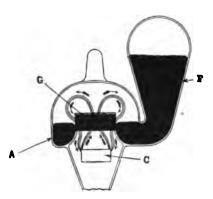


FIG. 59.—Details of top of tube, showing stream lines of circulation in electrolyte.

A. Mercury anode.

C. Iridium cathode.

F. Anode feeder.

G. Glass fence.

been devised by Professor Elihu Thomson. It consists essentially of a small motor in which the field coils carry the main current, and the armature is energised by a potential current.

Referring to Figure 60. The field coils C consist of two coils of thick wire, one on either side of the armature, connected in series with each other and the circuit whose energy is to be measured. The armature A consists of

a hollow ebonite frame wound with a set of coils of very fine wire, and the ends of the wire are attached to a small silver commutator E. The armature is fixed to a spindle S, which is set vertically, as shown: the lower end of S rests in a jewelled bearing B, and the upper end is geared into a chain of wheels actuating the counting mechanism. Two light springs with silver contact pieces bear upon the commutator, and constitute the brushes.

The fine wire armature is in series with a high

resistance fixed to the back of the instrument and having a negligible temperature coefficient. These form the

"pressure coils," the current in which varies with the volt-

age.

The pressure coils, having a resistance of about 3000 ohms per 100 volts, are permanently connected across the supply mains, so that, when a current flows in the field coils C, a magnetic field is set up across the armature and the latter tends to rotate. There being no iron parts, the speed of the motor will be directly proportional to the armature current x field coil current.

The torque producing rotation = H l m i dynes, where

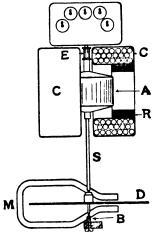


FIG. 60.—Motor meter with wound armature.

H = strength of field in which armature rotates, and is proportional to the main current C.

l =active length per turn of wire on armature.

m = number of turns of wire on the armature.

i = absolute units of current in the armature coils, and is proportional to the supply pressure E.

Since l and m are constant, the driving torque  $\infty$  EC  $\infty$  watts.

Now, assuming there is no friction, the speed will continue to increase indefinitely, so that it becomes necessary to introduce some retarding force to make the speed vary directly as the watts. This is accomplished by fixing to the spindle a small copper disc D, which rotates between the poles of three permanent magnets (only one, M, is shown in the figure). The eddy currents induced in the disc form a drag on the motor. The ohmic resistance of the disc remaining constant, it is evident that in a constant magnetic field such as is supplied by the permanent magnets, the current generated in the disc will vary directly as the speed. Thus a retarding force has

been provided, which bears the same proportion to the speed as the torque of the motor bears to the watts. The speed of the spindle actuating, the indicating mechanism will therefore be directly proportional to the watts.

Friction would very easily affect the accuracy of this instrument, and is compensated for by having a coil R in series with the armature wound along with the large coils C. This coil R being permanently connected to the mains, produces a magnetic field strong enough to just overcome the friction losses, so that the armature begins to rotate when the smallest power-consuming apparatus is switched on.

There is one inherent weakness in this method of overcoming friction, namely, should the supply voltage rise by a few per cent., then the field due to the coil R may be strong enough to start the

armature.

Example.—A meter of this type has field coils which produce, at full load, a flux across the armature of intensity 200. If the meter be intended for use on a 230-volt circuit, from the following data calculate the number of turns required for the armature.

```
Length of armature l = 5 centimetres.

Diameter of armature d = 5 centimetres.

Resistance of armature circuit = 7000 ohms.

Torque required at full load = 3000 dyne-centimetres.

Torque producing rotation = Hlmi dynes.

or 3000 = Hlmir dyne-centimetres.

where r = radius of armature = \frac{d}{2} = 2.5 centimetres.

H = 200 l = 5 i = \frac{230}{7000 \times 10} C.G.S. units.

Therefore the effective turns on armature = m = \frac{3000 \times 7000 \times 10}{200 \times 5 \times 230 \times 2.5}
```

= 365.

The turns constituting the armature winding set up a flux which may be divided into two equal parts: (1) The effective flux at right angles to the field flux, and (2) the ineffective flux in a direction parallel to the former. Since both components are equal, and the same current flows in each coil, the total number of turns =  $\sqrt{2}$  x effective turns =  $\sqrt{2}$  x 365 = 515.

(b) With rotating mercury.—A meter of this type

is illustrated in Figure 61. It consists of a permanent steel magnet A, having wrought - iron pieces B<sup>1</sup> B<sup>1</sup> attached it. the latter terminating in circular poles B B. The mercury chamber is formed between the ebonite blocks E E of circular form. which the pole pieces are embedded. The metal ring (Fig. 62), lined with leather, surrounds the two ebonite blocks and forms the side of the mercury chamber. The copper disc D lies in the mercury and is attached to a spindle F running in jewelled

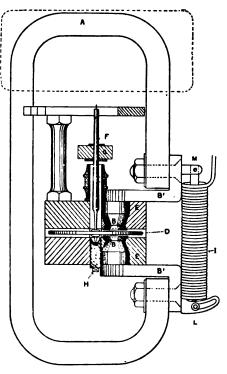
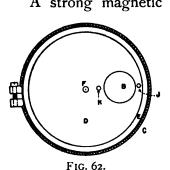


Fig. 61.—Motor meter (with rotating

The lower jewelled centre is shown carried centres. by the screw H. The upper end of the spindle is geared to and drives a counting train, the dials of this train being graduated in Board of Trade units. G is a brass weight which counterbalances the armature and prevents it from floating. Figure 62 is a horizontal section showing the position of the poles B

and the disc D. It also indicates the wires I and K, embedded in the ebonite, which convey the current to and from the mercury.

The action of the meter is as follows:



A strong magnetic field is produced between the poles B B by the magnet A. The current to be metered enters the mercury chamber at I, flows across the mercury to K, causing the former to rotate at a speed proportional to the current. The motion of the mercury is conveyed to the recording train of wheels by means of the disc D immersed in the mercury and carried

round by it. The brake force of the meter is provided by the eddy currents induced in the disc D as it revolves between the poles BB. This braking force, as in the previous case, is directly proportional to the

speed.

As the speed of the rotating parts increases the retardation due to the fluid friction of the mercury also increases, so that if no means is adopted to reduce the eddy current braking action, the meter would register low. This error amounts to 5 per cent., but is corrected for by winding a coil I, which carries the main current, on an iron core L M. The action of the coil is to divert part of the lines of force from the magnet poles B to the path L M. This weakens the field producing eddy currents in the disc D, and consequently reduces the retarding force. By adjusting the number of turns constituting the coil I, the reduction in the eddy current braking can be made to exactly compensate for the increased retardation due to fluid friction. The iron core L M is hinged so that the movement to or from the poles B<sup>1</sup> B<sup>1</sup> provides a sensitive adjustment of the speed of the meter. measuring very large currents these meters are shunted across a low resistance, so that only a fraction of the main current goes through the meter.

Clock Meters.—Meters belonging to this type work by the influence of a magnetic field set up by a current upon a swinging pendulum. Figure 63 illustrates a meter of this type in which two pendulums are employed, and the difference between their periodic time is recorded on a set of dials. Great sensitiveness is obtained by accelerating one pendulum and retarding the other, the change in the periodic time in each case being produced by the magnetic attraction or repulsion between coils carrying the main current and other coils which are attached to the pendulums and energised by the supply voltage. The difference in periodic time

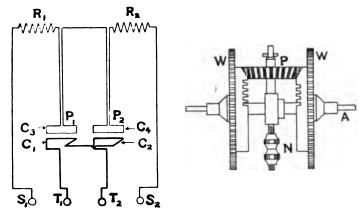


Fig. 63.—Clock meter.

thus produced is proportional to the watts, and is recorded through a chain of wheels on the dials of the meter.

Referring to the figure, T<sub>1</sub> and T<sub>2</sub> are the two main terminals. The current of the circuit to be metered enters at T<sub>1</sub>, and passes through the two coils C<sub>1</sub> and C<sub>2</sub> to the terminal T<sub>2</sub>. S<sub>1</sub> and S<sub>2</sub> are the terminals of the fine wire coils C<sub>3</sub> and C<sub>4</sub>, which are connected in series with the resistance R<sub>1</sub> and R<sub>2</sub>. The coils C<sub>3</sub> and C<sub>4</sub> are wound on the pendulums P<sub>1</sub> and P<sub>2</sub> respectively, and carry a current proportional to the voltage. and C<sub>3</sub> are so wound that they retard the oscillations of the pendulum P<sub>1</sub>, while C<sub>2</sub> and C<sub>4</sub> accelerate the oscillations of P<sub>2</sub>. The difference in the oscillations of

the two pendulums is recorded on the dials through differential gear also shown in Figure 63. The two side wheels WW run loose on the main driving axle A, and are driven in opposite directions at speeds proportional to the rate of oscillation of the two pendulums respectively. P is the planet wheel which gears into WW, and so long as the latter revolve at the same speed the planet wheel will simply turn on its own axis. On the other hand, if the wheels WW are driven at different speeds the main axle, which is at right angles to them, will revolve, carrying the planet wheel and its counterpoise nuts N bodily with it. To the main horizontal axle A is geared the counting mechanism, whose indications will be proportional to the difference in speed between the two side wheels.

The winding gear consists of an electro-magnet which pulls round an armature once every 30 seconds, winding up a short stiff spiral spring which releases itself and drives a double set of clockwork. By this

addition the meter is made entirely automatic.

# MAXIMUM DEMAND INDICATORS

These instruments are often connected in series with consumers' mains to determine the price to be charged

for the electrical energy consumed.

The expenses incurred in connection with a generating station may be regarded as consisting of two separate and distinct parts, namely, standing charges and running charges. The standing charges are made up of such items as interest on borrowed money, depreciation, taxes, wages, and repairs; these charges are, for a station of given capacity, the same whatever the load may be. The running charges include cost of fuel, oil, etc., and in a modern generating station do not exceed 0.5 of a penny per unit generated.

Now consider two consumers A and B each requiring the same amount of energy (say 20 B.T.U.) over a given period. Suppose A's 20 units to be made up of 10 kilowatts for 2 hours, while B's 20 units are made up of 2 kilowatts for 10 hours. Plant to the extent of

10 kilowatts must be provided in the station for A's requirement, while only 2 kilowatts are required to supply B, so that the standing charges in A's case will greatly exceed those of B, while the running charges will be practically the same.

It will therefore be seen that in two cases where the total energy consumed in a given time is the same the consumer requiring a large supply of power for say one hour is not so profitable as the consumer who requires a less amount of power for the greater part of 24 hours. In order to differentiate between good and bad consumers the greatest amount of power which is required at any period is measured by a maximum demand indicator, which is connected along with the supply meter in series with the consumer's mains. The consumer is then charged at the rate of say 6d. per unit for the first 100 hours at the maximum rate of demand, and 3d. to 1d. per unit afterwards. For instance, suppose an energy meter indicates that 500 B.T.U. have been consumed and the demand indicator reads I kilowatt. the consumer at the above rate is charged 6d. per unit for 1 kilowatt x 100 hours = 100 B.T.U., and 3d. to 1d. according to the nature of the demand for the remaining 400 units.

It is essential that the demand indicator should be sluggish in its action, so that it does not record momentary rises in current due to the switching on of a motor or an arc lamp. In fact, demand indicators should measure the average maximum value of the consumer's load.

Demand indicators are invariably constructed on either the thermal or electro-magnetic principle, and an example of the former type is shown in Figure 64. In principle the instrument is practically a differential recording thermometer, which measures the heat produced by an electric current. It consists of two bulbs A and B, of approximately the same size, connected by a U-tube C filled with a very hygroscopic liquid, and provided with a third graduated tube D closed at the bottom. A hygroscopic liquid, such as sulphuric acid, is necessary in order that the air in both bulbs may be kept free from

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aqueous vapour. Round the bulb A is wound a heating coil E consisting of one or two turns of platinoid strip, the ends of which are brought out to the two

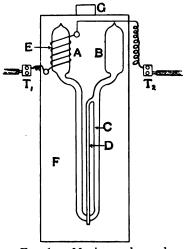


FIG. 64.-Maximum demand indicator.

into the right-hand bulb.

terminals  $T_1$  and  $T_2$ . coil E is connected in series with the main circuit, and the heat produced due to the passage of a current causes the air in bulb A to expand and depress the column of liquid in the lefthand limb of the U-tube, with the result that it rises in the other limb and slowly overflows into the reading The height which the liquid rises indicates the maximum current which has passed through the coil E.

The tubes are fixed to a board F, which is hinged at G inside an iron case. To re-set the instrument the board is tilted, thus allowing the liquid to flow completely out of the reading tube

### CHAPTER V

#### STORAGE BATTERIES

If two plates, one of pure lead and the other of lead peroxide, be placed in dilute sulphuric acid and connected to an ammeter a current will flow through the circuit, leaving the cell at the lead peroxide plate. After a time the surface of the plates becomes changed and the current gradually falls to zero. On sending a current through the cell in the opposite direction the plates return to their original condition, and the cell will again supply current.

Such a cell was discovered by Planté in 1860, and is known as either a storage cell, a secondary cell, or an accumulator. The process of regeneration is known as charging, and discharging takes place when the cell supplies current. The plate by which the current leaves the cell during discharge is called the positive plate, and the other the negative plate. Positive or lead peroxide plates are of a dark brown colour, while negative plates are a neutral grey.

An electrical storage cell may be defined as a piece of apparatus which is capable of receiving, retaining, and giving up again, when required, electrical energy. The name "storage cell" or "accumulator" might convey the idea that cells store electricity as electricity, but this is incorrect; the electrical energy put into the cell is converted into chemical energy, and the larger portion of the latter is transformed again to electrical energy during discharge.

The lead and lead peroxide are called the active materials of the cell, and, as will be seen, must be of a

spongy formation and supported by heavy grids, usually of lead.

A lead/lead peroxide-sulphuric acid cell gives an E.M.F. of about 2 volts when fully charged, and of the energy put in during charge 60 to 80 per cent. can be withdrawn.

Chemical Action.—A storage cell generates electrical energy in virtue of the chemical reactions which take place between lead, lead peroxide, and dilute sulphuric acid. There has been considerable discussion among electro-chemists as to the precise chemical changes which take place in the active materials during the periods of charge and discharge, and many theories, more or less hypothetical in character, have been evolved. There is, however, no doubt that the primary active constituents of the plates are finely divided metallic lead in the case of the negative plate and lead peroxide in the case of the positive: further, that when the plates are in a discharged state a considerable amount of lead sulphate (PbSO<sub>4</sub>) is present, and the electrolyte is reduced in specific gravity by the absorption of sulphuric acid.

Discharging. — When a cell is discharging it is probable that the lead on the negative plate liberates the hydrogen from the sulphuric acid and forms lead

sulphate-

$$Pb + H_2SO_4 = PbSO_4 + H_2.$$

The hydrogen thus set free travels to the positive plate and there unites with some of the oxygen, forming lead monoxide and water—

$$PbO_2 + H_2 = PbO + H_2O.$$

The lead monoxide thus formed unites with sulphuric acid, and forms lead sulphate and water—

$$PbO + H_2SO_4 = PbSO_4 + H_2O.$$

The reactions may not take place exactly in these stages, but the final result of discharge is that the lead and lead peroxide have partly become lead sulphate, and the density of the electrolyte has been lowered, due to the replacement of sulphuric acid by water. The

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following equation shows the change which takes place on the surface of the plates during discharge—

$$PbO_2 + 2 H_2SO_4 + Pb$$
  
=  $PbSO_4 + 2 H_2O + PbSO_4$ .

The actual composition of the active materials and electrolyte is not that indicated by the above equations. No cell contains pure sulphuric acid when fully charged, but the latter is diluted with a certain percentage of water; likewise, the water formed during discharge is mixed with sulphuric acid. The electrolyte is generally made in such proportions as to be given by  $H_2SO_4 + 14$   $H_2O$  and  $H_2SO_4 + 20$   $H_2O$  in a charged and discharged cell respectively. The symbol PbSO<sub>4</sub> also does not represent the true composition of the active material, there still remaining at the end of discharge some of the original lead and lead peroxide.

Experiments show that as much as 40 per cent. of the active material may still remain under the lead sulphate.

Charging.—During charging the elements are brought back to their original state, due to the desulphating of the active material. The charging current decomposes some of the water in the electrolyte into oxygen and hydrogen, and at the negative plate hydrogen acts on the lead sulphate, forming lead and sulphuric acid—

$$H_2 + PbSO_4 = Pb + H_2SO_4$$

At the positive plate the oxygen reacts on the lead sulphate and water of the electrolyte near to the active material, forming lead peroxide and sulphuric acid—

$$PbSO_4 + H_0O + O = PbO_0 + H_0SO_4$$

Again there is considerable doubt as to the accuracy of the above stages, but the resultant reaction during charge is known to be given by

$$PbSO_4 + 2H_2O + PbSO_4 = PbO_2 + 2H_2SO_4 + Pb.$$

While the active material is being desulphated no gas is evolved, but when the charging is nearly complete

hydrogen is liberated at the negative and oxygen at the

positive.

The sulphate of lead which is formed on the surface of the plates during discharge is insoluble and a bad conductor, so preventing the electrolyte from coming into contact with the active material. When sulphate covers the entire surface of the plates chemical action ceases, and the cell is said to be discharged. Hence the necessity for giving the active material as large a surface as possible, for the time occupied in covering the plates with sulphate will be longer, and consequently the cell will maintain a certain current for a longer period. The capacity of a cell therefore depends on the area of active material exposed to electrolytic action, and to be economical the surface should be as great as possible for a given weight of plate.

### FORMATION OF PLATES

The active materials, being porous, are mechanically weak; they have therefore to be supported by massive grids. The usual practice is to make the supports of either cast, rolled, or drawn lead, which must be as free from impurities as possible. The impurities in the lead forming the grid should not exceed 0.1 per cent., as any foreign material mixed with the lead causes corrosion and oxidation by local action, as will be explained hereafter.

Of impurities, copper is the most detrimental to the life of the plates, being transferred to the electrolyte, and there setting up a continuous counter E.M.F. which prevents the cell from retaining its charge for a reason-

able period of time.

The lead forming the grid is sometimes alloyed with I per cent. of antimony to add to its strength; but where present in larger quantities antimony may make the plate too rigid, so that it will crack, due to the expansion of the active material, whereas if the plate be more elastic it will stretch sufficiently without suffering damage. This is particularly the case with positive plates.

The structure of the grid must be sound and

homogeneous. This is, however, difficult to obtain,

owing to the complicated nature of the surface.

Plates are divided into the two following types, according to the process by which the active material is obtained—

- 1. Planté Plates.
- 2. Faure Plates.

Planté Plates.—These plates have their active material formed from the grid itself by electrolytic action, and are often referred to as formed plates.

If two plates of pure lead be put into a solution of dilute sulphuric acid, and a current sent through the electrolyte from plate to plate, the positive almost immediately gives off oxygen and becomes covered with a thin film of lead peroxide, while the other plate remains unaltered. Electrolytic action is set up, the water decomposing into its two elements hydrogen and oxygen; the latter unites with the lead on the positive plate and forms lead peroxide, while the hydrogen escapes. The chemical reaction may be represented thus:

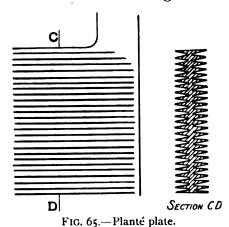
$$Pb + 2H_2O + Pb = PbO_2 + 2H_2 + Pb.$$

After a few minutes the thickness of the lead peroxide film shows no increase, and immediately the current is switched off the film of lead peroxide is reduced to lead sulphate by the action of the sulphuric acid on the plate. On again applying the current the sulphate is peroxidised, forming a thicker coating. Repeating these cycles, at each successive reversal the oxidising and reducing action sinks more deeply into the plates until the desired surface of spongy material is obtained.

As the formation proceeds the amount of lead peroxide increases, and the periods of rest must be lengthened to hours and ultimately to days. The formation of the active material in this manner is therefore a very tedious process, and to accelerate it, methods have been adopted to open up the lead peroxide and allow the acid to penetrate it more easily. This is done by

discharging the plates through a resistance after each charge, instead of leaving them on open circuit. The plates, however, should not be discharged too rapidly, because, if the peroxide is not allowed to assume a crystalline form before its reduction the soft oxide may be forced away from its support by the evolution of gas from the metallic surface. To further accelerate the process of forming, the plates are made either corrugated or ribbed; and besides these mechanical processes some manufacturers boil the plates in dilute nitric acid, so as to give to them as large a surface as possible before they are formed. By forming plates in this manner the developed surface may be increased to nine or twelve times the smooth surface.

In practice, where both positive and negative plates are to be formed, it is more economical to form both as positives against dummy negatives, and then reverse those intended to be negatives during the final charge, in



which case the lead sulphate is changed into pure spongy lead.

Grids for Plante plates are made in several forms, of which Figures 65 and 66 illustrate two representative specimens.

The form in Figure 65 is cast in one piece, and consists of a lead core carrying a large number of horizontal ribs, upon which the

active material is formed. The plate is about 8 millimetres thick and there are 8 ribs per centimetre.

The second form of plate shown in Figure 66 consists of a lead antimony frame, one centimetre thick, of great strength and stiffness. The holes, about 2 centimetres in diameter, which hold the active material, are cast countersunk on both sides. The active material is made from tapes of pure lead, which are corrugated on one side and

rolled into rosettes. The plate is subjected to a pressure of about 200 tons, which expands the outside face of the rosettes into the counter sinking, thereby riveting the rosettes into the plate. The corrugated ribbons

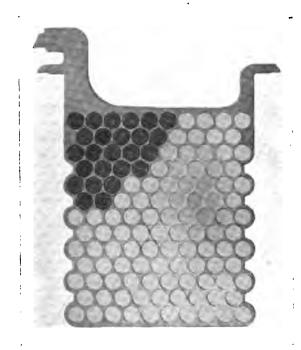


Fig. 66.—Planté plate.

cause the electrolytic action to take place right through the rosettes from one side to another.

Faure Plates.—Plates of this type are prepared by casting grids of pure lead generally containing a large number of small pockets, into which the active material, in the form of a paste, is forced. The grids are so made that the active material is held firmly in position.

The positive plates are pasted with minium or red lead oxide mixed in sulphuric acid; the two combine and form sulphate of lead and lead peroxide, the chemical change being represented by the formula

$$Pb_3O_4 + 2H_2SO_4 = PbO_2 + 2PbSO_4 + 2H_2O_4$$

The lead peroxide and lead sulphate eventually settle into a hard dry porous mass, which adheres to the grid.

The negative plates are pasted with litharge, a mixture of lead monoxide (PbO) and sulphuric acid which also forms lead sulphate. Litharge is used for the negative plates, as it has been found that by this method a given quantity of spongy lead can be formed by a less expenditure of initial charging current. Faure plates when formed are similar to plates in a discharged condition, and when a battery built with these plates is installed, the cells require to be charged at a slow rate, for from 36 to 48 hours continuously.

As both the lead sulphate and lead peroxide with

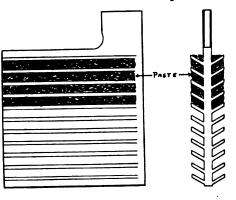


Fig. 67.—Faure plate.

which the positive plate is coated are insoluble in phuric acid, the changing active material into lead peroxide only takes place on the surface, and requires some time to penetrate into the interior. The thickness of the active material depends on the time during

which the sulphuric acid has been allowed to sink into the oxide of lead, so that the capacity of pasted plates increases with their life.

The grid shown in Figure 67 consists of a lead casting having a number of thin horizontal ridges on both sides; the latter are turned upwards so as to hold the active material, which is applied in the form of a paste.

The latest form of pasted plate is illustrated in Figure 68. It consists of two grids riveted together; the outer surfaces are like sheets of lead pierced with numerous holes, and the space between them is intersected by stout horizontal and vertical ribs, which give strength and rigidity to the plate. The ribs also divide up the

inside space into a number of cells, one of which is shown in Figure 69, the insides S of the frames being packed with the active material.

Plates formed by the Faure process are usually much

lighter than Planté plates of the same capacity, but active material which formed by Planté method heres better to the grid than that applied in the form of a paste. In making complete cells plates may be either type; the general practice, however, is to use Planté positive plates and Faure negatives.



FIG. 68.—Form of pasted plate.

Pasted plates, so far as manufacturing is concerned, have a great advantage over Planté plates, in that the

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FIG. 69.—Faure plate.

time required for forming is considerably less, and consequently the expenses of manufacture are lower.

The active material formed from a paste is liable to fall away from the grid, so that special attention has to be given to the method of fixing the pellets of active material into the grid.

Design of a Storage Cell.—To construct a cell of large capacity a number of negative plates are connected

in parallel and alternated with positive plates, also in parallel, as shown in Figure 70. L. Juman has found that a high current density suits the positive much better than the negative plates, and that the best results and highest capacity are obtained by making the total area of the negative plates greater than that of the positives. It is now customary to arrange the plates of a storage cell with a negative at each end, *i.e.* there is one more negative plate than positive.

Each plate has a projection or lug L, and in paralleling a number of plates their lugs are burned into a

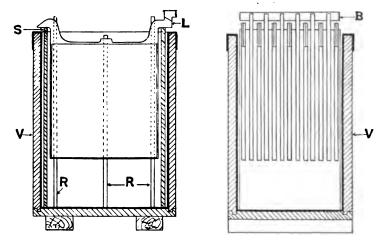


Fig. 70.—Accumulator.

connecting lead bar B. This connecting bar also terminates in a lug having a smooth horizontal or vertical face, by means of which two cells may be joined

together.

The plates are contained in either a glass or teak lead-lined vessel V (the latter being the case in Figure 70), which contains the electrolyte, and are suspended by the lugs from the sides of the containing vessel when of glass, and from stout glass or wood supports S when lead-lined boxes are used. A space varying from 5 to 16 centimetres according to the depth of the plate, should be left clear between the bottom of the plates and the base of the containing vessel. This

allows all waste deposit to sink to the bottom and keep clear of the plates, otherwise adjacent plates are liable to become short-circuited. The plates should be free to expand in all directions, and be separated from each other by two to four insulating rods R of glass or ebonite (for the sake of clearness these are not shown in the section) held upright by guides cast on the lugs of either plate. The distance between adjacent plates varies from 0.6 to 1.2 centimetres, depending on the type of cell. This allows any detached pieces of active material to fall to the bottom without causing an internal short circuit; and also if there be buckling, adjacent plates cannot come into contact.

The electrolyte, as will be explained, should be pre-

pared from very pure sulphuric acid, and diluted with pure water to required specific The specific 3 resistance of sulphuric acid varies with density in a peculiar manner, being a mini-1.220, above and below this value the specific sistance increases. shown in Figure An electrolyte having a specific gravity of 1.22 reduces the internal resistance of the cell. but on the other hand tends to cause trouble

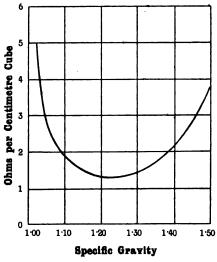


FIG. 71.—Variation in specific resistance of sulphuric acid with density.

due to local action. In general, a cell which is likely to stand for any length of time unused, should have a low density electrolyte, while a cell in constant use may have a higher density.

Variation of E.M.F. during charge and discharge.— The E.M.F. of a charged cell averages about 2 volts, but varies with the density of the electrolyte, other things remaining constant. The curve in Figure 72 indicates the variation of E.M.F. with the specific gravity as obtained by Gladstone and Hibbert,\* from which it will be seen that within the specific gravity limits of 1.07 and 1.300, the E.M.F. is a linear function of the specific gravity. With a lower specific gravity than 1.07 the E.M.F. falls off rapidly. The usual densities range from 1.200 to 1.220 when the cell is charged, to 1.185 to 1.195 when discharged.

During discharge the action of sulphation on the plates and the lowering of the specific gravity of the

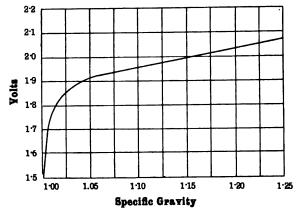


FIG. 72.—Variation of E.M.F. with density of sulphuric acid.

liquid goes on continually, so that theoretically the E.M.F. is always varying. However, by using a cell having a large quantity of acid, and arranging the plates so that the acid in the pores is kept at the same strength as that in the body of the liquid, the E.M.F. remains practically constant during the greater portion of discharge.

Curves in Figure 73 show the variation in E.M.F. of a 180-ampère-hour 13-plate cell during the process of charge and discharge, the normal discharge rate being 21 ampères. These curves may be taken as typical of all lead/lead peroxide sulphuric acid cells.

<sup>\*</sup> Journal of Institution of Electrical Engineers, 1892, vol. xxi. p. 420.

If the discharge be commenced immediately after charging, the E.M.F. rapidly falls from 2.15 volts to about 2 volts, after which it remains approximately constant for some hours. This high but variable initial electromotive-force is probably set up by the adherence to the negative plate of some of the hydrogen evolved towards the end of charge; this, however, is readily oxidised, and the E.M.F. falls to its normal value. This high initial E.M.F. is more noticeable with cells having pasted

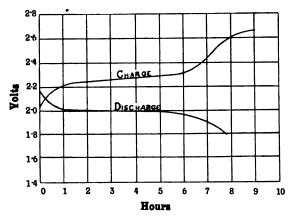


Fig. 73.—Charge and discharge curves of an accumulator.

negatives, due to a much larger quantity of hydrogen adhering to the more porous active material.

As discharge proceeds the E.M.F. remains practically constant at 2 volts for about 4 hours, then, as the electrolyte is lowered in density due to the formation of water, falls more rapidly to 1.8 volts. If discharge be continued beyond this the lead sulphate formed on the plates completely separates the active material from the electrolyte, so that chemical action ceases. Cells discharging at their normal rate should never be further discharged when the E.M.F. reaches 1.8 volts.

On charging, the E.M.F. rapidly rises from 1.8 volts to a little over 2.20, then rises very slowly to about 2.30 volts, which is reached when the cell is about charged. After the voltage of the cell reaches 2.30 it rapidly rises to about 2.6 in a manner shown by the curve.

During the latter period hydrogen is freely evolved, the electrolyte having the appearance of boiling. The cell is

then said to be "gassing."

When a cell is fully charged it has been pointed out that hydrogen and oxygen are liberated at the negative and positive plates respectively. The presence of these gases at each pole of the electrolyte sets up an E.M.F. which opposes the charging E.M.F., hence the increase

in the applied E.M.F.

A cell should never be left in a discharged condition, as reactions take place which are very detrimental to the In a discharged condition the active material has been converted into lead sulphate, PbSO4, and it is supposed that another form of sulphate, expressed by the symbol Pb<sub>2</sub>SO<sub>5</sub>, is formed by the PbSO<sub>4</sub> combining with lead monoxide PbO. This Pb<sub>2</sub>SO<sub>5</sub> is referred to as white sulphate, and when present in considerable quantities is readily recognised. It is only removed with considerable trouble, and should a cell get into this condition it requires to be subjected to a long charge with a small current, which will in time reduce the sulphate to active material. This white sulphate is very adhesive, and should it be detached from the plate during charge it generally carries with it some of the active material.

Local Action.—When a battery remains unused for a period of five or more days the above changes do not take place, but others occur which tend to lower the specific gravity of the liquid, and consequently the E.M.F. of the cell. Should the electrolyte contain any foreign materials, such as copper or iron, they will set up local currents between themselves and the plates, decomposing the sulphuric acid into water, and forming lead sulphate

on the plates.

If this local action goes on for any length of time the plates become sulphated, and the acid is considerably weakened. Too great importance cannot be given to obtaining the electrolyte and plates as chemically pure as possible. With plates of the Planté type, which are given porosity in the course of manufacture by treatment in some oxidising solution containing nitrogen compounds, such as nitric acid, ammonia, and nitrates of sodium,

precautions should be taken to eliminate all traces of these compounds. Assuming the plates to be pure, the main source of trouble is due to impurities liable to be introduced through the medium of the electrolyte. Impurities may be present either in the sulphuric acid, or in the water with which it is diluted. According to Dr. Lunge, the concentrated acid of commerce may contain, among others, the following impurities:

. 135 parts in a million. Sodium Sulphate

Ferrous 291 Lead . 172 Arsenic 500

Copper, Zinc, and Iron . Rarely.
Sulphurous Acid . Varying quantities.

Sulphuric acid is prepared either from sulphur, by heating it in a current of air to form sulphur di-oxide, or from sulphide of iron. The former method gives what is known as "brimstone" acid, and the latter method gives an acid which may contain traces of iron, arsenic, or other metals. It is preferable to use "brimstone" acid (which is free from arsenic) for battery purposes.

Pure water should be used to dilute the sulphuric acid, as ordinary town water contains the following impurities:

Hydrochloric acid. Sulphates. Ammonia. Nitric acid.

Boiler water should under no conditions whatever be used, as it contains among other impurities special alkaline softening fluids. R. W. Vicary has recently found that 10 to 0.1 per cent. of ammonia added to the electrolyte decreases the capacity immediately by some 20 to 30 per cent., thus showing the deleterious effect of nitrogen compounds. G. D. Aspinall Parr \* has found that if 2 per cent. of sulphurous acid be present in the electrolyte, the capacity of a cell is reduced by 50 per

<sup>\*</sup> Journal of Institution of Electrical Engineers, December 1905, pp. 406-420

cent. This local action is about three times greater at a specific gravity of 1.300 than at 1.170 for a temperature of 15° C. Hence the necessity for having a medium density of electrolyte.

Capacity and Output.—The capacity or rated output of a cell is the ampère-hours it will give when discharged at a particular current rate within the practical limits of

charge and discharge.

The absolute capacity would be the quantity of electricity obtained when the cell is discharged until the E.M.F. is zero. By examining the curve in Figure 73 it will be observed that when discharging at a normal rate the E.M.F. remains approximately constant until it reaches 1.80 volts, when it falls immediately to zero. In such a case, practically the whole of the available energy has been withdrawn from the cell by the time it reaches 1.8 volts, and this energy represents the working capacity of the cell. This, as will be explained, is only the case when the cell is discharged at a slow rate, and from Figure 74 it is observed that a large amount of energy can still be withdrawn after the E.M.F. falls to 1.8 volts; in fact in some cells, discharging at a very high rate, the ampèrehours not utilised at this E.M.F. may exceed those actually withdrawn. It is, however, very detrimental to the life of the plates to discharge the cell to a very low E.M.F., no matter how small a percentage of their maximum output has been obtained.

The practical capacity of a cell is usually defined as the ampère-hours the cell will give before the E.M.F. falls to some pre-determined limit, in practice somewhere between

1.9 volts and 1.7 volts, generally 1.8 volts.

The normal charge and discharge current of a cell depends on the type and mechanical strength of the plates, and is expressed in so many ampères per square decimetre of positive, reckoning both sides of the plate. In Planté plates the support surface is large, due to the mode of formation, so that the current density may be higher than with Faure plates. The discharging current of present-day cells varies between 1 and 3 ampères, and the charging current between 0.5 and 2 ampères per square decimetre of positive plate.

In specifying the capacity of a cell the normal rate at which it may be discharged and charged must also be given. The resistance of the cell being low, the discharge current depends on the external resistance. With a low external resistance the cell would discharge at a high rate, and if the current be very high the cell may be ruined in a very short time. High rates of discharge cause the plates to buckle and active material to be dislodged. This is due to the excessive heating of the grid, and probably also to the tendency of the surface layers only of the active material to take part in the voltaic action, producing a non-uniform expansion and contraction.

In Figure 74 are a series of curves obtained from a

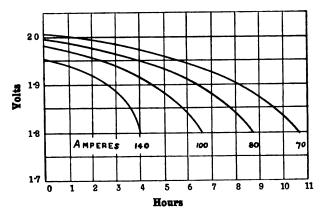


Fig. 74.—Discharge curves of an accumulator.

cell which gave an output of 750 ampère-hours when discharged at its normal rate of 70 ampères. The curves were obtained when discharging at 70, 80, 100, and 140 ampères; as indicated, the outputs at these respective currents in ampère-hours were .750, 700, 650, and 560, respectively, the cell being considered discharged when its E.M.F. fell to 1.8 volts.

The rapid fall in E.M.F. when discharging at high rates is probably due to a diminution in the strength of the acid in the pores of the active material. The acid in the pores is rapidly weakened, as diffusion with the stronger electrolyte in the body of the cell does not take place fast enough, when the former is weakened due to

electrolytic action. That this may be the explanation is obtained from the fact that if a cell discharging at a high rate be put on open circuit after the E.M.F. falls to say 1.8 volts, then the E.M.F. gradually rises to say 1.95 volts, for then the weak acid in the pores becomes diffused with the stronger acid in the body of the electrolyte.

Efficiency.—The efficiency of a storage cell is the ratio of energy given out by the cell during discharge, to the energy required to charge it to precisely the same condition as it was when the discharge commenced.

Energy efficiency =  $\frac{\text{watt-hours output}}{\text{watt-hours input}}$ 

This may vary between 60 and 90 per cent., depending upon the conditions under which the battery has been charged and discharged.

The quantity efficiency is expressed in terms of the ampère-hours output and input, and is given by:

Quantity efficiency = ampère-hours output ampère-hours input

With cells working under normal conditions this varies between 90 and 98 per cent.

If a cell be discharged from 2.4 volts to 1.85 volts and then recharged again to 2.4 volts, and these cycles be repeated, the energy efficiency would be about 80 per cent. for a low rate. A cell which is charged and discharged through a very narrow range during short intervals of time may have a comparatively high efficiency. For instance a cell which is discharged for say five minutes and charged for the same time repeatedly, may have an efficiency of between 90 and 92 per cent.

The longer a cell is allowed to gas during charge the lower will be the quantity efficiency, as during this period the whole of the wasted current takes part in the decomposition of the water of the electrolyte. Should charging be stopped before gassing commences the cell might have an ampère-hour efficiency of nearly 100 per cent., but the de-sulphation of the active material would be incomplete, and if continued would reduce the output

and permanently injure the cell. Local action and external leakage also affect the ampère-hour efficiency.

The ampère-hour efficiency is not affected by internal resistance and gaseous polarisation during charge, but as these cause a lowering of the E.M.F. during discharge and an increase at charge, they affect the watt-hour efficiency.

G. D. Aspinall Parr \* has recently made a series of tests on several large 9-plate storage cells having 4 Planté positives and 5 pasted negatives. The results given in the accompanying table are interesting and instructive, as they show the effects of a variation in the charge and discharge rates on the capacity and efficiency of the cells.

The normal charging current = 32 ampères, discharging current = 29 ampères at the 10-hour rate, and 134 ampères at the 1-hour rate. This table shows clearly that the higher the discharge rate the lower the quantity and energy efficiency.

Discharge.			Ampère- hours.		Watt-hours.		Efficiency.	
Rate in Hours.	Limit in Volts.	Current in Am- pères.	In- put.	Out- put.	In- put.	Out- put.	(Am- père- hour) Quantity.	(Watt- hour) Energy.
10	1.85	29	318	290	764	574	91.2	75.1
6	1.80	42.5	288	255	730	449	88.5	67.7
3	1.75	70	256	220	630	402	85.9	63.8
	1.70	134	168	134	414	247	80.0	59.7

Erection of Storage Cells.—In arranging a battery of cells it is of importance that it be so arranged that each individual cell is easily accessible for inspection purposes. Cells should, when possible, be arranged in rows on wooden stands or shelves, and when in tiers a space of about 30 inches should be allowed between each shelf.

<sup>\*</sup> Journal of Institution of Electrical Engineers, December 1905, vol. xxxii. pp. 412, 413.

Large-sized cells, such as are used in central station work, arranged in single tiers, need only be placed on two timbers running the length of the row, as shown in Figure 75. Small and medium-sized cells are usually arranged on stands built entirely of wood, the dimensions of which must of course depend on the size of cells to be erected and the nature of the connections.

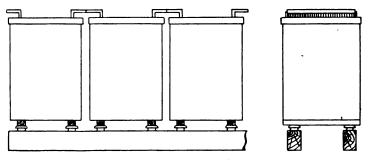


FIG. 75.—Method of erecting cells.

erecting the cells the stands should be well covered with some acid-resisting paint or varnish.

When a battery is almost fully charged it gives off sulphuric acid spray which covers everything, in its immediate neighbourhood, with a film of acid moisture. This would cause a leakage of current to take place from one cell to another by way of the surfaces of the containing vessels, fixings, or earth; and if no means be taken

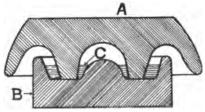


FIG. 76.—Oil insulator for accumulators.

sult from leakages to earth. To prevent this each cell is mounted on four or six mushroom-shaped oil-insulators, shown in Figure 76. The insulators consist of a glass base B having a channel C, in which is placed a quantity of non-evaporating insulating fluid, such as resin oil. In this channel C rests the inner rim

to prevent this the bat-

itself while on open circuit. Should the battery form part of a large distributing plant, serious consequences might re-

might discharge

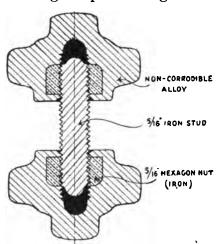
of the upper half of the insulator. Any leakage current from the cell to earth must pass from A to B, and as a portion of the path is across the surface of the oil, leakage is practically eliminated.

Cells contained in lead-lined wood boxes are mounted directly on the insulators: glass boxes, being liable to fracture if they rest directly on the insulators, are placed in wooden trays covered with saw-dust, the tray resting on the insulators.

When connecting a number of cells in series the best connection is effected by burning the positive lug of one

cell on to the negative of the next; this insures a uniform and permanent joint, unaffected by acid spray.

Where lead burning is not practicable the lugs are generally clamped together by an iron bolt and nut, protected by a lead covering. Iron is rapidly attacked by acid when exposed to the air and in contact with another metal such as lead, with which it forms a galvanic couple. of connector.



F.IG. 77.—Lead-covered bolt and nut.

Figure 77 illustrates one form

The condition of a cell being indicated by the density of its electrolyte, two or three hydrometers should form part of the equipment of every battery.

Application of Storage Batteries.—Storage batteries have been applied to nearly every branch of Electrical Engineering, but are particularly adapted for electric-lighting stations. During light load the dynamos may be shut down and the load supplied from the battery; the latter also acts as a stand-by when the generating plant has to be shut down for a short period of time. Batteries are also very serviceable for electric

traction work. They are connected in parallel with the mains, and assist the generators during periods of heavy load, and are charged during periods of light load.

As an instance of the application of a storage battery, consider the case where it is used for storing energy obtained from a dynamo and, as required, supplies current at constant potential to a load of lamps. The arrangement of the dynamo D, battery B, and lamps L is shown diagrammatically in Figure 78. It

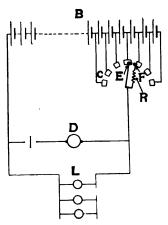


FIG. 78.—Battery, dynamo, and lamps.

may be inconvenient to have the dynamo working during the evening when the current is required, so that the battery has to be charged during day. As the battery the discharges the E.M.F. falls, that to maintain the pressure across the lamps constant a number of end cells must be used for controlling the voltage. This is best illustrated by a concrete case.

Example.—A battery has a discharging E.M.F. of 2.05 volts per cell at start,

and gradually falls to 1.85 volts at end of discharge. If the internal resistance of each cell is 0.0005 ohm, and the resistance of the leads from the cells to the lamps 0.011 ohm, what number of cells must be used (1) at commencement and (2) at end of discharge if they supply current to 500 60-watt 220-volt lamps?

Current taken by the lamps =  $C = \frac{500 \times 60}{220} = 136$  ampères.

Terminal E.M.F. of each cell = E.M.F. on open circuit –  $C_r$ , where r = resistance of each cell.

Volts drop in leads =  $0.011 \times 136 = 1.5$  volts.

Therefore the battery has to supply current at pressure of 220 + 1.5 = 221.5 volts.

.: No. of cells

$$= \frac{221.5}{\text{terminal E.M.F. of each cell'}}$$
Cells at commencement of discharge = 
$$\frac{221.5}{2.05 - Cr}$$

$$= \frac{221.5}{2.05 - 136 \times 0.0005} = 115 \text{ cells.}$$
And cells at end of discharge

And cells at end of discharge

$$= \frac{221.5}{1.85 - 136 \times 0.0005} = 128 \text{ cells.}$$

The number of end regulating cells must equal 128-115=13.

At commencement of discharge 115 cells give the requisite voltage. As the discharge proceeds the regulating cells are switched into circuit, one by one, by means of the regulating switch, and at the end of discharge the 13 regulating cells are in circuit.

The end regulating cells never become completely discharged, as they are only in service during a portion of the time that the battery is discharging. When the battery is being charged the end cells are placed in circuit at the commencement, and gradually cut out of circuit as each becomes charged.

A battery regulating switch requires to be of special design, so that the voltage may be controlled without interrupting the current flowing from the battery, or short-circuiting any one cell. The end cells are connected to the switch studs C, over which the movable contact arm passes. The latter consists of two pieces E and F, connected with each other through the resistance R. When passing from one stud to the next, before the contact E leaves the first stud the contact F has come on to the next stud, thus preventing an interruption of the current. For the instant that E and F are on different studs, the cell between them would be short-circuited, but by the introduction of the resistance R, the short-circuit current is limited to the normal discharge of the cell.

Example.—In the previous example what must be the E.M.F. of a dynamo to charge the above cells at

200 ampères? Each cell has an E.M.F. of 2.4 volts when fully charged. The resistance of the leads from the dynamo to the battery is 0.03 ohm.

Maximum charging E.M.F. for each cell

$$r = 2.4 + Cr = 2.4 + (200 \times 0.0005)$$
  
= 2.5 volts.

Suppose that near the end of charge only 5 regulating cells are in circuit, then the total E.M.F. required to charge the battery

$$= 120 \times 2.5 = 300.$$

Now the drop in leads =  $0.03 \times 200 = 6$  volts. Therefore the dynamo must generate 306 volts.

#### CHAPTER VI

## ELECTRIC LIGHTING

## INCANDESCENT LAMPS

The incandescent or glow lamp is an application of the principle that when an electric current flows through a conductor the latter becomes heated, and the quantity of heat generated in calories is given by C<sup>2</sup>R×0.24. The energy radiated from a hot body consists of trains of waves of different lengths. The sensation of light is caused by those whose lengths lie between 40 and 80 millionths of a centimetre.

By Guillaume's law the light varies as the twelfth power of the absolute temperature of the source. This being known, attempts were made to find a conductor which could be raised to a high temperature without fusion. It is also necessary that the conductor should have a high specific resistance and be conveniently shaped, so as to provide small units of light.

From 1850 to 1890 many substances were experimented with, but carbon—specially prepared—seemed to be the only material possible. Within recent years experiments have been carried out on some of the more refractory metals, with the result that tantalum, osmium, and tungsten can now be formed into filaments for incandescent lamps; in fact, the carbon filament lamp may, within a few years, become extinct, due to the superiority of the above refractory metals.

Optical Efficiency.—Any source of illumination is simply a transformer of energy, and the vibratory motion of the ether, which is produced, requires for its support

an expenditure of energy. In oil or gas lamps the energy is taken from the combustible: in an electric lamp it is furnished by the current. The transformation of this energy, in each case, is accompanied by losses which depend upon the radiant employed. Each source of light has an efficiency which indicates what fraction of the total energy expended is capable of producing a luminous impression.

Optical efficiency is the ratio of the energy reappearing in the form of luminous rays to the total energy

supplied, and is given by

optical efficiency =  $\frac{\text{useful energy developed}}{\text{total energy absorbed}}$ .

The optical efficiency of an artificial source of light is low. When the temperature of the source is below 400° C., the vibrations in the ether are not rapid enough to be sensible to the eye as light, in which case the

optical efficiency is zero.

The total luminous energy radiated by a glow lamp can be estimated in the following manner, as suggested by Tyndall. The lamp is placed in the water of a blackened metal calorimeter, and the increase in temperature of the water after a certain time is noted. The lamp is then transferred to a clear glass calorimeter, in which the increase of temperature will be due only to the obscure heat rays. The difference between the amount of heat given to the water by each of these methods is a measure of the luminous energy given out by the lamp.

By this method the optical efficiency of carbon filament lamps is found to be about 5 per cent.; that is, 95 per cent. of the electrical energy supplied to the lamp is merely transformed into heat, and so far as the production of light is concerned this energy is lost. In order to effect a comparison with other sources of illumination, see Table V.

Commercial Efficiency.—For practical purposes, in stating the efficiency of a glow lamp, the light energy emitted is expressed in candle-power, and the electrical energy absorbed in watts: thus expressing the efficiency

TABLE V

Illum		Optical efficiency					
Gas burner						4 P	er cent.
Carbon filament lamp					- 1	5	,,
Metal ", "	•	•		•	•	12	**
Ordinary arc lamp"	•	•	•	•	•	15	"
Flame "		•			.	25	,,

by stating that the lamp develops a certain candlepower per watt absorbed. However, the more usual method of expressing efficiency is in watts per candlepower, which, correctly speaking, is the inefficiency. This is known as the commercial efficiency and is simply referred to as "the efficiency."

Commercial efficiency

 $= \frac{\text{power absorbed in watts}}{\text{illuminating power in candles}} = \frac{W}{C.P}.$ 

= watts per candle (W.C.P.).

For instance, a lamp taking 0.3 ampère at 200 volts, and giving an illumination of 16 candle-power, has an efficiency of  $\frac{0.3 \times 200}{16} = 3.75$  watts per candle. This is about the average efficiency of a good carbon filament lamp, and as the optical efficiency is only 5 per cent., about 3.6 watts produce heat and the remainder light.

Polar Curves of Illumination.—No lamp gives a complete uniformity of light distribution, the intensity of light being greater in certain directions than in others. Figure 82 is a curve showing the distribution of light about the vertical plane of a carbon filament lamp: this is known as a polar curve of illumination.

To obtain the polar curve of a lamp the candlepower at a given distance is measured in different directions, and in what follows it is assumed that the radiation in any angular direction round the vertical axis of the lamp is fairly uniform. If this cannot be assumed then the illumination must be measured by rotating the lamp at a speed of three or four revolutions

per second in each new angle with the vertical.

In testing a lamp it should be arranged that it can be rotated about a vertical axis in steps of 10° at a time. The intensity of light in each direction is then measured in a manner described on pages 191 to 193.

Referring to Figure 79, let L indicate the position of the lamp, which is rotated about the axis AB

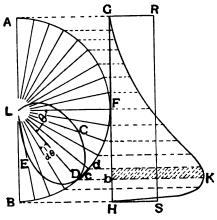


FIG. 79.—Rousseau's construction.

in equal steps of 10 degrees, shown by the respective radii. Marking off each radius a length proportional to candle-power in direction, the curve LCDE drawn through these points is half the polar curve, and in general both halves of these curves similar.

Mean Spherical Candle-Power of a

Lamp.—By the mean spherical candle-power of a lamp is meant that candle-power, uniform in all directions, which would give the same total illumination as that from the lamp in question. Considering the light to fall on the surface of a sphere with the lamp at its centre, the total illumination will be the sum of each unit area multiplied by the intensity of light over that area, i.e. the total illumination is given by  $\Sigma$  (IA). If  $I_m = \text{mean}$  intensity of illumination, then  $4\pi r^2 I_m = \Sigma$  (IA), r being the radius of the sphere. Denoting the mean spherical candle-power by  $P_m$ ,  $P_m/r^2 = I_m$ , and  $4\pi P_m = \text{total}$  illumination over the sphere.

If the distribution of light given by a polar curve is known, then the mean spherical candle-power of a lamp can be deduced from the following construction

due to Rousseau.

In Figure 79, let ADB be a semi-circle, which by revolution round the diameter AB sweeps out a sphere. Through F is drawn GH, parallel and equal to AB. Set off from b, and perpendicular to GH, is the line bK, proportional to the candle-power of the lamp, in the direction LD. Carrying out the same construction for a number of different observed candle-power readings at known angles above and below the horizontal plane, the curve GKH drawn through all the points, such as K, will be described.

Suppose the candle-power to be uniform in a circle of radius r round the lamp, then in any zone of width  $cd = rd\theta$ , the illumination

= LD x area of zone

 $= LD \times 2\pi r \cos\theta r d\theta$ 

 $= I \times 2\pi r^2 \cos\theta \ d\theta$ 

and the total spherical illumination

$$= \int_{-\frac{\pi}{2}}^{+\frac{\pi}{2}} I \times 2\pi r^2 \cos \theta \cdot d\theta,$$

 $\theta$  being the angle FLD.

This may be calculated for each radius at different angles, but can also be determined graphically, for  $rd\theta$ .  $\cos\theta$  = projection of element cd on the vertical, and the shaded area = I  $rd\theta$   $\cos\theta$ .

Constructing for other elements, the area of curve GJH

$$= \int_{-\frac{\pi}{2}}^{+\frac{\pi}{2}} I\cos\theta \cdot rd\theta.$$

The rectangle GRSK is drawn so that its area =

area of GJH. Then  $HS_{2r} = \int_{-\pi}^{+\frac{\pi}{2}} I\cos\theta \ rd\theta$ 

$$2\pi r^2$$
.  $2HS = \int_{-\frac{\pi}{2}}^{+\frac{\pi}{2}} I\cos\theta \cdot d\theta \cdot 2\pi r^2$ ,

that is,  $4\pi r^2 HS = \text{total spherical illumination}$ therefore HS = mean spherical candle-power.

#### CARBON FILAMENT LAMP

Carbon is a non-metallic substance which cannot by any ordinary means be melted or volatilised. It oxidises readily when heated in an atmosphere containing oxygen, hence the air must be exhausted from the glass bulb containing the filament. The carbon forming the filament of glow lamps has a specific resistance of 0.004 of an ohm per centimetre cube, and a negative temperature coefficient = 0.00054 per degree centigrade.

Carbon used for glow lamps is specially prepared from organic substances, such as cotton wool or wood fibre. This raw material is dissolved in chloride of zinc, and the syrup so formed is purified and run into jets proportioned to the diameter of filament required. After the material has set, the threads are formed to the required shape and carbonised by placing in crucibles packed with graphite and raising the temperature to about 2000° C. This great heat is necessary in order (1) to make the carbon hard and durable, (2) to increase its conductivity, and (3) to reduce its acclusion or power to retain gases. At this stage the filaments are reduced from their previous state of high and irregular resistance to

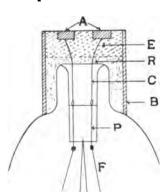


Fig. 80.—Carbon filament glow lamp.

one in which their resistance is low but uniform. The process consists of electrically the filaments in heating hydro-carbon gas or liquid to such a temperature that the latter is decomposed into its elements hydrogen and carbon, the latter being deposited in a solid form on the surfaces of the white-hot filament. latter process is known "flashing."

In mounting the filaments connection is made to them

by means of platinum wires P fused into the glass, as indicated in Figure 80. Platinum is used because it is the only conductor having the same coefficient of

thermal expansion as glass, and hence the latter does not fracture on cooling. The cap consists of an insulated brass collar B fixed on with plaster of Paris R, and the filament F is connected by means of the platinum P and copper wire C to two contact plates A embedded in the cement E.

Relation between Voltage, Candle-Power, and Efficiency of Carbon Filament Lamps.—The efficiency of an incandescent lamp depends upon the temperature

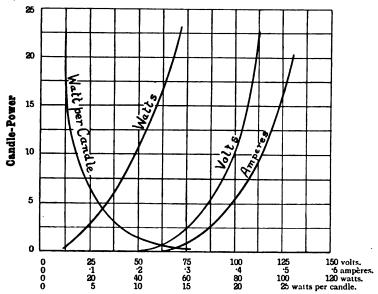


FIG 81.—Candle-power and efficiency curves of a carbon filament lamp.

of the filament, and since the radiant light is proportional to the twelfth power of the absolute temperature, the greater the latter the higher must be the efficiency.

In Figure 81 are a series of curves obtained from a 105-volt 16-candle-power lamp having a normal efficiency of 3 watts per candle. The candle-power was measured in a horizontal plane, and is plotted as a function of—(1) the voltage across the lamp terminals, (2) the current flowing through the lamp, (3) the watts absorbed, and (4) the efficiency in watts per candle. The curves are characteristic of all carbon filament lamps,

and show that the candle-power increases much more

rapidly than either the amperes, volts, or watts.

From the voltage curve it will be seen that an increase in pressure of 5 per cent. above normal increases the candle-power by 30 per cent., or expressing this mathematically, C.P. & E6. The candle-power varies as the third power of the watts, i.e. C.P. ∝ W³.

A large increase in the efficiency and candle-power is obtained by increasing the voltage by a few per cent. above the normal, and a thoughtful student will ask: "Why is a lamp worked at a particular efficiency and

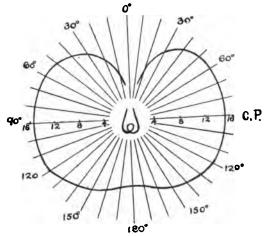


FIG. 82.—Polar curve for a carbon filament lamp.

not at the maximum?" This is fully explained on page 156, but before dealing with it the theory of the incandescent glow lamp must be further examined.

In Figure 82 is given the polar curve for a carbon filament lamp, from which it will be observed that the intensity of light is greater in a horizontal plane than directly below the lamp. The filament was of the form indicated in the figure.

Life of Carbon Filament Lamps.—An incandescent lamp, besides having a filament which will remain unfractured for a considerable period, must also remain near to its rated candle-power and efficiency, as the most economical lamps are those which give the maximum candle-power-hours for the minimum operating cost.

In Figure 83 curves are plotted for 16-c.p. 230-volt lamps, showing the variation in candle-power and efficiency with their life. The curves are the mean of a series of tests performed on a number of lamps run at their normal pressure, the candle-power and watts absorbed being measured at intervals. These curves are typical of a good carbon lamp. It will be observed that the candle-power and efficiency increase during the first 60 hours, and then gradually diminish in a

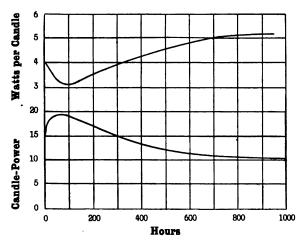


FIG. 83.—Variation in candle-power and efficiency of a carbon filament lamp.

manner shown by the curves. This increase in the efficiency of a new lamp is probably due to either a better vacuum being obtained or a change in the structure of the filament, which reduces its resistance and allows a larger current to pass through it.

The chief causes which lower the candle-power are (1) Alteration in the character of the surface of the filament, and (2) blackening of the bulb.

Of these, the greater effect results from the first cause, it having been shown that with a well-made lamp the deterioration in 1000 hours, owing to the blackening of the bulb, does not amount to more than

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10 per cent. of the total deterioration. The deterioration by change in the character of the surface of the filament is caused by some of the carbon volatilising, and leaving the surface of the filament an aggregation of fine particles of carbon with many elevations and depressions. There will be therefore an increased radiating surface, and consequently the temperature of the filament will be lower for the same consumption of energy. The volatilised carbon which leaves the filament, besides increasing the surface, also reduces the mean area of cross-section, thereby increasing the resistance of the filament, and decreasing the current and illuminating power.

The cause of the blackening of the bulb will now The volatilised carbon condenses on the comparatively cold glass, and as the life of the lamp increases the inner surface of the bulb becomes coated with a thin layer of carbon, which absorbs some of the radiant light rays. Experience shows that the efficiency and candle-power of lamps which have either (1) their filaments carbonised at a very low temperature, or (2) inferior vacuums, decrease very rapidly during their

The greater the temperature of the filament the more rapidly does this disintegration take place, and as a very high efficiency lamp means a high temperature of filament, high efficiency lamps will last a much shorter time than low efficiency ones. The useful life of a lamp is considered to be limited to the period in which the original candle-power has not diminished by more than 20 per cent. That the above is the case is confirmed by the figures in Table VI., showing the effect of overand under-running 200-volt 16-c.p. lamps.

The average life of a carbon filament lamp, having a normal efficiency of 3.5 watts per candle at the start, is between 800 and 1200, while a very high efficiency

lamp may only last 200 or 300 hours.

The life of a lamp is greatly reduced if it be supplied with current at varying pressures, the lamp then becomes blackened much sooner than would be the case if the pressure remained constant. This is obvious

Volts. Candle-power. Watts. Life in Hours. 184 9.0 4000 53.2 188 10.2 56.2 3100 2250 192 12.0 59.3 196 14.0 1440 200 16.0 800 18.0 530 20.2 360 212 23.0 230 26.0

TABLE VI

from the above table, for when the voltage increases, the temperature of the filament also increases, and probably during a considerable period of its life the lamp may have been run above its normal.

# METALLIC FILAMENT LAMPS

It has long been known that certain metals could withstand much higher temperatures than carbon, but the more refractory metals are very brittle at ordinary temperatures, and the difficulty experienced in forming these metals into fine wires prevented them being tried as lamp filaments. Means have now been devised for working some of the refractory metals into fine wires having a diameter of 0.05 millimetre, so that glow lamps are now made on a commercial scale having tantalum and osmium filaments.

Tantalum Lamps. — Tantalum is an exceedingly hard metal, and in a pure state is ductile. When cold it is unaffected by chemical reagents, and is attacked solely by hydrofluoric acid. The tantalum is melted in an electric furnace; the ingots are raised in temperature to a red heat, then hammered into sheets, and finally drawn into wires. From a low red heat upwards it has a great affinity for hydrogen and nitrogen, and with these it forms combinations of a metallic appearance. This latter property renders necessary the placing of a tantalum filament in a vacuum. Tantalum

has a specific resistance of 16.5 microhms per centimetre cube, which is considerably less than carbon. The temperature coefficient is positive and has a value of

0.234 per cent. per degree Centigrade.

The tantalum from which the filaments are made is purified by chemical processes, and the gases contained in it are driven off by heating in a vacuum. Filaments having a diameter of 0.05 millimetre require a length of 650 millimetres for a 25-c.p. 110-volt lamp, so that special means are adopted to fix a filament of such length in the ordinary glass bulb. The low specific resistance of tantalum makes it unsuitable for high-voltage lamps, owing to the great length of filament required.

Efficiency and Candle-Power of a Tantalum Lamp.—The candle-power of a tantalum lamp is proportional to E<sup>4,4</sup>, and since the filament can be run at a very high temperature the efficiency is much higher than that of the ordinary carbon lamp, being of the order

of 1.7 to 2 watts per candle.

Tantalum having a positive temperature coefficient, these lamps will give better regulation than a carbon filament lamp, and their life is probably less affected by voltage variations. The maximum light is emitted at an angle of 85 degrees with the vertical, and is much less in a vertical plane below the lamp: the distribution of light in a horizontal plane is on an average a circle.

Life of Tantalum Lamps.—In Figure 84 are two curves, showing how the efficiency and candle-power of tantalum lamps vary with their life. The test from which these curves were obtained was on some 22-c.p. 110-volt lamps, and they indicate the general behaviour

of this type of lamp.

During the first few hours of their life tantalum lamps, like most carbon ones, increase in candle-power and efficiency, the latter increasing from 15 to 20 per cent., while the power consumption drops from 1.4 watts to 1.3 watts per candle. After reaching this maximum, the candle-power gradually decreases, while a corresponding decrease in the efficiency occurs. The initial increase of illuminating power and decrease in the

power consumption is probably brought about by a change in the structure of the filament, this being accom-

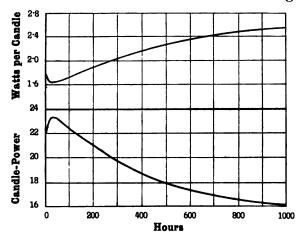


FIG. 84.—Variation in candle-power and efficiency of a tantalum lamp.

panied by a reduction in resistance and the phenomena resulting therefrom.

The useful life of this lamp averages between 600

and 800 hours when commencing with an initial efficiency of 1.7 watts per candle. Some specimens have had a useful life of as long as 1100 hours, but this is an exceedingly rare occurrence, in fact under normal working conditions the absolute life seldom exceeds 1000 hours.

Experience shows that the tantalum lamp blackens but little, unless it has been strongly overheated in consequence of a partial short circuit.

When a lamp has been in use for some time the structure of the filament becomes Fig. 85.-Apcompletely changed. A new filament is smooth and polished, but after some use assumes an irregular form, and at the end of its life is remarkably disjointed, as indi-

pearance of tantalum filament being in use for 600 hours.

cated in Figure 85. This change is more marked if the lamp be used on an alternating current circuit; in

fact an alternating current, due to some cause yet to be explained, is so detrimental to the life of a tantalum lamp, that the latter never exceeds 200 or 250 hours.

After being in use for 200 or 300 hours the tantalum filament loses a large amount of its mechanical strength and becomes exceedingly brittle. It is therefore advisable when lamps have been in use for some time not to remove them from their fittings, as this might easily cause the filament to fracture.

A feature which marks tantalum lamps is the ability of the filaments sometimes to repair themselves after having been broken. If the broken ends of the filament come into contact with another portion of the filament so that the circuit is completed, the lamp once more lights up. A junction of this sort may result in a very strong weld, so that it does not necessarily constitute a point of weakness. After a repair of this sort, in which a part of the filament has been cut out, the lamp glows more intensely and even too intensely, so that only a small span of life may be left for it. These occurrences of breakages and repairs account for irregularities in the life of tantalum lamps.

The behaviour of a tantalum lamp under increased pressure shows its superiority over the carbon lamp. It has been ascertained that tantalum lamps giving 25-c.p. at 110 volts and 1.7 watts per candle, only burn out when the pressure reaches about 250 volts by gradual increase. A carbon lamp designed to work under the same conditions could not withstand anything approaching this pressure.

Tantalum lamps are made for pressures of from 50 to 125 volts, so that where the current is supplied at 230 or 250 volts two lamps must be run in series. This is rather inconvenient for lighting small rooms, where one lamp might be sufficient, but for the lighting of large rooms, halls, and business premises, tantalum lamps are more economical than carbon ones.

The light is white in colour, and as the area of illumination is large the distribution is good.

Osmium Lamps.—Osmium is the most refractory metal known, and is too hard to be drawn into a wire,

so that in the preparation of the filaments a paste is formed by mixing the osmium with organic materials. The paste is squeezed through dies so that it may assume cylindrical form, and when the foreign material has been expelled by heating, there remains a porous bright filament. When cold the osmium filament is brittle, but becomes soft during incandescence, so that it requires to be well supported.

As with tantalum, osmium has a low specific resistance; these lamps are only made, therefore, for voltages not greater than 130, in which case the filament consists of four or five loops in series, each being anchored at its

lower end.

The filament of an osmium 37-volt 22-c.p. lamp has a diameter of 0.087 millimetre and a length of 280 millimetres.

These lamps give a white light and have an efficiency of 1.5 watts per candle. With a 10 per cent. increase in volts above the normal the current increases 6.5 per cent. and the illumination by 40 per cent., as compared with an increase of 12 and 80 per cent. respectively in the case of a carbon filament lamp.

It is not possible to state definitely the life of an osmium lamp, but 1500 hours have been repeatedly exceeded. The surface of the filament is at first somewhat rough, but gradually becomes smoother, thus causing the candle-power and efficiency to increase during the first 250 hours or so. It is claimed that the bulb of these lamps does not blacken under normal conditions.

At present they are expensive in prime cost, and this, coupled with the fact that they are only made for low voltages, makes their commercial use limited.

# NERNST LAMPS

The main principles of this lamp were discovered by Jablochkoff in 1877. He found that oxides of rare earths which are non-conductors when cold, became conductors when raised to a certain temperature. Jablochkoff suggested a method of first heating the filament or rod by covering it with a thin layer of carbon, through which a current was passed. layer became hot, thus increasing the conductivity of the filament sufficiently to make it a conductor.

Professor Nernst along with others continued the research, and in 1897 produced the lamp bearing his name.

The filament of the Nernst lamp is generally a mixture of one or more of the oxides of zirconium, thorium, and cerium made in the form of little rods or spirals. Such substances as these become conductors

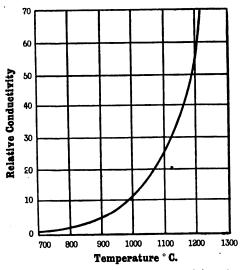


Fig. 86.—Variation in conductivity of a Nernst lamp filament.

become incandescent.

raised when temperature of about 700° C., and for this purpose a heating coil is connected in parallel with the fila-This heater ment. consists of a platinum wire having a high resistance. and wound in a spiral over the filament. When this arrangement is connected to supply circuit current flows through spiral, and the heat generated radiates out and raises

the temperature of the filament. On becoming a conductor current flows through the filament, causing it to

This lamp differs from the lamps already discussed, in that the filament does not require to be placed in a The curve in Figure 86 indicates how the conductivity of the filament varies with the temperature, the conductivity at 700° C. being taken as unity. At 900° C. the filament becomes incandescent. The rapid increase in conductivity with temperature would cause the illumination to be very unstable when the supply pressure varied within a few per cent. To reduce the effect of voltage variation a steadying resistance of fine iron wire, having a value between 9 and 15 per cent. of that of the whole lamp, is put in series with the filament. The resistance is so designed that it is at a red heat when the filament is incandescent, and any variation in the conductivity of the latter is balanced by the alteration in resistance of the iron wire, as any increase in the current through the filament increases the resistance of the iron wire.

Figure 87 is a sectional diagram of a lamp in which the

filament is placed horizontal. The filament F and heater H, carried by a porcelain collar P, are connected at one end E to a socket D, the other ends being connected to C and B respectively. The heater is painted with cement to protect it from the intense heat of the filament. nection is made to the top portion of the lamp through the thin split rods S carried by a hollow porcelain box K. The split rods fit into the sockets B, C, and D. Two of the rods carry contact guide skates, which make connection with the steadying resistance R; the latter is placed in an exhausted glass tube to prevent the iron from becoming oxidised. The porcelain box K contains a small electro-magnet M, having an arma-The exciting coil of this magnet carries the current flowing through the filament, the coil M,

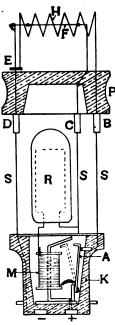


FIG. 87.—Nernst lamp.

resistance R, and the filament F being in series, and connected to the two contact blocks marked + and -.

The current enters by the + terminal, and from this point there are two paths, one through the coil M, resistance R, and filament F, but as the latter is cold no current in the first instance will flow through this circuit; the second path is completed through the armature A and heater H. On the passage of the current the heater glows dull red, and the temperature

of F at the same time rises. After an interval of from 30 to 60 seconds the filament reaches the critical temperature and becomes a conductor, so that current flows through it and causes it to become incandescent. On the current flowing through the coil M the armature A is attracted and breaks the heater circuit. The heater, if always retained in the circuit, would absorb a considerable amount of energy and thus lower the efficiency. In the diagram, A is in the position occupied when no current flows through the filament; the position when a circuit is completed through the latter is indicated by the dotted lines.

When supplied with direct current electrolytic action apparently takes place, oxygen appearing at the anode end while the filament undergoes reduction at the cathode end. These lamps must therefore have their respective terminals connected to the proper supply main. The filament is made tapered, and after burning for some time electrolytic action causes it to assume cylindrical form, after which thinning occurs at the end that was previously the thicker, and the process goes on until the filament breaks. Should the terminals be wrongly connected, the thin end is further diminished and breaks prematurely.

Efficiency and Life of Nernst Lamps.—The filaments of these lamps are worked at a very high temperature—about 2500° C.—the efficiency should therefore be high. At this high temperature, however, the filament is so dazzling that the light requires to be subdued by coloured globes, and this greatly reduces the efficiency, which

varies between 2 and 3 watts per candle.

In Figure 88 are two curves which show the variation of candle-power and efficiency with the life. The test was performed with 10 horizontal filament 110-volt lamps. They were equipped with opal-glass globes, and the photometric measurements were made in the vertical axis of the lamp. It will be seen that the candle-power diminishes rapidly during the first 50 hours, and then remains practically constant at about 11 candle-power for the next 500 hours; after 500 hours the candle-power rapidly falls. These curves are characteristic of lamps of this type.

The normal candle-power and efficiency of a Nernst lamp is that which it assumes at the end of 50 or 60 hours, and from the curve it will be observed that the normal efficiency is about 2.7 watts per candle. The average life of the 10 lamps tested was about 500 hours,

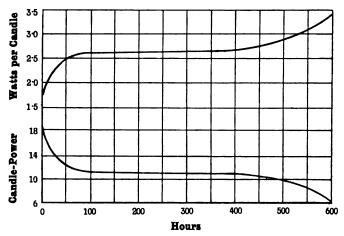


FIG. 88.—Variation of candle-power and efficiency of a Nernst lamp.

although the author has found that they are very unreliable, and that their life, on the whole, seldom exceeds 400 hours.

Premature failure and high initial cost give the present form of Nernst lamp very little advantage over the ordinary carbon filament lamp.

# THE MOST ECONOMIC EFFICIENCY

Assuming the supply voltage to remain steady to within, say, 2 per cent., it has been shown that lamps having a high efficiency have a short life compared with low efficiency ones; consequently it has to be decided whether it is more economical to use high efficiency lamps and more of them, or low efficiency ones and a smaller cost of renewals.

Owing to the varying cost of electrical energy and variations in the useful life of different lamps, there is a best efficiency at which to run a lamp in order to obtain

the maximum economy, *i.e.* the minimum operating expenses. When energy is cheap and lamps expensive, the efficiency should be low; but when the reverse is the case high efficiency lamps should be used. In practice the total operating expenses are generally near a minimum when the cost of lamp renewals is about 15 per cent. of the whole.

To determine the best efficiency for a lamp to work on a particular circuit, the following must be known: (1) The cost of a new lamp, (2) the average life of the type of lamp when run at various efficiencies, and (3) the cost of electrical energy. (1) and (3) are readily obtained, but a knowledge of (2) entails carrying out life tests on samples of the lamps under consideration. This information, however, in some cases can be given by the makers of the lamps.

Example.—If a particular 16-c.p. lamp costs 1s. 4d. and its life varies with the efficiency as in Table VII., find the most economical lamp to use, assuming electrical energy to cost 4d per unit.

Cost in Pence per 100 Hours. Lamp Life Efficiency. in Hours. Total Lamp Energy. Operating Cost. Renewals. 4.5 W.C.P. 0.38 pence 4200 29.0 29.4 2000 0.80 25.6 26.4 4.0 " ,, 22.4 1200 3.5 " " 3.0 600 2.65 19.2 21.85 ,, 2.5 310 5.15 16.0 21.15 ,,

TABLE VII

The cost in pence for (1) lamp renewals and (2) energy during some period of time, say 100 hours, must first be determined.

(1) Lamp renewals per 100 hours for a 4.5 watt per candle lamp cost  $\frac{16 \times 100}{4200} = 0.38$  pence. Similarly, the

cost of renewals at other efficiencies can be calculated, and are given in the third column of the table. In Figure 89 the cost of lamp renewals per 100 hours is plotted as a function of the watts per candle and curve A is obtained.

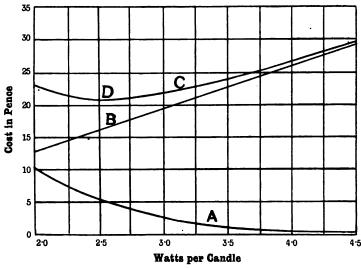


FIG. 89.

(2) Energy. In calculating the cost of energy per 100 hours for each particular lamp, let CP = candle-power of the lamp, W = watts per candle, and P = the cost in pence for 1 Board of Trade unit; then the units used by each  $lamp = \frac{CP \times W \times 100}{1000}$ . The cost of energy for that period per lamp is therefore

$$\frac{CP \times W \times P \times 100}{1000} = \frac{16.4 \times 4 \times 10 \times W}{1000} = 6.4W.$$

The values are given in the fourth column, and when plotted in the figure give the straight line B. Adding the ordinates of the two curves, a third curve C is obtained, which gives the total cost in pence to run the lamps for 100 hours. Their individual values are given in the last column of the table. It will be observed that in the curve C there is a minimum D, which gives the

minimum operating cost per 100 hours. So that when energy costs 4d per unit, the most economic efficiency is obtained by using a lamp having an efficiency of 2.5 watts per candle.

#### ARC LAMPS

It is well known that when a circuit, through which a current passes, is broken the current does not immediately die down, but has a tendency to continue to flow by bridging across the gap thus formed. The existence of the current is evidenced by a flame or arc set up between the points at which the circuit was broken. The electric arc is based upon this phenomenon, and was first demonstrated by Davy before the Royal Institution, London, in 1808. He employed two carbon rods, and connected them to a 2000 volt supply provided by a battery of galvanic cells. On bringing the two carbons together a current passed from the battery through the carbons, and on being separated a luminous bridging arc appeared between them.

When two carbon rods—commonly called electrodes—are brought together heat is generated at the tips, and they begin to glow, due to the high resistance offered at the point of contact between the carbons. On the electrodes being pulled a few millimetres apart an arc is formed by the carbon vapour which is evolved from them on becoming heated; this conducts the current across the intervening air-gap. An E.M.F. of between 40 and 50 volts is required across the electrodes, for reasons which are explained later.

If the arc be allowed to burn for a few minutes the distance between the electrodes will increase, due to the volatilisation of the carbon. The length of the arc will go on increasing until the resistance becomes too great for the available E.M.F. to overcome; the arc will then be extinguished.

From the above it will be evident that in a commercial arc lamp the electrodes must be attached to some mechanism which will cause them to come together and strike the arc when the current is switched on, and also feed the carbons towards each other as they burn away, and so maintain the distance between them constant.

Form of Electrodes. — Since the temperature of volatilisation of a substance determines the intensity of light emitted, the electrodes of an arc lamp must be made of a material which has a high temperature of volatilisation. Carbon is invariably used, though in some cases it is mixed with chemicals, such as sodium, in order to increase the intrinsic brilliancy of the arc. Carbon volatilises at a very high temperature, but if foreign materials are present in the electrodes the temperature of volatilisation will be lowered, and with it the intensity of the light, for a given consumption of power, will be correspondingly reduced. Arc lamp carbons must therefore be of the purest, and formed into rods having a uniform sectional area and density.

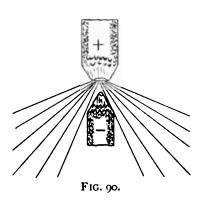
Types of Arcs.—Of these there are two. The first type includes those in which the carbons are placed coaxially, as shown in Figure 90, and if the arc be supplied with direct current the positive carbon, i.e. the one by which the current enters the arc, is placed uppermost. This type will herein be referred to as the Ordinary Arc. The second type is known as the Flame Arc, and has its carbons placed at an angle of about 30 degrees with each other, as shown in Figure 98.

# ORDINARY ARC LAMPS

It is essential in the first instance that the carbons touch each other, otherwise a large E.M.F. would be required to start an arc between them. When the arc is struck the intense heat produces volatilisation, and a vapour fills the space between the two carbon tips, which so reduces the resistance that the electric circuit made at the instant of contact is maintained. The current, once started, very quickly increases the amount of carbon vapour formed, and so raises the temperature and luminosity of the arc to a value depending upon the current flowing.

The carbons burn slowly away, the positive twice as

fast as the negative, and after burning for some time they assume the appearance shown in Figure 90. The positive has its end hollowed into a cup-shaped form, which becomes incandescent, and is known as the crater. The negative carbon assumes a pointed shape, the tip of which also becomes incandescent, and small nodules of molten



impurities solidify on the part just outside the light-giving area. The stream of carbon vapour forming the arc has a light violet colour, and is surrounded by a faint green.

The area of the white spot on the tip of the negative carbon increases with the current, but at a much slower rate than the area of the crater; so that the

ratio of crater area to the area of white spot on the

negative increases rapidly with the current.

Illumination from an Arc with coaxially-placed Carbons.—The amount of light given out depends upon the temperature to which each particular part is raised. On examining an arc it will be found that all parts are not equally bright, but show at least four distinct parts. The temperature of the crater is supposed to be about 4000° C., while the temperature of the negative tip is about 2000° C. The crater is the brightest part of the arc, and gives 85 per cent. of the total illumination; the tip of the negative carbon gives about 5 per cent., and the remainder is given by the arc and the gaseous vapour round it, the arc itself supplying but a small fraction of the total light.

The crater of the positive carbon will be most usefully employed when placed above the negative carbon, as shown in Figure 90, so that as many light rays as possible may radiate downwards. An inherent defect of coaxially-placed carbons is that the negative obstructs a large proportion of the light emitted from the crater. For this reason it is usual to employ carbons for the

negative electrodes of as small a sectional area as the current density permits.

Owing to the obstruction of the light from the crater by the negative carbon the illumination of the area below the lamp is not uniform, but is distributed as indicated in the figure; the maximum illumination being at an angle of 45 or 50 degrees to the axis of the carbons.

Figure 91 represents half the polar curve obtained

from an arc plied with direct cur-The direction maximum will tensity vary according the to relative sizes of the two carbons and the shape of the crater. The illumination at any point underneath the arc is proportional to the area of crater visible at that

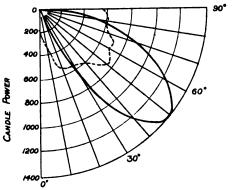


FIG. 91.—Polar curve of illumination for a direct-current arc.

from 140 to 170 candle-power per square millimetre of crater visible.

What has been said up to this applies only to arcs working on direct-current circuits, but alternating currents of frequency between 40 and 80 are equally applicable. Experience shows that arc lamps connected to alternatingcurrent circuits, having a frequency less than 40, do not work well, as the intensity of the light fluctuates greatly, due to the continual reversing of the direction of the The latter causes the carbons to be alternately current. positive and negative, and the distribution of light from an alternating-current arc will consequently differ from that produced by a direct current. In the former both carbons become cratered and distribute the same amount of light, so that the distribution will be as much above the This diminishes the illumination horizontal as below it. in a downward direction as compared with a direct-current arc absorbing the same power; consequently the illumination on a horizontal plane below the lamp is considerably reduced. In an alternating-current arc both carbons are of the same diameter, and are consumed at equal rates.

Behaviour of an Arc.—In a direct-current arc the positive carbon is volatilised at twice the rate of the negative, since the incandescent portion of the former is at double the temperature of that of the latter. With the positive carbon the highest temperature is at the centre, and to this is due the cup-shaped formation called the crater.

The current flowing through an arc tends to take the path of least resistance, or, in other words, if the carbons be of uniform section the arc will maintain itself in the shortest path between them: hence as the carbon is consumed at one point the resistance increases, and causes the arc to take up a new position; consequently the arc continually alters its location, and produces a varying distribution of light. Some method must be adopted to reduce this variation to a minimum by inducing the arc to remain in a position with its axis coincident with the axis of the carbons. In order to accomplish this the best positive electrodes are formed with a core of specially purified carbon, which tends to confine the gyrations of the arc within a much-restricted area. The cored part of the carbon is about 5 millimetres in diameter. A hole of this diameter is left in the carbon when being manufactured, and afterwards filled in under pressure with the lower-resistance carbon.

The sizes of the carbons vary with the current taken by the arc, and in Table VIII. is given the approximate sizes of the positive and negative carbons for different currents. In an alternating-current arc lamp both carbons have the same diameter, the diameter being the same as the negative carbon in a direct-current arc taking the same current. The length will vary according to the time the lamp is required to burn.

Relation between E.M.F., Current, and Length of Arc.—The relation between the P.D. of the carbons, the current, and the length of arc has been investigated by many observers, with the object of giving it a mathematical expression.

Current.	Diameter of cored positive Carbon.	Diameter of solid negative Carbon.  Millimetres.		
Ampères.	Millimetres.			
5	13	8		
6	14	9		
8	16	11		
10	18	12		
12	20	13		
15	20	13		

#### TABLE VIII

According to Frölich the E.M.F. between the two carbons consists of two parts and is expressed by the formula E = a + bl, in which a is a constant equal to about 39, b a function varying inversely as the current and having a value between 1 and 2, and l the length of the arc in millimetres.

Mrs. Ayrton has found that in a direct current arc between solid carbon rods the E.M.F. across the carbons is given by  $E = a + bl + \frac{c + dl}{C}$ .

If the E.M.F. be in volts, the current C in ampères, and the length l in millimetres, these constants have the following values: a = 38.9, b = 2.07, c = 11.7 and d = 10.5

Hence E = 
$$38.9 + 2.07l + \frac{11.7 + 10.5l}{C}$$
.

The constant a in the above equations is introduced probably by a counter E.M.F. set up between the carbon vapour forming the arc and the positive carbon, as experiment shows that there is a constant drop of this value between the positive carbon and a point in the arc very near to the former. This counter E.M.F. is quite independent of the length of arc and total E.M.F. required to maintain it.

Prof. S. P. Thompson suggested that this phenomenon might be due to the fact that electrical energy is expended in volatilising a certain portion of the positive carbon without changing the temperature, so that the vapour may be considered as having latent heat. This vapour is subsequently condensed on the negative carbon with the same quantity of latent heat, and in doing so the latter may be again transformed to electrical energy and set up a back E.M.F.

Hissing Arc.—As the current increases the area of the crater also increases, while the voltage diminishes; if this be continued until the crater extends to the sides of the carbon, then the voltage falls suddenly by about 10 volts and the current rises by 2 or 3 ampères. At the same time the arc begins to hiss, and in this hissing condition, if the current be further increased, the P.D. of the carbons remains constant over wide limits. Mrs. Ayrton\* has shown that the hissing is mainly due to the oxygen which gains access from the air to the crater, when the latter becomes so large as to overspread the ends of the positive carbon. According to Blondel, hissing takes place whenever the current density exceeds about 0.3 or 0.5 ampère per square millimetre of crater area.

Enclosed Arc.—The rate of combustion of matter varies with the quantity of oxygen present, the greater the latter the more rapidly does combustion take place. The carbons in an open arc burn at the rate of about 6 millimetres per hour, but this rate can be reduced to one-fifth by enclosing the arc in an almost air-tight globe.

At first completely air-tight globes were experimented with, but they quickly became obscure, due to the carbon vapour diffusing through the enclosed space and depositing on the cool sides of the glass. If, however, the arc be not completely enclosed it is then possible to admit air in such small quantities that the air oxidises the carbon vapour escaping from the arc and so prevents obscuration of the containing globe: provision must also be made for the escape of the heated and rarefied gases produced by combustion.

Since the arc is enclosed in a nearly air-tight globe, its length can be so increased as to allow it to be operated with double the pressure and half the current required for an open arc giving the same illumination.

<sup>\*</sup> Journal of Institution of Electrical Engineers, vol. xxvii. p. 200.

It would be impossible to operate a long, low-current arc in an open globe, because such an arc would be blown out by the least draught of air. Enclosed arc lamps are operated with pressures varying between 90 and 110 volts, the current absorbed being about 5 ampères.

The carbons when operated in this manner burn flat, thus modifying the distribution of light as compared with

an open arc.

The enclosing globe will necessarily absorb some of the light and so reduce the efficiency of the lamp, which is usually 60 per cent. that of an open type of arc. The reduced consumption of carbon is therefore obtained at the expense of the efficiency, but the former more than balances the latter.

Types of Arc Lamps with coaxially placed Carbons.—
The mechanism of an arc lamp is required to strike the arc when the current is switched on, and thereafter to maintain the distance between the two carbons constant. The latter operation may be performed either by causing one carbon only to move, the focus of the arc being thus constantly changed, or by causing the two carbons to move towards each other as they are consumed, thus keeping the focus of the arc in the same position.

Arc lamps are now generally controlled by electromagnets. The electro-magnets for this purpose consist of one or two solenoids, which when carrying a current, attract an iron core running through them. The strength of the pull thus effected depends upon the ampère-turns of the coil: this property of the solenoid, in conjunction with the electrical resistance of the arc, is made use of in

regulating arc lamps.

Two coils are employed, one being wound with many turns of fine wire and connected in parallel with the lamp terminals, the strength of this coil as a magnet depending upon the voltage across the arc. The second coil is connected in series with the arc, and is therefore wound with wire capable of carrying the main current. The two coils are connected in such a manner that their magnetic effects are opposite: this arrangement is referred to as a differential winding.

There are two methods of applying the above principle.

Figure 92 represents diagrammatically one form of differential arc lamp. The negative carbon A is fixed and the positive carbon B is free to move in a vertical direction, the latter being attached to an iron plunger P, which forms the core of the series and shunt coils. The series coil  $S_1$  is wound so as to attract the plunger

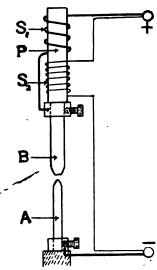


FIG. 92.—Principle of arc lamp.

against the force of gravity, while the shunt coil S<sub>2</sub> acts in the opposite direction.

Suppose the carbons are apart when the current is switched on, the shunt coil alone becomes energised and the plunger is pushed down, and with it the positive carbon, thus bringing the two carbons into contact. The current now flows through the series coil, and the pull overcomes that of the shunt winding so that the plunger and positive carbon are pulled up, thus striking the arc.

The normal resistance between the two carbons is such that the strength of the two coils equalises each other, and so

the iron core is kept floating between the two balanced attractions. As the carbons are consumed the length of the arc increases, thus increasing the resistance and so reducing the current in the series coil. When the current falls to a certain value the shunt coil prevails, resulting in a lowering of the plunger and carbon B until equilibrium is re-established.

A lamp working on this principle is illustrated in Figure 93. To the lower part of the plunger P is fixed a lever L, one end of which is slotted and supported by the pin C; the other end is attached to a piston moving in the dash-pot D. This serves to steady the controlling

mechanism. In the space S are wound the shunt and series coils, the former wound underneath the latter. The positive carbon is attached to the carbon holder H, which is kept in position by the guide tube T. The plunger P is tapered at its upper extremity so as to correspond to the shape of the pole-piece N, while the lower end is grooved in three places (only one shown in diagram) and each groove contains a clutch ring R<sub>1</sub>.

These rings are so fitted that when the plunger P is attracted up, they grip the carbon holder H and so raise the positive carbon. As the plunger descends the rings release their grip and allow the carbon holder to descend also.

The carbons of the lamp illustrated are enclosed in an inner globe G, which is airtight at all parts except at the bottom, where there is an airhole large enough to admit just sufficient air to maintain combustion. The positive carbon is guided into the inner globe G by means of three centring rings R, and the negative carbon is fixed to a frame F, which also supports the globe G. The mechanism is enclosed in sheet-iron case E.

The current passes from the terminal + through the series winding, and is led into the posi-

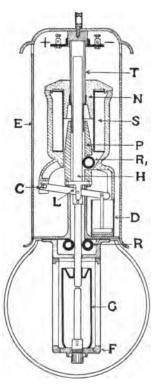


Fig. 93.—Type of arc lamp.

tive carbon by the rings R, which provide a smooth and frictionless contact: connection is made between the negative carbon holder and the terminal—. The shunt coil is connected directly across the lamp terminals.

The second method of applying the principle of the differential coils is shown in Figure 94. There are two

solenoids, one S<sub>1</sub> in series and the other S<sub>2</sub> in shunt with the arc. Each solenoid is provided with a soft-iron plunger indicated by P<sub>1</sub> and P<sub>2</sub> respectively; the upper ends of them are freely suspended from the opposite ends of a rocking lever L. W is a brake wheel which carries a brass drum D turning on the same axis. Round the former passes a brake band B, which is fixed by one end

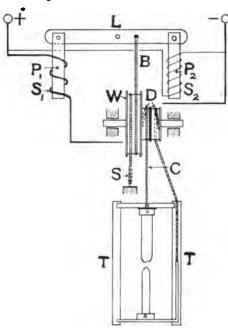


Fig. 94.—Principle of arc lamp.

to the lever L, the other, end being attached to a spring The drum D is made in two parts, bolted together, but insulated from each other. The carbon holders, sliding upon guide tubes T attached to the lamp, suspended flexible means of copper cords C, one from each half of the The susdrum D. pension cords each have a turn round the drum in opposite directions. so that when the drum rothe carbons tates

either approach or recede according to the direction of rotation. The current is conveyed to and from each part of the drum by either spiral connections or brushes

bearing on the revolving rings.

The spring S is so adjusted that when no current is passing the carbons are always brought together. When current is switched on, the plunger P<sub>1</sub> is pulled down; this tightens the brake band and turns the brake wheel and drum. The drum D so revolves that the upper carbon is raised and the other one lowered, thus striking the arc. As the arc lengthens the series current diminishes and the shunt coil prevails, so that

the plunger P<sub>2</sub> is pulled down and the brake band is released sufficiently to allow the carbons to move towards each other. When the series current increases the brake band holds the wheel, and so equilibrium is maintained.

The lamp illustrated in Figure 95 works on a modifica-

tion of the above principle. D and E are the series and shunt coils respectively, and P<sub>1</sub> P<sub>2</sub> their plungers, which are connected to the rocking lever L pivoted at K. tached to L are two clutch racks B. between which works the positive carbon holder C. The negative carbon is fixed and both carbons burn inside the inner globe M. Under the action of gravity the carbon G comes into contact with H, so that, when the current is switched on, the plunger P<sub>1</sub> is attracted up. The canting of the lever L causes the clutch racks B to come together and grip the holder C, and at the same time to move in a vertical direction. lifting C and the carbon G. When the length of arc increases the shunt plunger prevails, slackens the tension of B on the carrier C, and allows the carbons to feed. To one end of the lever L is attached a piston working in a dash pot F which serves to steady

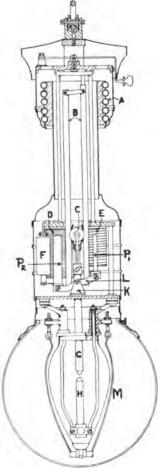


Fig. 95.—Type of arc lamp.

the feeding arrangement. A is a resistance coil for steadying the arc, the function of which will be explained later.

#### FLAME ARC LAMPS

In arc lamps with their carbons arranged coaxially a large percentage of the light emitted from the crater is obstructed by the negative carbon, and the light emitted by the arc itself is only a small percentage of the total. In flame arc lamps the above defects have been remedied as follows:

1. By placing the electrodes at an angle of about 30 degrees with each other, as shown in Figure 98. The arc is maintained between the tips of the electrodes, thereby forming the crater in such a position that none of the light emitted by it is obstructed by the negative carbon.

2. By impregnating the carbons with metallic salts the arc formed by the vapour is rendered more luminous. Carbons so treated are generally termed *chemical* 

carbons.

Composition of Chemical Carbons.—Flame arc lamps are subject to flickering, due to the composition of the carbons, and up to the present this has not been entirely eliminated, though it has been greatly reduced in more recent lamps. In the early forms of chemical carbons a large proportion of calcium salts, mixed with the carbon, produced irregularities in burning. They now usually consist of three zones: the outer zone or envelope is composed of pure carbon, which gives the necessary mechanical strength; the next zone contains carbon mixed with various salts, such as those of calcium and sodium; while the inner centring core is made of the same materials less strongly compressed.

Poisonous fumes are given off by the burning chemicals, and thus render a lamp having chemical carbons unsuitable for use in a room not sufficiently ventilated. These fumes must escape from the combustion chamber to the atmosphere, so that the design of globe does not permit of making the arc totally enclosed. In consequence of this the life of the carbons is very short—60-centimetre carbons lasting only 17 hours. This, coupled with the fact that the carbons are more expensive than ordinary carbons, renders the upkeep of chemical carbon lamps rather costly.

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Distribution of Illumination.—The light emitted by the crater of a chemical carbon lamp is only about 30 per cent. of the total, the greater portion of the light being emitted from the arc itself, as is clearly shown in Figure 96,\* the photograph being taken from a 38-volts 10-ampère arc. This is apparently due to the minute burning particles in the flame being raised to a very high state of incandescence. It has also been determined that the intrinsic brilliancy of the flame of a chemical carbon lamp is about one-third that of the positive crater. The author of the paper referred to



FIG. 96.—Arc of chemical carbon lamp.

in the footnote, specially points out that these chemical carbon lamps are efficient not on account of the crater light at all, but simply because they produce a flame which has a very high illuminating power, and because the light which emanates from the flame is, to a large extent, in the direction in which it is required.

The distribution of light is very different from that of an ordinary arc, as will be observed from Figure 97, which indicates the distribution of light from a flame arc. The maximum luminosity is directly below the arc; the spherical candle-power, and consequently the efficiency, is

<sup>\*</sup> Taken from Journal of Institution of Electrical Engineers, vol. xxxvii. p. 11, December 1906. Paper on "Flame Arc Lamps" by L. Andrews.

much greater than other forms of arc lamps consuming

the same power.

A yellow light is given out by the majority of chemical carbon lamps, and its spectrum is said to be similar to daylight. For the illumination of public buildings and street lighting the yellow-coloured light

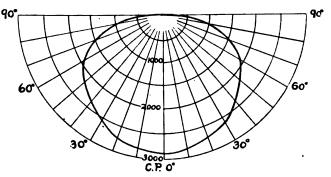


FIG. 97.—Polar curve of illumination for flame arc lamp.

is very effective, and experience has shown that it is the

best illuminant for penetrating fogs.

Construction of Flame Arc Lamps.—The flame arc, produced by carbons arranged side by side, is, as a result of its great length and fan-like expansion, so sensitive to air currents that a very slight draught is sufficient to cause the light to be unsteady. Consequently it is necessary to construct an enclosing cover so that the arc may be protected against draughts: but it must take such a form that no impedance is offered to the free ventilation necessary to conduct away the products of combustion. Such an arrangement is called an economiser, and is indicated by E in Figure 98. It is made of porcelain, which can stand the high temperature of the arc, and is in two parts, kept together by a metal holder; if solid it would crack when subjected to the intense heat.

The fumes evolved during combustion are injurious to the mechanism and insulation of the coils of the lamp, so that to preserve these the combustion chamber must be separated from the compartment containing the mechanism.

Figure 98 illustrates the construction of one form of flame arc lamp. There are three compartments: the top one containing the regulating mechanism; an intermediate one containing an electro-magnet, carbons, and

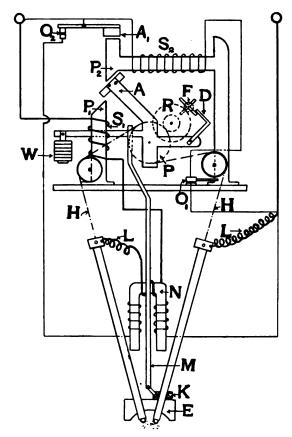


Fig. 98.—Flame arc lamp.

guide rods; and the third one is the combustion chamber enclosed by the globe.

Referring to the figure, there are two electro-magnets at right angles to one another; the vertical one  $S_1$  has its coil in series with the arc, while the coil of  $S_2$  is connected in shunt. Between the respective poles  $P_1$  and  $P_2$ , shaped as indicated, swings an armature A, forming part of a three-limbed casting. The second arm of the

casting carries the detent D controlling the feeding gear, while the third arm carries the balance weight W. The carbon holders running in guide rods are suspended by chains H wound round the pulley P, which is operated by the spur-wheel reduction gear R. The lower ends of the carbons are led into the economiser E, which is supported by the lower part of the frame-work. Above the economiser is the mechanism for striking the arc, which consists of a slider K mechanically connected to the rod M in such a manner that any movement of the armature A moves the extremity of the right-hand carbon. Connection is made to the carbons by means of flexible leads L insulated with glass beads.

The action of the mechanism is as follows:

When the lamp is connected to the supply circuit the shunt magnet becomes energised and attracts the armature A. The detent D then disengages the fourarmed fly-wheel F, and the reducing gear R, being then free to rotate, allows the carbons to come together, due to the attraction of gravity. As soon as the carbons come into contact a current flows through the series winding, and the armature A is attracted towards P<sub>1</sub>. The rotation of A lifts the connecting rod M and slider K, thus separating the carbons and striking the arc. As the length of the arc increases the current through the series coil diminishes so that A moves towards P<sub>8</sub>, thus causing the detent D to release the fly-wheel F, which makes a quarter of a turn and thus allows the carbons to feed by a very small amount. The armature then returns to its position of equilibrium between the poles P<sub>1</sub> and P<sub>2</sub>. The length of the arc is, in the first instance, determined by the strength of the two solenoids S<sub>1</sub> and S<sub>2</sub>, but the final adjustment is made by the balance weight W.

The electro-magnet N is excited by a coil in series with the arc, the result being that its field repels the arc to the tip of the carbons.

As the carbons approach each other at a sharp angle there is a risk that, when the carbons have burned their full time, and consequently do not feed further forward, the arc itself may travel up, with the result that the economiser and some of the frame-work might be destroyed. To prevent this, when the carbons are in their lowest position and cannot feed further, the shunt circuit is automatically broken by a carbon-faced switch  $O_1$  mechanically operated by a small detent on the chain supporting the right-hand carbon. When the shunt circuit is thus broken the armature  $A_1$  is released and the shunt circuit of N is completed at  $O_2$ . This increases the magnetic field of the latter to such an extent that the arc is "blown out."

#### ARC LAMP ACCESSORIES

Globes.—The light from an arc lamp generally requires to be diffused by means of glass globes, the design and density of which are according to the illumination required. Enclosing the arc by globes considerably reduces the amount of light actually obtained from the lamp, and the following gives an approximate value of the percentage of light absorbed by various forms of globes:

Form of Globe.	Light absorbed.			
Cut glass	5-20 per cent.			
Clear ,,	10-20 ,, ,,			
Ground ,,	25-40 ,, ,,			
Opal "	40–60 ,, ,,			

A globe alters considerably the distribution of light from an arc, making it much more uniform, as is shown in Figure 91, in which the dotted lines represent the light distribution when the arc was enclosed in an opal glass globe.

The figures in Table IX. give a comparison between the three types of arc lamps, the same form of globe being used with each lamp.

TABLE IX

Lamp.	Current in Ampères.	Volts on Lamp Terminals.	Mean power in Watts.	Mean hemispherical Candle-power.	Watts per c.p.
Open arc .	10	44	476	633	0.753
Enclosed arc .	6	77	486	338	1.435
Flame arc .	8	44	382	1352	0.282

From the above it appears that the watts per mean hemispherical candle-power are, in the case of the flame arc, only 37 per cent. of those required for the open arc, and 20 per cent. of those required for the enclosed arc; but, as already stated, the high rate of carbon consumption to a great extent nullifies this increase of efficiency.

Steadying or Line Resistance.—Any variation in the current taken by an arc alters the area of the crater on the positive carbon, and this causes the illumination to be very unstable. Hence it is necessary to introduce some compensating device which will maintain a steady distribution of light. The steadying arrangement consists of a resistance R (Fig. 99) connected in series

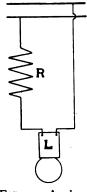


FIG. 99.—Arc lamp steadying resistance.

with the lamp L; the former varies the potential across the lamp terminals inversely as the current. In practice an additional 10 to 30 per cent. of the E.M.F. required on the terminals of the lamps is necessary for steadying the arc.

The action of this steadying resistance is best illustrated by a concrete case. Suppose the steadying resistance of an arc lamp, taking 10 ampères as normal current, is 2 ohms and the pressure available 65 volts. The voltage absorbed by R when the lamp takes the normal current =  $10 \times 2 = 20$  volts, thus leaving 45 volts across the lamp

terminals. Next suppose the current increases by some cause or another to 12 ampères, the voltage absorbed by R is then 24 volts; this leaves only 41 volts across the lamp terminals, and so reduces the current taken by the arc to its normal value. The resistance R thus tends to maintain an approximately constant current through the arc.

The steadying resistance often referred to as the line resistance, generally consists of a length of iron wire wound on a porcelain cylinder, the two ends of the wire being connected to suitable terminals. In some cases this resistance is contained in the lamp itself, as shown at A in Figure 95. A certain amount of energy is

absorbed by the line resistance, which in the example taken is 200 watts, so that the commercial efficiency of the lamp is considerably reduced. For lamps connected to alternating current circuits the line resistance is replaced by a choking coil, the function of which is explained in books on alternating currents.

Arc Lamp Circuits.—For street lighting and the illumination of large buildings the system invariably used is the series parallel arrangement from 230 or 460 volts. The lamps are arranged in groups of from three to ten (according to the type), connected in series, each group being connected in parallel with the supply mains. The method of grouping different types of arc lamps on supply circuits having voltages between 50 and 460, is indicated in Table X.

 Voltage of Circuit.
 Open Arcs in Series.
 Enclosed Arcs in Series.

 50
 1
 ...

 100
 2
 1

 200
 4
 2

 230
 5
 3

 460
 10
 5

TABLE X

When four or more arcs are connected in series no steadying resistance is necessary, as any slight alteration in the length of one arc produces no appreciable alteration in the current.

Cut-out Resistance.—With a number of lamps in series, should the carbons of one lamp cease to feed and the arc increase in length so much that it cannot be maintained, then it, along with all the lamps in series, would be extinguished. To prevent the other lamps from being extinguished, some automatic arrangement must be made to complete a circuit through the lamp that has failed. If the lamps be connected to a constant potential circuit, then not only must the circuit be completed but a resistance must be inserted which absorbs the same voltage as the arc, and so maintain the

normal pressure across the other lamps. Such an arrangement is called a cut-out resistance, and is indicated

diagrammatically in Figure 100.

It consists of an electro-magnet M, excited by a coil  $S_1$  in series with the shunt coil S, which controls the mechanism. When the main circuit through the lamp is broken, the voltage across the lamp terminals + and—increases, and in the same proportion the current through the coil  $S_1$ . This increase in current is sufficient to cause the magnet M to pull down the armature A

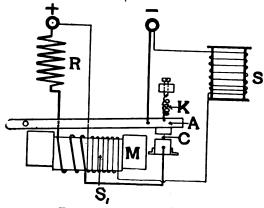


FIG. 100.—Cut-out resistance.

against the spring K, thereby completing the main circuit through the resistance R, contact C, and armature A. The wire forming the resistance R should be capable of carrying the main current for a considerable time, and also absorb the full voltage required by the

lamp.

When the circuit is completed through R the voltage across the shunt coil falls, thus reducing the current and allowing the spring K to pull up the armature and break the circuit. The armature would then go on vibrating, but to prevent this a few turns of wire in series with R is wound round the electro-magnet M. These turns compensate for any drop in volts across the shunt coils, and so maintain the electro-magnet at such a strength that the circuit through R is maintained until the lamps are switched off.

## ILLUMINATION AND PHOTOMETRY

When light falls on a surface it is said to be illuminated. The illumination of a surface depends upon two factors, namely, the candle-power emitted by the illuminant and the distance between the illuminant and the surface illuminated.

Unit of Illumination.—The standard of illumination is that produced by a standard candle at a distance of 1 foot, and is referred to as a candle-foot. The standard candle used as the unit of light in Britain is made of spermaceti and burns at the rate of 120 grains per hour, with a flame 1.8 inches high. It is a very imperfect standard, and when a number of these candles are tested one against another they are found to vary considerably. Other standards of light are the Carcel and the Hefner-Altenck lamps. The Carcel lamp burns colza oil at a given rate and the Hefner lamp burns amyl-acetate, the height of the flame in both cases being adjusted to a definite value. Students who wish for further information regarding these standards are referred to advanced text-books on "Light."

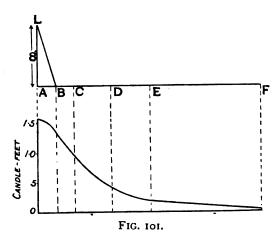
Distribution of Illumination.—The candle-foot is a convenient unit of illumination, being that required for reading purposes. It has been estimated that the illumination due to the sun during a bright day on the streets of London varies between 30 and 40 candle-feet, while the illumination in full moon varies between  $\frac{1}{60}$  and  $\frac{1}{100}$  of a candle-foot.

If c.p. denote the candle-power of a certain lamp, then the illumination on a surface d feet from the lamp  $= c.p./d^2$  candle-feet, this being on the assumption that the surface illuminated directly faces the source of light. When the surface is inclined to the direction of the rays of light, the illumination will diminish in proportion as the projected area of any part of the surface diminishes when viewed from the source of light. The decrease in illumination varies with the cosine of the angle of incidence, the latter being the inclination between the rays of light and the perpendicular to the surface. A ray proceeding horizontally will therefore be

at 90 degree incidence, and a ray falling on a point immediately below the lamp will be at 0 degree

incidence on the horizontal plane beneath it.

The simplest case is the illumination of a horizontal plane by a light radiating uniformly in all directions, it being assumed that the intensity of the light remains constant. Referring to Figure 101, let L A represent the height of a lamp L above the horizontal plane A F, and the angle A L B  $(=\theta)$  the angle of incidence, then



denoting the candle-power of the lamp by c.p. the illumination at B is given by

$$i = \frac{\text{c.p.}}{\text{LB}^2} \cos \theta$$
.

Street Illumination. — Example. — A 100 candle-power lamp giving a uniform distribution of light is placed 8 feet above the street level; draw a curve showing the illumination along the street for a distance of 30 feet.

Referring to Figure 101, let L represent the position of the lamp; then the illumination is calculated for say six positions, A, B, C, D, E, and F along the street, each at a distance of 0, 2.5, 5, 10, 15, and 30 feet respectively from A, a point directly below the lamp.

At A the illumination = 
$$\frac{100}{8^2}$$
 = 1.56 candle-feet.

At B the illumination = 
$$\frac{100}{LB^2}$$
 cos ALB

= 
$$\frac{100}{2.5^2 + 8^2} \times \frac{8}{\sqrt{2.5^2 + 8^2}}$$
 = 1.31 candle-feet.

Similarly the illumination at C, D, E, and F is equal to 0.96, 0.38, and 0.027 candle-foot respectively. The illumination curve is as shown, the ordinates giving the illumination at different positions. The curve indicates how the illumination along a horizontal plane decreases rapidly with the distance.

H. T. Harrison\* has suggested the following as the minimum direct illumination for street lighting:

Main thoroughfares . . . 0.05 candle-foot. Side streets . . . 0.025 ,, ,, Suburban streets . . 0.005 ,, ,,

In main thoroughfares are lamps giving about 500 c.p. each should be erected at a height of from 7 to 9 metres, the distance between them being about 10 times their height. In streets which are narrow or shaded by trees, smaller units of light placed closer together will give better illumination.

Photometry. — The candle-power of a lamp is measured by comparing it with a standard light; the apparatus used is called a photometer, and its principle is as follows:

The eye is only capable of very roughly estimating the relative intensity of illumination from two sources, but it is capable of perceiving with considerable accuracy when the illuminations are of equal intensity. Hence to compare the illuminating power of two sources of light, a screen, which may consist of a piece of white paper having a uniform "grease spot" at its centre, is placed between them and adjusted with respect to the distances, so that both sides of it are equally illuminated.

<sup>\*</sup> Journal of Institution of Electrical Engineers, vol. xxxvi. p. 198, December 1905.

Referring to Figure 102, let P and Q represent the two sources of illumination and A the screen having the grease spot. The screen A is known as the photometer head. When both sides of the screen are equally illuminated let the distance from P to the screen be  $d_1$ , and from Q to the screen  $d_2$ . If

$$P \xrightarrow{\text{Fig. 102.}} Q$$

the illuminating power of the sources P and Q be in candle-power and denoted by c.p.<sub>1</sub> and c.p.<sub>2</sub> respectively, the illumination on A due to the source P is c.p.<sub>1</sub>/ $d_1^2$  candle-feet, and that due to the source Q is c.p.<sub>2</sub>/ $d_2^2$  candle-feet.

The two illuminations are equal; therefore

$$\frac{\text{c.p.}_1}{d_1^{\frac{1}{2}}} = \frac{\text{c.p.}_2}{d_2^{\frac{1}{2}}}.$$

If c.p., be the illuminating power of the standard Q, the candle-power of P is given by

$$c.p._1 = c.p._2 \times \frac{d_1^2}{d_2^2}$$
.

For instance, if the standard Q be 16 c.p. and the distances  $d_1$  and  $d_2$  be 80 centimetres and 120 centimetres respectively, then the candle-power of the lamp being tested

$$= 16 \times \frac{80^2}{120^2} = 7.$$

For electrical engineering work a secondary standard of light is used and is generally a carefully made glow lamp which has been previously calibrated against an absolute standard, so that the candle-power can be obtained from a knowledge of the watts consumed.

A great variety of photometers have been devised, but they all work on the above principle. The Bunsen

photometer is similar to the one described above, with the addition of two mirrors inclined at an angle of 45 degrees to the screen, so that both sides of the screen can be viewed simultaneously, thus enabling a more accurate reading to be obtained.

Lummer-Brodhun Photometer.—The photometer in most general use is that illustrated in Figure 103 and is known as the Lummer-Brodhun photometer. It consists of an opaque screen S placed inside a metal case

M, so that it can be illuminated from two sources of light, and Ο. The two sides of the screen are viewed through the telescope T by an arrangement of two right-angled prisms P1 and P. and a double glass prism Ps. The latter prism consists of two right-angled prisms placed tobeing partly beveiled.

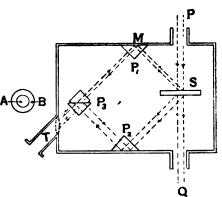


Fig. 103.—Lummer-Brodhun photometer.

gether so as to form a cube, the largest face of one

The path of the light is as shown, and an observer looking into the telescope T will see an illuminated ring surrounded by another zone of different intensity. The central rays reaching the eye at T come from the top face of the screen, and the surrounding rays come from the bottom face. The observer therefore moves the photometer until the central part A, illuminated from P, and the outer part B, illuminated from Q, are of the same brightness. The intensity of illumination on both sides of the screen is then the same, and the relative candle-powers of the two sources can be determined as above.

The relative illuminating powers of two sources of light are only strictly comparable when the colour of the light emitted by both is the same, but this very seldom happens when testing electric lamps. When there is a

difference in colour a rough comparison can be made by comparing the candle-power of the two sources, when a red, a yellow, and a blue coloured glass are placed in turn between the eye of the observer and the telescope T. The mean of the three values thus obtained may be taken as the true photometer reading.

Trotter's Photometer.—Figure 103A illustrates the

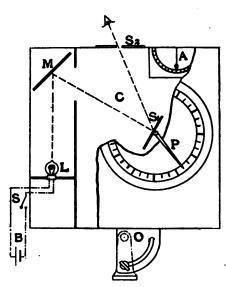


FIG. 103A.—Trotter's portable photometer.

design of a portable photometer measuring either illuminating power or the illumination in candlefeet at any required angle. A small standard lamp L throws off a beam of light, which is reflected by mirror M on to the screen S<sub>1</sub>, the parts mentioned being enclosed inside a case C. The screen S, can be rotated about an axis. and is viewed through three small slits in the screen S<sub>2</sub>, which receives the illumination

to be measured. The lamp L is carefully aged and standardised, so that it can be relied upon to retain its candle-power almost indefinitely, since it is only in use during the actual time the reading is being taken, and this, as a rule, does not exceed 30 to 40 seconds. A portable 4-volt battery B supplies current to L, the circuit through which is made by the switch S. In operating the instrument the screen S<sub>1</sub> is rotated about its axis, and the illumination on it thereby varied, until a balance of brightness between S<sub>1</sub> and S<sub>2</sub> is obtained. The illumination of S<sub>2</sub> in candle-feet is then read off on a direct reading scale over which the pointer P passes, the latter being fixed to the axle of the screen S<sub>1</sub>.

The case C is pivoted at O, and can be moved through an angle of 90 degrees, thus allowing the illumination to be measured on any plane between the horizontal and the vertical, the setting of the photometer being adjusted by the aid of a plumb-bob A, which moves over a graduated scale.

If, instead of the illumination, the candle-power of the source of light is required, the screen S<sub>2</sub> is turned towards it so that the angle of incidence shall be o degrees. The measurement of illumination is then made, and this value, multiplied by the square of the distance in feet of the photometer from the light, gives the candle-power required.

The instrument is calibrated, in the first instance, by producing known illuminations on the screen  $S_2$ , and finding the corresponding positions of the pointer P which give a balance. In order to make the instrument applicable to lights of every colour, specially coloured screens are provided, which can be substituted for  $S_1$  or  $S_2$  as required.

### CHAPTER VII

### UNDERGROUND AND AËRIAL CONDUCTORS

ALL conductors have a definite resistance, so that when current is transmitted along them a certain expenditure of energy takes place. The energy expended generates heat, and is proportional to C<sup>2</sup>R, where C is the current and R the resistance of the conductor. With a given current the temperature gradually increases until the rate of generation of heat is equal to the rate of loss of heat by radiation, at which stage the temperature remains constant for a particular current.

For a given current the increase in temperature of

a conductor will depend upon:

1. Its electrical resistance.

2. The nature of its radiating surface.

3. The material and condition of the surrounding medium.

As mentioned in Chapter II., copper, on account of its low specific resistance, is generally used as the conductor in the transmission of electrical energy, although, under certain conditions, aluminium and iron are employed for aërial lines. The copper used for such purposes should be electrolytically refined, and of not less than 98 per cent. conductivity, according to the standard suggested by the Engineering Standards Committee. (The E.S.C. standard for annealed high conductivity copper is a uniform wire 1 metre long, weighing 1 gramme, and having a resistance of 0.1508 standard ohm at 15.6° C., i.e. 60° F.)

Copper produced by the process of smelting is less expensive, but in the best practice is not now used for

electrical purposes, as its conductivity, due to the presence of small quantities of foreign materials, is never as high as that electrically deposited.

As regards radiation, a blackened or rough surface radiates heat at about twice the rate of a polished surface. Professor S. Forbes has determined that gutta-percha is a better radiator of heat than rubber in the ratio of 48 to 41.

Copper wires used as conductors are of circular crosssection drawn into certain definite sizes or gauges, the usual practice among British cable manufacturers being to adopt the standard wire gauge (S.W.G.). Appendix I. gives details of the various sizes of copper wires employed in electrical engineering, the values being expressed in metric units.

For the transmission of electrical energy the standard practice is to use stranded conductors or cables, the wires forming the cable being twisted into strands having 3, 7, 19, 37, 61, or 91 separate wires; for instance, a 37/20 cable consists of 37 wires of size No. 20, S.W.G. This arrangement ensures the necessary flexibility, and largely eliminates the inherent mechanical weakness of solid copper to fracture when subjected to repeated bending.

Dimensions of Conductor.—The size of conductor required to transmit a given current must be settled from a knowledge of—

- 1. The permissible percentage transmission loss.
- 2. The maximum permissible temperature rise.

The Standardising Committee of the Institution of Electrical Engineers recommend the following formula for determining the carrying capacity of a conductor:

$$C = 2.6 a^{0.82}$$

where C is the current in ampères and a the area of cross-section of the conductor in square inches. The current density determined by this formula is such that the maximum temperature rise will not exceed 17° C., while conductors of small sectional area will be worked

at a relatively higher current density than those of larger sectional area. This follows because the radiating surface per unit area of cross-section decreases with increase in diameter; consequently in order to maintain a uniform temperature rise the current density must be reduced as the area of cross-section (or diameter) increases.

The more general practice among British engineers is to limit the current density to 155 ampères per square centimetre (1000 ampères per square inch) of sectional area, thus obtaining a drop in pressure of 2.7 volts per 100 metres.

Table XI. gives the dimensions, capacity (on the basis of (1) I.E.E. formula, and (2) 155 ampères per square centimetre), resistance, and weight of stranded copper conductors used in practice. The values are given both in British and metric units.

In certain cases the values of current given in the accompanying table are not adhered to, but each problem is considered on its merits, as shown by the following

example:

Example.—Current is required for a group of 200 230-volt lamps taking 60 watts each: the lamps are at a distance of 100 metres from the source of energy. What must be the size of cable, if the loss of pressure is not to exceed 2.5 per cent. of the required P.D. across the lamp?

Current transmitted along the cable

$$=\frac{200 \times 60}{230} = 52$$
 ampères.

Volts drop in cable =  $2.5 \times \frac{230}{100} = 5.75$ .

Resistance of cable =  $\frac{E}{C} = \frac{5.75}{52} = 0.11$  of an ohm.

Area of cross-section of cable =  $\frac{\rho \times l}{R}$ .

 $\rho$  for copper = 1.6 × 10<sup>-6</sup> ohms per centimetre cube.  $l = 100 \times 2 = 200$  metres = 2 × 10<sup>4</sup> centimetres.

Area of cross-section of cable

= 
$$\frac{1.6 \times 10^{-6} \times 2 \times 10^{4}}{0.11}$$
 = 0.29 square centimetre.

## DIMENSIONS, CARRYING CAPACITY, WEIGHTS, AND

No. of wires	Carrying	Capacity.	Effective sectional		
and S.W.G.	Ampères at 155 per square centimetre.	Ampères at I.E.E. standard.	Square inches.	S mil	
7/22	4.3 5.6	8.5	0.0043		
7 21	5.0	10.6	0.0056		
7 20 7 19	7.0 8.7	12.9	0.0070 0.0087		
7 18	12.5	15.3 20.6	0.0125		
7 17	17.1	26.6	0.0171		
7 16	22.3	33.1	0.0223		
7 15	28.2	40.2	0.0282		
7.14 7.13	34.0 46.0	47.8 60.1	0.0340 0.0460		
19 20	19.1	29.2	0.0191		
19 19	23.6	34.7	0.0236		
19/18	34.0	46.8	0.0340		
19/17 19/16	46.3 60.4	60.3 75.0	0.0463 0.0604		
19'15	76.5	91.1	0.0765		
19114	94-4	108.3	0.0944		
19,13	124.9	136.2 166.4	0.1249	l I	
19/12 19/11	159.5	199.2	0.1595		
37 '16	117.6	129.6	0.1176		
37 15	148.9	157.3	0.1489		
37/,14	183.8	187.0	0.1838	j	
37/13 37 12	243.1 310.5	235.2 287.4	0.2431 0.3105		
61/16	193.9	195.4	0.1939	<u> </u> 	
61/15	245.5	237.0	0.2455	1	
61/14	302.9	281.6	0.3029	1	
61 13 61 12	400.8 512.0	354-3 433.1	0.4008 0.5120		
91/15	368.0	329.0	0.3680		
91:13	451.9	391.0	0.4519	1	
91 13	597.7	<b>4</b> 89. <b>o</b>	0.5977	ı	
91 12	763.8	598.o	0.7638	,	
91 11	950.4	719.3	0.9504		

# RESISTANCES OF STRANDED COPPER CONDUCTORS

a.	Weight of	Conductor.	Resistance at 15.5° C. (60° F.) Standard Ohms.			
e res.	Lbs. per	Kilogrammes per kilometre.	Per 1000 yards.	Per kilometre.		
,	50 66	25	5.636	6.164		
?	83	32 41	4.316 3.410	4.720 3.729		
	103	50	2.761	3.020		
	148	73	1.918	2.097		
	201	100	1.410	1.541		
1	263	129	1.080	1.181		
	333	163	0.852	0.932		
	411 544	202 267	0.690 0.522	0.755 0.571		
	226	111	1.257	1.375		
	279	137	1.019	1.114		
	402	197	0.707	0.773		
	547 715	269 351	0.517 0.398	0.568 0.4305		
	905	445	0.3143	0.3437		
	1,117	549	0.2547	0.2785		
	1,478 1,888	726	0.1926	0.2106 0.1649		
	2,349	928	0.1507 0.1211	0.1325		
	1,394	685	0.2045	0.2236		
l	1,763	866	0.1615 •	0.1766		
	2,176 2,878	1069 1417	0.1309 0.0989	0.1431 0.1082		
	3,678	1808	0.0774	0.0847		
	2,296	1129	0.1240	0.1356		
	2,907	1429	0.0979	0.1071		
	3,589	1764	0.0794	0.0868		
	4,746 6,065	2333 2981	0.0600 0.0470	0.0656 0.0514		
	4,337	2131	0.0653	0.0715		
	5,355	2631	0.0532	0.0582		
	7,080	3480	0.0402	0.0440		
	9,048	4444	0.0315	0.0344		
	11,256	5532	0.0253	0.0277		

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From Table XI. a 19/17 cable has the equivalent required sectional area.

#### INSULATED CABLES

The material forming the insulation of cables is generally referred to as the di-electric, and should

- 1. Be mechanically strong, so that it is not easily injured.
- 2. Have flexibility, so that it can be bent without cracking.
- 3. Be capable of standing moderately high temperatures without injury.
- 4. Be unaffected by gases or acids with which it is liable to come into contact.

The materials used for insulating cables may be broadly divided into two classes; namely, hygroscopic and non-hygroscopic. The hygroscopic materials chiefly used are jute and paper. To the non-hygroscopic class of di-electric belong materials such as pure rubber, vulcanised rubber, and bitumen. Table XII. gives the specific resistance of the materials most generally used for insulating cables. The resistance is given in megohms per centimetre cube, and the temperatures are those at which the values were obtained: the latter are necessary, as the specific resistance of all insulating materials decreases with increase of temperature.

TABLE XII

SPECIFIC RESISTANCE OF INSULATING MATERIALS
USED FOR CABLE DI-ELECTRIC

Material.		 Megohms per centimetre cube.	Temper- ature.
Gutta-percha	:	$250 \times 10^{6}$ to $450 \times 10^{6}$ $400 \times 10^{6}$ $3000 \times 10^{6}$ $4000 \times 10^{6}$ $5000 \times 10^{6}$ to $10,000 \times 10^{6}$ Infinity.	15° C. 15° C. 15° C. 15° C.

Pure rubber, as will be seen, has the highest specific resistance, and the best class of rubber for insulating purposes is that obtained from the Para rubber tree. Pure rubber, however, readily oxidises, and has a great affinity for moisture, so that its physical state changes with time, thereby lowering its specific insulation. Vulcanised rubber, prepared as described below, is now largely used, and although its specific resistance is lower than that of pure rubber, it does not deteriorate so rapidly under atmospheric conditions. Gutta-percha is now seldom used; for, although it originally has a high specific insulation, it becomes brittle when exposed to atmospheric changes and softens at a comparatively low temperature.

The necessary thickness of a di-electric depends upon the specific resistance of the insulation, the working pressure, and the diameter of the conductor. For pressures up to 600 volts the thickness varies between 2 and 3.3 millimetres, while for pressures between 1000 and 10,000 volts the minimum thickness of di-electric is about 3.7 millimetres, and increases by 1.2 millimetres per 1000 volts.

From a knowledge of the specific resistance of the insulating material, the insulation resistance of a length of cable can be determined in the following manner:

From the formula  $R = \frac{\rho \times l}{a}$ , the resistance of a thin circular lamina of the di-electric, having a radius r, thickness dr, and length l, is given by

$$R_1 = \frac{\rho \times dr}{2\pi r l}.$$

The di-electric may be considered as a series of concentric laminæ similar to above, in which the radii vary from  $r_1$  the internal radius of di-electric, to  $r_2$  the external radius. The total insulation resistance of the cable will then be given by

$$R = \frac{\rho}{2\pi l} \int_{r_1}^{r_2} \frac{dr}{r}$$
$$= \frac{\rho}{2\pi l} \log_e \frac{r_2}{r_1}.$$

Example.—Calculate the insulation resistance of a kilometre of cable, the di-electric of which is vulcanised india-rubber, having a specific resistance of  $4 \times 10^{16}$  ohms per centimetre cube. The radius of the core of the cable is 5 millimetres, and the di-electric is 2.5 millimetres thick.

 $r_1 = 0.5$  centimetre.  $r_2 = 0.5 + 0.25 = 0.75$  centimetre.  $\rho = 4 \times 10^{16}$  ohms per centimetre cube.  $l = 10^5$  centimetres.

The insulation resistance is given by

$$R = \frac{4 \times 10^{16}}{2\pi \times 10^{6}} \times \log_{2} \frac{0.75}{0.5} = \frac{2 \times 10^{10}}{\pi} \times 0.4$$
= 2.5 × 10<sup>9</sup> ohms = 2500 megohms.

Cables for electrical purposes may be divided into three classes:

- 1. Cables insulated with vulcanised rubber.
- 2. Cables insulated with plastic materials.
- 3. Cables insulated with fibrous materials, impregnated with oil or bituminous compounds, and covered with some waterproof material such as lead.

Vulcanised Rubber Cables.—In the early days of electrical engineering, rubber-insulated cables were the only ones used, but owing to the increasing cost of rubber they have been largely superseded by classes two and three, and are only used where high insulation and easy manipulation are of first importance.

Vulcanised rubber is prepared from pure rubber mixed with about 5 per cent. of sulphur, the vulcanising taking place at a temperature of about 150° C. Some of the sulphur forms crystals in the vulcanising process, and when the cable is exposed to moisture or chemical action the crystals dissolve, causing the dielectric to become perforated, and lowering the insulation resistance of the cable. Manufacturers, however, take the necessary precautions to reduce this deterioration to a minimum.

The strands of conductors insulated with vulcanised rubber should always be tinned, and the cable covered

with a few layers of pure rubber tape to prevent the sulphur used in the vulcanising process from attacking the copper. The importance of perfect tinning cannot

be over-rated for the following reasons:

The deterioration to which rubber is most liable is that due to oxidation, and this takes place to a greater extent with pure rubber than with vulcanised rubber. Copper has a great affinity for oxygen, but will readily part with its oxygen to a substance which has a greater affinity for it. Rubber is one of these substances. Hence in a rubber-insulated cable there are two substances—copper and rubber—in close proximity which, for chemical reasons, should be kept apart. The coating of tin on the conductors acts as the separating medium, and from the above facts the great importance of its efficient application is clear.

The first layer of di-electric should consist of rubber without admixture of any kind, and for manufacturing purposes should have certain good mechanical properties. The rubber used for such purposes is that obtained from the Para rubber tree. In order to give it the necessary mechanical properties, the rubber is "aged" by hanging in dark rooms at a certain uniform temperature for several months. In the case of cheap cables, pure rubber is substituted by a lower grade rubber in which the requisite elasticity and mechanical properties are obtained, by treating the surface with chloride of sulphur in carbon bi-sulphide. Such "rubber" thus contains an ingredient which is inconsistent with the function of the rubber; also in many cases traces of hydrochloric acid are present as an after-result of this chemical treatment. It will be obvious that there are considerable risks in using such substitutes.

The vulcanised rubber forming the body of the dielectric should have for its basis fine Para rubber, be vulcanised with the minimum proportion of sulphur, and mixed with mineral matter only to the extent required for the particular grade of cable which it is intended to produce. Rubber substitutes should never be used; in fact no organic matter other than rubber should be Any known substitutes increase the liability to

oxidation, because they only form mechanical mixtures, and neither combine chemically nor cohere physically, but form cables which soon become electrically and mechanically defective.

The usual test for the presence of such substitutes is to place a sample of the di-electric in a steam chamber at a temperature of 150° C. for, say, four hours. The presence of any of the deleterious substances indicated

becomes apparent by their saponification.

In order to protect the di-electric from slight mechanical injury, it is covered with specially treated braiding, woven so as to resist moisture. Rubber itself. being of a highly inflammable nature, cables insulated with rubber compounds should preferably be served with an overall layer of some non-inflammable covering in the form of tape or braiding; tape and braiding together are commonly used, and such cables are commercially known as "Fireproof" or "Fire-resisting" cables.

Figure 104 shows a section through a single core

cable, insulated in the manner described.

Condensed vapour, if present in appreciable quantity, is very detrimental to rubber-insulated cables. The deterioration of rubber under such conditions is not, as is commonly

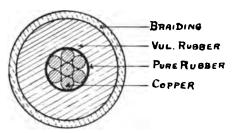


FIG. 104.—Vulcanised rubber insulated cable.

supposed, due to the direct soaking-in of the water, but to chemical actions which gradually decompose the rubber. In some cases moisture from wet plaster finds its way into the pipes or ducts in which cables are laid, and this being usually of an alkaline nature is fairly rapid in its deteriorating action. This action is most noticeable where low-grade di-electrics are used, as they are much less homogeneous than pure rubber compounds, and therefore the reactions between the moisture and the sulphur (which ingredient plays the

chief part in these reactions) can take place with greater

facility.

The increasing cost of rubber-insulated cables, due to the immense development within recent years in electrical engineering and other industries in which rubber is extensively used, has stimulated investigations into the di-electric properties of other materials. These investigations have resulted in the adoption, with more or less success, of bitumen, paper, fibre, etc., as insulating media.

Vulcanised Bitumen Cables.—Cables insulated with pure bitumen were found to be liable to decentralisation. Vulcanised bitumen is now used, and is produced by sulphuretting the products of distillation of certain bituminous oils. This alone, or with other compounds, forms the basis of several cable-insulating compounds. In cables thus insulated the conductor is first covered with a thin layer of fibrous insulation, such as jute or paper impregnated with insulating compounds. The dielectric proper is vulcanised bitumen applied warm, and then subjected to special treatment to give it the necessary mechanical strength. The dielectric is finally covered with the necessary protecting tapes and braidings to suit the conditions under which the cable is to be used.

The disadvantages of this type of cable are:

First. Its tendency to soften and decentralise under undue heat applied externally, or internally through overloading. Bitumen-insulated cables should not be worked at a greater current density than 155 ampères per square centimetre.

Second. Their lack of mechanical strength necessitates more careful handling than with other classes of

cables.

A di-electric of this nature for ordinary cables, which may be subject to considerable variation in temperature, should be such that it does not get too soft at fairly high temperatures, or too brittle at low temperatures. Hardened compounds are made by loading the vulcanised bitumen with mineral matter which can only form a mechanical mixture, and therefore subdivides the vulcanised bitumen, so that instead of a

homogeneous resilient mass a hard mixture is obtained which is highly susceptible to the deteriorating influences to which cables are usually exposed.

The compounds commonly used contain elements which are affected by various external agencies. Air, for instance, has a gradual hardening and oxidising effect on them, producing brittleness, particularly if the adulterants be free oils or other oxidisable materials. Acids, too, have much the same effect, but alkaline solutions produce most rapid deterioration.

Fibrous Di-electric Waterproof-Sheathed Cables.— The fibrous insulating materials generally used are paper, jute, and cotton: the former generally consists of manilla paper and is the more extensively used; the latter are frequently applied in the form of a yarn. These fibrous materials are impregnated with oil or bituminous compounds to enhance their insulating properties, and also to render the cable more pliable and reduce the liability to absorb moisture. Resin oil, or resin and resin oil are frequently used for this purpose.

Inferior forms of fibrous di-electric cables usually contain small proportions of manilla paper and large proportions of straw, esparto, and wood, all chemically treated. The introduction of such substances has the

following effects:

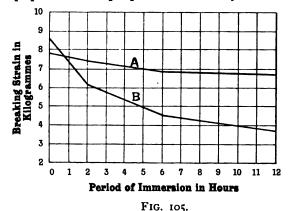
First. The di-electric strength and insulation resistance is lowered. A cable for 10,000 volts working pressure, having chemical wood for the di-electric, requires 70 per cent. greater thickness than a cable of the same di-electric strength in which manilla paper is the di-electric.

Second. The mechanical strength and resilience are impaired. The extent and rapidity of the deterioration of woody papers under the influence of heat are shown in Figure 105. The curves are reproduced from a paper on Electrical Cables by Atkinson and Beaver.\* Two samples of di-electric were experimented with, one prepared with manilla paper and the other containing

<sup>\*</sup> Manchester Section of the Institution of Electrical Engineers, 31st January 1905.

sulphite (chemical wood) paper: these were placed in oil at a temperature of 155°C., and the breakdown stress in kilogrammes was obtained at various periods as indicated by the curves. Curve A is for manilla paper, and B for chemical wood-paper. Subsequent analysis of the latter indicated that traces of residual chemicals probably contributed largely to its more rapid deterioration. The curves represent the average results of about 100 separate tests on each class of di-electric.

Third. There is a danger of disintegration in course of time due to the action of residual chemicals. Manilla paper can be prepared with very little chemical



treatment, but the fibrous material prepared from straw, esparto, or wood fibres, requires to be subjected to severe and drastic chemical treatment, and it becomes practically impossible to free the fibre from every trace of the chemicals used.

The impregnating compounds used by different manufacturers vary considerably. From an electrical point of view they should have the highest possible specific resistance, their specific inductive capacity should approach as nearly as possible that of the fibrous material, and their consistency should be plastic but not fluid.

Fibrous di-electrics have rather a high temperature coefficient, and Figure 106 is a curve illustrating the variation of insulation with temperature for a standard

paper-insulated cable. At 16° C. the insulation resistance is 500 megohms, but at 26° C. it is only 100 megohms, this being equivalent to a variation of 20 per cent. per degree centigrade

degree centigrade.

The weak point of this class of cable is that, however well the fibrous material is impregnated, it is always liable to more or less readily take up moisture from the atmosphere, whereby the insulation resistance is reduced; hence the necessity of covering with a waterproof sheath. In most cases the sheath consists of lead. The

thickness of the lead is such that it forms an additional mechanical protection against damage in handling and external corrosion. The lead is applied in a plastic state under hydraulic pressure, the greatest care being taken to ensure an absolutely non-hygroscopic covering. Failure to attain this appears to have been the cause of many breakdowns with this class of

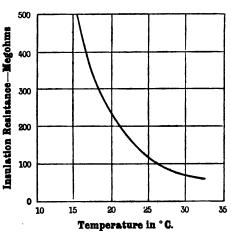


FIG. 106.—Variation of insulation resistance with temperature for paperinsulated cables.

cable, though many more have been due to corrosion in various forms.

The chief causes of corrosion in lead coverings under working conditions may be summarised as follows:

- 1. Impurities in the lead causing local galvanic action.
- 2. Corrosion by chemical action.
- 3. Electrolysis.

The first cause of corrosion is now very rare, as analyses show that the total proportion of impurities in practically any brand of new soft British pig lead will not average more than 0.5 per cent. The only impurity likely to get into the lead during the manufacturing

process is lead oxide, but the chances are remote owing to improved methods of manufacture.

Corrosion due to the second cause is fairly common, and may occur in certain soils where organic acids are produced by the decomposition of wood or vegetable matter, or where cables are laid in "made-up" ground

consisting of ashes, domestic refuse, etc.

Electrolysis is by far the most serious form of lead corrosion, and is also the most common. The word electrolysis is here taken to mean the electro-chemical action due to the passage of a current to or from the lead. The corrosive effect will depend upon the magnitude of the current, and the character of the corrosion may vary from minute holes to large patches, though faults would not be apparent until the di-electric was sufficiently exposed to absorb moisture and cause a dead earth or short circuit. The deterioration, due to electrolytic action, can be greatly reduced by careful attention to bonding at joints, which ensures electrical continuity throughout the sheath, the latter being well earthed at suitable points.

Instead of a covering of lead a waterproof envelope of non-hygroscopic material, such as vulcanised bitumen, may be provided. Such cables have all the advantages of the high specific insulation and di-electric strength of the lead-covered paper-insulated cables, and, in addition,

the electrolytic action is eliminated.

Cables of this class are comparatively low in first cost, and if constructed of good materials are very efficient. They have been largely used for lighting and power mains at all voltages. Again, with the use of paper as an insulator, greater overloads can be carried with safety than would be possible with vulcanised rubber or bitumen. This in many cases is an advantage.

The great disadvantage of paper-insulated cables lies in the extreme care necessary to exclude moisture, as the insidiousness with which it creeps when once absorbed is not less than amazing. Figure 107 illustrates a special terminal for sealing the ends of paper-insulated cables. The conductor is sweated into the socket S, and the joint is covered with a hollow glazed porcelain

insulator P attached as shown, the inside being filled up solid with bituminous compound B poured in through the aperture A. The joint is entirely surrounded by bitumen, which effectually excludes moisture from the di-electric. When the cable is lead-sheathed the lead terminates in a metal end-piece M which is screwed into the porcelain, the end-piece being "wiped" to the lead sheath.

Multiple Core and Concentric Cable.—Where two, three, or four conductors of a system of feeders or

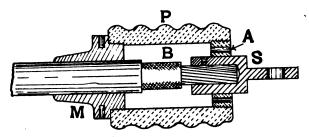


FIG. 107.—Sealing end for paper-insulated cables.

distributors follow a common route, it is sometimes considerably more convenient in handling and laying to have them in the form of a single cable than as separate single conductors. Cables are therefore made consisting of two or more conductors, arranged either side by side or concentrically.

A three-core cable is shown in section, Figure 108. It consists of three conductors of circular section, each separately insulated, bound together, and insulated in common as shown.

Figure 109 shows a section through a two-conductor concentric cable consisting of the inner conductor or core; the first di-electric; the second or outer conductor (the wires of which are selected to have an equal sectional area to the inner conductor); the second di-electric; a lead sheath; and finally braiding or armouring, depending upon the conditions under which the cable is to be used. Two-conductor concentric cables are usually referred to as simply "concentric cables," and the three-conductor variety as "triple concentric cables."

The latter are chiefly used on three-wire direct-current systems.

In concentric cables the inner conductor should always be the negative, in order to reduce the effect of osmosis. The phenomenon of electrical osmosis, whereby moisture tends to accumulate at the negative conductor but is repelled from the positive, can be readily observed by placing two metal plates, connected to a source of E.M.F., into some moist clay. The osmotic action commences immediately there is a

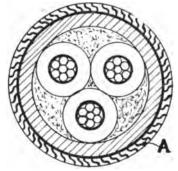


FIG. 108.—Three-core armoured cable.

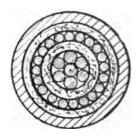


FIG. 109.— Concentric leadsheathed cable.

difference of potential between the two conductors and varies in intensity as the E.M.F., and if the outer conductor be the negative there is a tendency to lower the insulation resistance between that conductor and earth, until finally minute currents pass from the negative conductor to earth causing electrolytic action. Hence the advisability of keeping the negative conductor as far away from earth as possible, owing to the natural tendency to become earthed.

Armouring.—If a cable is to be laid directly in the ground or placed where it is likely to meet with rough usage, a mechanical protection or armouring should be applied. Armouring may take the form of steel tape, usually in two layers, the lays being in opposite directions and lapped over the cable in such a manner that the space between adjacent convolutions of the first is covered by those of the second. Joints in the tape

should be either brazed or welded, no other joint being permanent. After application, the armouring is coated with some waterproof material, and the cable finished off with an overall serving of yarn, or jute braiding soaked in tar.

Armouring is also sometimes in the form of galvanised iron or steel wires of a suitable gauge and having a tensile stress of not less than 4000 kilogrammes per square centimetre. The wires must closely envelop the cable, and are applied over a bed of tarred jute, lapped on in the opposite direction to the lay of the wires forming the conductor. This armouring is finally treated as in the case of steel tape. In special cases the wires are of the cross-section shown at A in Figure 108, each wire locking into the side of its neighbour. This forms the best and strongest mechanical protection devised for direct application to cables.

#### METHODS OF LAYING INSULATED CABLES

Insulated cables for the transmission of electrical energy are invariably laid underground in one of three systems:

- 1. Solid.
- 2. Draw-in.
- 3. Direct.

Solid System.—In this system the cables are laid in wood, earthenware, or iron troughs, filled up solid with an insulating compound poured in when heated to a fluid state. Cables laid in this manner do not require to be armoured, as the troughing affords a good mechanical protection.

Wood troughing is the least expensive, and can be conveniently made in greater lengths than troughing of either of the other materials. It should be of well-seasoned material impregnated with a suitable preservative, great care being taken to ensure that the preservative contains no ingredient likely to be injurious to the filling-in compound.

Glazed earthenware troughing of various forms is

also largely used, and has the advantage over wood that it is not liable to rot. Its cost does not materially exceed that of wood, and is considerably less than the cost of cast iron. It cannot, however, be conveniently obtained in greater lengths than I metre, so that a large number of joints is inevitable.

Cast-iron troughing is the most costly, even when of very thin section. Cast-iron and earthenware troughs are usually supplied with socket ends, whereby each

length of troughing is jointed with the next.

Cables laid in troughing are supported every few metres on insulating bridge-pieces, so that the filling-in compound entirely surrounds the cables. The bridge-pieces are usually of wood or asphalt. Asphalt bridge-pieces are far more efficient, because under proper conditions of filling the trough, the surfaces which come into contact with the hot compound are melted, and, in cooling, the whole forms a practically homogeneous mass.

The material used for filling the trough should be either refined bitumen or the best coal-tar pitch. Coaltar pitch is liable to crack, but to render it plastic it is mixed with a certain quantity of shale-oil. Trinidad bitumen is the most efficient material to use, and in a semi-refined state contains natural oils which render it more adhesive and less liable to crack.

After the trough has been filled up solid it is generally

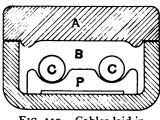


FIG. 110.—Cables laid in bitumen.

covered with a single layer of bricks or tiles, except in the case of cast iron, when the cover is usually of the same material. Several cables may of course be laid in one trough by making it of sufficient width. Figure 110 shows a section through a trough made of earthenware. The cables C

rest on the bridge-pieces P and so are entirely surrounded by the bitumen B. The cover A is fluted longitudinally on the under surface, and so held firmly in position laterally. Draw-in System. — In this system the cables are drawn into ducts, of which there are several forms. In the early days of electrical engineering cast-iron pipes were invariably used, but owing to their high initial cost have been superseded by stoneware conduits. The latter may be either in the form of ordinary drain pipes of 7 to 10 centimetres internal diameter, or of casing, in which a number of ducts are made up in one block. The latter is the more general practice, and Figure 111 illustrates a 3-way conduit.

Such conduit is usually made from hard-burnt glazed stoneware. This material is strong and tough,

and is thoroughly proof against the chemical action of the soil, and hence very durable. Earthenware conduits are invariably of rectangular section, and by grouping a number of ducts in one block a given number of ways can be provided within the minimum space. It is found a convenient

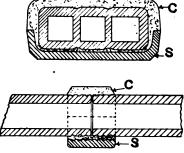


FIG. 111.—Three-way conduit.

plan to adopt a 3-way or 4-way conduit as a unit, and to build up multiples to the required number.

The ducts are laid at a depth of about 40 centimetres or less below footways and 80 centimetres or more under roadways. At intervals of from 40 to 80 metres draw-in boxes are built in line with the conduit. These boxes should be of at least sufficient area to conveniently pass in the maximum size of cable without undue bending, and are usually constructed of brick, provided with a cover C, as illustrated in Figure 112.

The jointing of lengths of conduit is effected with compound or cement C, as shown in Figure 111. A mandril, capable of being mechanically expanded in situ, is inserted at the joint to prevent the intrusion of the jointing material. The mandril is, of course, released and withdrawn as soon as the joint is sufficiently set. The lengths of conduit are kept in alignment by

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means of permanently placed earthenware saddles S, which also serve as moulds for the joints. The conduits are sometimes laid on a bed of concrete, in

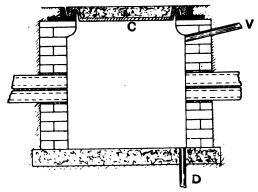


FIG. 112.—Draw-in box.

which case saddles at the joints may be dispensed with.

Some of the London Electrical Power Companies

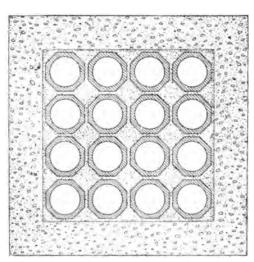


FIG. 113.—Built-up conduit.

have their conduits built up of single ducts of circular interior and octagonal exterior cross-section, as shown in Figure 113, the conduits being built up in blocks of any desired number and the whole encased in concrete.

An advantage claimed for the draw-in system is that when once the conduit has been

laid, repairs and additions to the system can be made without excavation, whereas with cables laid on the solid system, unless sufficient cables for all future requirements are laid down at first, it is necessary to open the whole length of the road in order to lay an additional cable. The best practice is to use the draw-in system for feeder cables which go direct from the generating station to the feeding points, and the solid system for distribution.

Conduits are liable to become charged with explosive gases caused either by leakage from gas mains in the vicinity, or by leaks from the cables themselves, the insulation of which when heated gives off explosive gases. It is therefore necessary to provide efficient ventilation. The draw-in boxes as well as the conduits themselves should be effectually drained. These desiderata are generally accomplished by connecting a drain pipe D and ventilator V to each draw-in box, as

shown in Figure 112.

Direct System.—Armoured cables are generally laid directly in the ground, and have no further protection than that afforded by their own armouring. This method of laying is the least expensive, and in certain soils, which are free from sulphur, has been attended with great success. The cables are laid at a depth of from 60 to 90 centimetres, and each individual cable should be surrounded with at least 7 centimetres of soft earth well pounded. In many cases these armoured cables are left entirely unprotected; in others a line of bricks or lengths of creosoted boards are laid directly over the cable before reinstatement of the trenching. This precaution gives an indication, to future excavators, of the presence of the cables.

Cable Joints.—All joints in cables should be made in proper joint boxes, and the jointing performed in such a manner that a thoroughly good electrical contact will be obtained. Figure 114 shows the arrangement of a "straight-through" joint box for single-core cable. The ends of the cables to be jointed are passed, one from each end, into a cast-iron box, which should be designed so as to allow ample space for making the

joint.

In making the joint the insulation is cut away from the cable ends so as to leave 5 to 7 centimetres of the conductor bare. The free end of each cable is set

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into a tight-fitting metal sleeve M, the two ends butting together. In dealing with paper-insulated cables, it is necessary to tin the strands before inserting the ends into the sleeve, as tinning is not a precautionary necessity with this as with other forms of insulating materials, and forms no part of the process of manufacture of paper-insulated cables. The sleeve, which is usually of brass, should be well tinned. The joint is made by heating the sleeve, so that its tinned inner surface adheres to

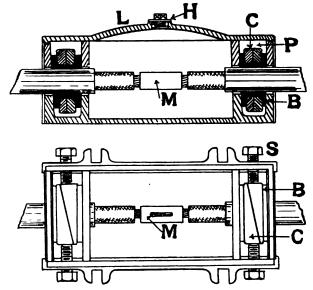


FIG. 114.—Joint box for single-core cable.

the tinned strands, and solder is poured in at a small aperture shown in the figure.

No other flux than resin should be used for soldering. Analyses of the fluids, pastes, and solid compounds made for soldering purposes show that they nearly all contain chloride of zinc in various forms, some of which distinctly promote the fluxing action; and though most of them are suitable for jointing exposed solid conductors, there is a great risk in using them on insulated stranded cables, due to their creeping quickly up the strands, setting up a corrosive action on the conductor, and attacking the di-electric.

After the conductors have been soldered, the interior of the box is filled up solid with bituminous compound. The compound used should be of a high adhesive and insulating quality. Some jointing compounds contract as much as 25 per cent. on cooling, particularly if poured in at too high a temperature. It is therefore best to pour in the compound at the lowest temperature which permits of its flowing uniformly over the box, as too high a temperature may also injure the cable insulation. When full, the box is covered by the cast-iron lid L, and after cooling, the shrinkage of the compound is made up by pouring in more, through the "filling-in" hole H, which is afterwards stopped with a screw-plug.

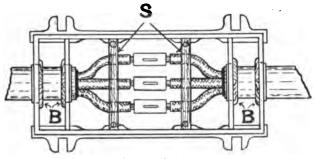


FIG. 115.—Joint box for three-core cable.

In jointing lead-covered cables the electrical continuity of the sheath should be preserved. A good method is to bond the sheath on to the box by lead bonds fitted into pockets placed outside the joint box, as shown in the figure. The bonds B are so designed that by adjusting the set-screws S on either side of the pockets P two wedge-shaped pieces of cast iron C are forced towards one another. This action forces the flanges of the lead bonds, previously put round the cable, against the sides of the pockets, and also causes the lead bond to make good contact with the sheath itself.

Figure 115 illustrates a joint box for a three-core cable. The three cores are separated by wooden spreaders S so as to keep the separate joints at least 5 centimetres apart. The glands of the box are packed with wood

bushes B, treated with preservative compounds, the bushes being of such dimensions as to tightly grip the cable and prevent the movement of the internal fittings. The method of making the joints is similar to that described above.

A joint in a concentric cable is illustrated in Figure 116. The core of the cables is sweated into a brass sleeve S<sub>1</sub>, which is then covered with three or four layers of special cotton tape T treated with resin oil. A split sleeve S<sub>2</sub>, tapered at each end, is next placed over the core joint, and the several strands of the outer conductor are cut to suitable lengths, twisted round the tapered portion of the fitting, bound with No. 18 or 20

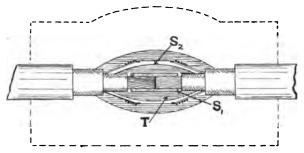


FIG. 116.—Joint in concentric cable.

S.W.G. tinned copper wire, and then efficiently soldered. The second joint is taped as before, and the joint box (the outline only of which is indicated in the figure) filled with compound.

#### AERIAL CONDUCTORS

Aërial lines are constructed by supporting bare conductors on insulators placed on cross arms attached to poles or lattice columns. The poles, either of wood or iron (more often the former), are selected of sufficient strength to carry the weight of the conductors. Aërial conductors carried overground in this manner form the cheapest method of distribution, and have been largely used in America and on the Continent, although, even yet, in Great Britain they have only been adopted to a very limited extent.

Until quite recently hard-drawn copper was the only conductor used, but owing to the development of improved methods of manufacture aluminium is coming into more extended use. Aluminium has a low specific gravity, but its tensile strength and conductivity are also low compared with hard-drawn copper.

·	Aluminium (97.5 per cent. pure).	Copper (hard drawn, 100 per cent. pure).
Specific gravity	2.7	8.9
Specific resistance (microhms	·	-
per centimetre cube) .	2.66	1.6
Tensile strength (in kilo-		
grammes per square		
centimetre)	2000	3500
Coefficient of linear expansion		
per degree C	0.0000231	0.0000168

The difficulty of jointing aluminium wires was an obstacle which delayed the general use of this material as a conductor. Joints in large aluminium wires are now made by inserting the ends to be jointed into an aluminium sleeve, and a positive metal to metal union is effected by hydraulic pressure. The joint thus formed has a shearing stress in excess of that of the conductor itself.

Poles and Cross-Arms.—In districts where there is no liability to the attacks of destructive insects, etc., wooden poles are used: white Canadian cedar or Norwegian fir make the best poles, but very often from transport and other considerations local timber, where available, is requisitioned. The cross-arms for carrying the insulators are generally made of some strong and tough wood, such as oak, and are fastened to the poles by galvanised iron bolts. For ordinary construction the cross-arms have a section of about 8×8 centimetres, and vary in length from 0.75 to 2.5 metres, depending upon the number of conductors to be supported. The height of the poles ranges from 7 to 13 metres, depending upon the nature of the district traversed and the rules enforced for the regulation of supply.

To increase their durability, the poles are usually

creosoted or treated with some similar preservative. In the creosoting process they are placed in iron vats from which the air can be exhausted. The vacuum allows all the sap, etc., to leave the wood, after which steam at a pressure of about 7 kilogrammes per square centimetre is applied so as to swell the wood and open its pores for the reception of the preservative. The wood is again placed in a vacuum, and the water which gained admittance during the steaming process is withdrawn. Finally, preserving compounds, such as crude petroleum oil, are applied at high pressure; this replaces the moisture formerly in the wood. Experience has shown that poles thus treated remain sound for as long as twenty years under normal conditions.

In special cases, as in India and other tropical climates, where wood poles would be quickly destroyed by ants, tubular iron poles or lattice columns are used.

Calculation of Pole Dimensions.—Poles are subject to stresses due—

First—To the weight of the conductors. This weight acts vertically downwards, tends to break the cross-arm at the centre where it is fixed to the pole, and to crush the pole as a column. The weight is liable to be augmented in winter, due to the accumulation of snow.

The length of a cross-arm is determined by the number of conductors to be carried and also the transmission voltage. The simplest construction is illustrated in Figure 117, where a cross-arm, of length 2l, breadth b, and depth d, carries two conductors. These dimensions must be such that they satisfy the equation

$$S = \frac{6Wl}{bd^2}$$

where W is the total weight in kilogrammes resting on one insulator, S the maximum permissible fibre stress of the cross-arm in kilogrammes per square centimetre, and l, b, and d are expressed in centimetres. The permissible values of S for different materials are given in Table XIII.

Second—To unequal tension of the conductors. These are the most important stresses to be dealt with,

and occur (1) where the pole line changes in direction, and (2) at the termination of one or more conductors. Under such conditions the poles are subject to a bending stress equivalent in the first case to the resultant of the tension of all the conductors, pulling the poles sideways. If the value of the tensions on both sides of the insulators and the angle of change of direction be known, the magnitude and direction of the resultant force tending to deflect the pole can be determined from the principle of the parallelogram of forces. The cross-arm of a corner pole is usually set parallel to the direction of the resultant force, so that the latter, except at terminal poles, does not produce a bending stress on the cross-arm.

In the second case of unbalanced tension the bending moment is determined from a knowledge of the algebraic sum of the tensions in all the conductors tending to pull the pole over. If W be the resultant horizontal force in kilogrammes due to the pull of the wires, then the diameter d of the pole at the ground and the height h (Figure 117), both in centimetres, must satisfy the

equation

$$S = \frac{32 \text{ W}h}{\pi d^3}$$

where S is the maximum permissible fibre stress of the pole in kilogrammes per square centimetre as given in Table XIII.

TABLE XIII TENSILE STRENGTH OF TIMBER

Material.						Tensile Strength in Kilogramme per Square Centimetre.	
Ash (white).					•	700 to 1100	
Birch						500 to 1500	
Cedar (Canadia	n)					800	
Deal (Christian	ia)					900	
Elm						400 to 700	
Oak						700	
Pitch pine .						600	
Yellow pine.						350 to 850	
Norwegian fir						550	
_						1	

Third—To wind pressure. The action of the wind against the conductors develops lateral stress, which tends to produce a dangerous vibration of the poles. Standard practice is to select poles of sufficient mechanical strength to withstand a wind pressure of from 1 to 1.5 kilogrammes per square decimetre of surface, depending upon the climatic situation of the line. In calculating the force on a cylindrical surface the exposed area is taken to be two-thirds of the product of the mean diameter and the length of the exposed part. If P denote the wind pressure in kilogrammes per square decimetre, d the diameter of pole at base, and h the height of the pole above the ground, the bending moment

$$= \frac{\frac{2}{3} \times d \times h \times P}{2} = \frac{d \times h \times P}{3}.$$

Staying.—Whenever possible all lateral strains, whether at angles or terminals, should be counteracted by stays. The strain on a stay is always greater than that in the line, and is given by the formula  $P = S \cos \theta$ , where S = the strain in the stay, P the line strain, and  $\theta$  (Fig. 117) the angle the stay makes with the ground. Stays therefore should be of sufficient strength to withstand the strain obtained as above. The stay wires or rods are fixed, at one end, to the pole; the other end is attached to a stay anchor buried in the ground, as illustrated in the figure.

In using the foregoing formulæ it is customary to allow a factor of safety of between 4 and 10, so that the actual tensile stress in kilogrammes per square centimetre varies from 0.1 to 0.25 of the value given in the table.

Pole Construction.—Single poles, of the construction shown in Figure 117, are the more often used, but for withstanding heavy loads the construction illustrated in Figure 118 is well adapted. Two members, having the requisite strength, are set at an angle of about 10°. The feature of this form of construction, due to C. Wade,\* is the method adopted to hold the members at the top. In the form illustrated the two members are scarfed to such an extent

<sup>\*</sup> Journal of Institution of Electrical Engineers, vol. xxxviii. p. 312, May 1907.

as to reduce their diameter by one-third, the length of the scarfing depending upon the angle at which the members are set. They are held together by bolts. At the base the two members are held by a stout piece of timber bolted to each, about 0.6 of a metre from the butt. A centre tie bolt and tubular distance piece are also attached to the two members about 2.5 metres above the ground level.

The result of Wade's tests was that an "A" pole

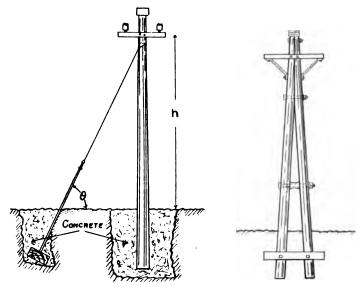


FIG. 117.—Single pole.

FIG. 118.-" A" pole.

would sustain, in a direction across its two members, i.e. at right angles to the line, a load four or five times as great as an unstayed single pole of the same diameter as either of the members. As regards flexibility, some single poles 12 metres long projecting 10 metres above the ground have been tested and deflected from 4 to 4.5 metres before breaking, and those that were released before breaking showed a very small permanent set. On the other hand, an "A" pole would only deflect a few centimetres, and in nearly every instance failed through buckling of the member in compression.

The cross-arms are sometimes tied to the pole by

flat iron stays; this helps to prevent twisting, and in the case of "A" poles also assists in preventing the two

members from parting.

In places where the soil is soft and marshy, or where the stresses brought upon the poles by tension of the wires are excessive, the pole should be erected on a concrete foundation, with 1.5 to 2 metres of the pole butting below the ground.

Insulators for supporting Conductors. —Insulators

used for supporting aërial conductors should be

(1) Made of a hard and non-hygroscopic material.

(2) Sufficiently strong to withstand (a) crushing due to the dead-weight of the conductors, and (b) fracture when subject to lateral strains due to the swaying of the conductor.

(3) So constructed that the length of the leakage paths along the surface of the insulator may be as great

as possible.

Various materials, such as glass, porcelain, ebonite, and stoneware, have been used in the manufacture of insulators, but present forms are generally made only from the first two materials.

Glass is considerably more hygroscopic than porcelain, and, as is well known, has a great affinity for moisture, due to the alkali in it. These properties rapidly lower the insulating value of glass, so that glass insulators are chiefly used in dry climates. Blown glass is superior in every respect for this purpose to that which is cast, but, being more expensive, moulded insul-

ators are generally used.

Vitrified porcelain insulators are invariably used in Britain and on the Continent, and when glazed with a non-alkaline material make very efficient insulators. Stoneware was largely in use at one time, but porcelain, as now made, has better insulating properties. The composition of porcelain used for insulators varies considerably, and consequently also its insulating properties. The material under the glaze in some forms of insulators is very spongy, so that if the glaze cracks the porcelain rapidly absorbs moisture and so destroys the insulator.

If the insulators are made of glass or thoroughly vitrified porcelain the leakage current through the material of the insulator is practically negligible so long as it is free from fractures. The main trouble in all insulators is the leakage of current over the surface. This leakage current may assume considerable proportions, but can be reduced to a minimum by suitable The leakage will vary directly as the length of the leakage path over the surface of the insulator, and inversely as the area of the exposed surface. The best insulators, therefore, should have the maximum surface length with the minimum area of exposed surface, so far as is consistent with obtaining the requisite mechanical strength. This is accomplished by designing insulators so that they have a series of deep grooves on their under-side.

There are two distinct types of insulators: first, those in which the entire leakage surface is of glass or porcelain; and second, those in which the leakage over the surface is intercepted by a surface of oil. Of the two, the former is the simplest in construction, and the more often used.

Insulators of the first type are of single-, double-, or triple-cup form; the double-cup insulator is the form invariably used for overhead direct-current lines. Single-cup insulators are seldom if ever used for power transmission lines; multiple-cup forms are preferred because a flaw in one cup does not destroy the whole insulator. Multiple-cup insulators are either made in one piece or a series cemented together.

Figures 119 and 120 illustrate a double- and triplecup insulator of this type. Each insulator is carried by a galvanised-iron bolt (not shown in the figures), the interior B of the insulators being screwed with internal thread to receive the bolt. C indicates the cups forming the insulator, the outer of which is shaped as shown, so that drops of water accumulating at the rim fall away, the inside of the insulator being thus kept perfectly dry. The insulators have an exterior groove at the top, in which the conductor rests, so that the path of any leakage current from the conductor

to the iron bolt is in the direction indicated by the arrows.

An insulator of the second type is illustrated in Figure

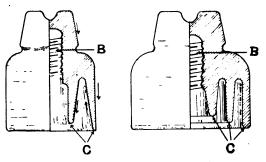


FIG. 119.—Doublecup insulator.

FIG. 120.—Triple-cup insulator.

121. It is of the single-cup form, and the lip of the cup is turned inwards so as to form an annular channel in which is placed some highly insulating non-evaporative oil. The leakage current must take the path indicated

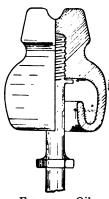


FIG. 121.—Oil insulator.

by the arrows, and has to cross the clean surface of the oil. The insulator is provided exteriorly with a top groove for carrying the conductor, and is fitted with a galvanised-iron bolt for attachment to the cross-arm. The bolts are either screwed or cemented into the insulator. The former is preferable, as the insulator can be more easily removed and replaced in case of breakage. When the bolt is cemented into the insulator it should be provided with a ragged end.

Stresses in Wires. — In erecting conductors on poles the general practice is to adjust the tension to one-fourth that of the breaking strain when the wire is shortened by the coldest weather. When the tension of a wire, suspended between two supports, is such that the sag at the centre of the span is less than one-twentieth of the length, the

curve formed by the wire may be considered a parabola, and the tension of the wire in kilogrammes is given by the formula

$$T = \frac{l^2 w}{8d}$$

where l is the length of the span in metres, d the sag at the centre of the span also in metres, and w the weight of the wire in kilogrammes per metre. Solving for l

$$l = \sqrt{\frac{8aT_m}{70}}$$

where  $T_m$  represents the maximum safe tension of the wire in kilogrammes, *i.e.* the tensile strength in kilogrammes divided by the factor of safety, which is generally taken as 4. The tensile strengths of copper and aluminium are given on page 219. From the above formula it would appear that poles can be spaced farther apart the greater the tensile strength of the wire and permissible sag.

The spacing of the poles depends greatly upon the nature of the transmission line and the district through which the line is constructed. In the case of heavy power lines the poles should be placed close together, so as to distribute the weight of the conductors over a large number of insulators: this is necessary to prevent insulators being crushed. The general practice is to space the poles 24 metres apart for heavy power lines (this is the spacing on the Niagara-Buffalo line), and 30 to 36 metres for ordinary electric lighting and power lines. Wherever the line passes round a curve the poles should be spaced closer together, so that stresses due to unbalanced tension may be reduced.

When the sag is a small fraction of the length of the span the length in metres of the wire is given by

$$L = l + \frac{8d^2}{3l}$$

l and d having the same meanings as in the previous equation.

Overhead conductors should, if possible, be erected during warm weather, so that as the temperature falls the wire contracts, the tension of the wire at the same time increasing. It therefore becomes important to erect the wire with such a sag that at the minimum temperature the safe tensile strength of the wire is not exceeded.

Let t denote the temperature at which the wire is erected, L and d the corresponding length of wire and sag respectively; also let  $L_1$  and  $d_1$  be their values at the minimum temperature  $t_1$ . From the equation

$$T_m = \frac{l^2 w}{8d}$$

the sag  $d_1$  in the wire at the minimum temperature can be calculated; and substituting in the equation

$$L = l + \frac{8d^2}{3l}$$

the corresponding length of wire L<sub>1</sub> can be obtained.

The length of wire L at the time of erection is given by

$$L = L_1\{ I + a(t - t_1) \}$$

where a is the coefficient of linear expansion of the wire. Substituting the value of L in the equation

$$L = l + \frac{8d^2}{3l}$$

the sag d at the time of erection can be calculated. Again, by substituting d in the equation

$$T_m = \frac{l^2 w}{8d}$$

the safe tensile stress may be obtained, and when erecting the wires the tension should be adjusted to this value. The effect of stretching of the wire as the tension increases is generally neglected in practical work, as the error introduced is small and always on the safe side, so that the tension at minimum temperature is even less than that calculated as above.

Example.—An aërial transmission line, in which the poles are spaced 30 metres apart, is constructed of No. 1

S.W.G. copper wire. If the minimum temperature be 5° C., and that when the wires are erected 35° C., determine the tension to which the wires can be adjusted.

No. 1 S.W.G. wire weighs 0.405 kilogrammes per metre. Tensile stress of hard-drawn copper wire = 3500 kilogrammes per square centimetre, so that, allowing for a factor of safety of 4, the safe tension of the wire at minimum temperature

=  $35\infty/4 = 875$  kilogrammes per square centimetre.

Now No. 1 S.W.G. has a cross-sectional area of 0.456 square centimetres, so that the maximum safe tension of the wire =  $T_m = 875 \times 0.456 = 400$  kilogrammes.

The sag at centre of span at 5° C.

$$=d_1 = \frac{l^2w}{8T_{m}} = \frac{30^2 \times 0.405}{8 \times 400} = 0.114$$
 metre.

Length of wire in span at 5° C.

= 
$$L_1 = l + \frac{8d_1^2}{3l} = 30 + \frac{8 \times 0.114^2}{3 \times 30}$$
  
= 30 metres (approximately).

Since the coefficient of linear expansion for copper = 0.0000168 per degree centigrade, the length of wire at 40° C.

= 
$$L = 30 \{1 + 0.0000168(30 - 5)\}$$
  
= 30.016 metres.

Substituting the value of L in the equation

$$L = l + \frac{8a^2}{3l},$$

the sag at the time of erection =  $d = \sqrt{\frac{(L_1 - l)_3 l}{8}} =$ 

$$\sqrt{\frac{0.016 \times 3 \times 30}{8}} = 0.425$$
 metre.

Substituting this value in the equation  $T_m = \frac{l^2 w}{8d}$ , the tension of wire at time of erection has to be adjusted to

$$T_{m} = \frac{30^{2} \times 0.405}{8 \times 0.425} = 105$$
 kilogrammes.

### Insulation Resistance

Measurement of Cable Insulation Resistance by Substitution Method.—The insulation resistance of standard insulated cables ranges from 300 to 6000 megohms per mile, the 6000 megohm grade being used for high-pressure systems of distribution. Before electrical cables are dispatched from the factory their insulation resistance is determined in the following manner:

Referring to Figure 122, the length of cable A to be tested is coiled up and placed in water contained in a zinc tank D, the ends of the cable projecting about 30 centimetres above the water. The insulation at the ends

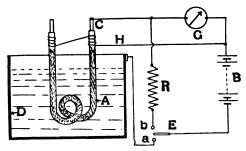


FIG. 122.—Testing the insulation resistance of a cable.

of the cable is cut away so as to leave about 4 or 6 centimetres of bare copper. The end C is connected to one terminal of a galvanometer G, of which the other terminal is connected to the 2-way switch E through a battery or source of E.M.F. B. The contacts a and b of the switch E are respectively connected to the tank D, and a standard high resistance R, which is in turn connected to the galvanometer as shown.

Having made the connections, the insulation resistance of the cable may be determined as follows:

The resistance R is connected in series with the source of E.M.F. B and the galvanometer G by turning the switch K to contact b. The deflection  $d_1$  of the latter is then observed. The switch is then turned to a, thus substituting the cable insulation for the resistance R. The corresponding deflection  $d_2$  of the galvan-

ometer is then observed. Now the deflections  $d_1$  and  $d_2$  are respectively inversely proportional to the resistance R and the insulation resistance of the cable, so that if R be in megohms

Insulation resistance of the cable =  $R \times \frac{d_1}{d_2}$  megohms.

The cable insulation varies inversely as its length, so that, knowing the length of cable tested the insulation resistance can be expressed in megohms per mile.

It is found that the value of the insulation resistance varies with the testing E.M.F., the period of electrification, and the period of immersion in water. Hence the standard test is to immerse the cable in water for 24 hours, and to measure the resistance after one minute's electrification at an E.M.F. of 600 volts.

In order to eliminate errors due to surface leakage at the cable ends, 3 or 4 turns of bare copper wire H are wound round the insulation about 4 centimetres away from the bare ends, and connected to the battery side of the galvanometer as shown. Any leakage current which may then be set up passes from the external surface of the insulation to the battery by way of the guard wire H instead of going through the galvanometer.

Measurement of Insulation Resistance by an Ohmmeter.—For testing the insulation resistance of electric-light wiring, street cables, and electrical machinery an instrument is necessary which, by the deflection of a pointer over a graduated scale, directly indicates the insulation or other resistance connected to its terminals. Several types of instruments have been devised for this purpose, but the one designed by Sidney Evershed is probably the most widely used.

The principle and construction of Evershed's ohmmeter, or "Megger," as it is sometimes called, is illustrated in Figures 123 and 124. It consists of a moving-coil instrument combined in one box with a hand-driven direct-current generator to provide current for the test. The armature G of the generator, wound for a pressure of from 100 to 1000 volts, is centred in bearings between the poles N<sub>1</sub> and S<sub>1</sub> of the permanent

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magnets MM, and coupled through gearing to the driving handle.

The magnets MM are magnetised to a strength of

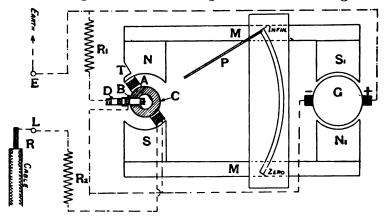


FIG. 123.—Evershed's ohmmeter.

about 2000 lines per square centimetre, and to those ends remote from  $N_1$  and  $S_1$  are fitted the poles N and S. Between the latter is fixed a specially shaped iron

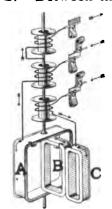


FIG. 124.—Moving system of Evershed's ohmmeter.

core C. The magnetic flux passes from N to S by way of C, and thereby sets up a uniform magnetic field in the airgaps under the poles. Pivoted on the same spindle, between N and S, are two coils, A and B, fixed at an angle of about 70 degrees with each other. The coil A is wound so as to embrace the core C, while B extends from the centre to one side of C, as shown. To the spindle supporting the coils is attached the pointer P, which moves over a scale graduated from zero to infinity.

The coil B, known as the "pressure coil," is connected in series with a high resistance R<sub>1</sub> across the generator ter-

minals. The "current coil" A is connected, in series with the resistance R<sub>2</sub>, between the terminals L and the negative brush of the generator, the positive of the latter being connected to the terminal E.

The resistance R to be measured is connected between the terminals E and L, and in testing the insulation resistance between the conductor of a cable and earth, terminals L and E are respectively connected to the conductor and to earth,—a water pipe forms a good connection with earth.

When the resistance R is "infinite" no current flows in the series coil, and the pressure coil will take up the position shown in Figure 123, the pointer P at the same time indicating "infinity." When a current does flow through the series coil, the latter will have an opposing turning moment, so that the moving system rotates clockwise. The angle made with the infinity position is a function of the resistance in circuit with the series coil and independent of the generator voltage. The instrument is made dead-beat by winding the coil A on an aluminium frame.

In order to protect the instrument from the influence of stray magnetic fields, a compensating coil D is fixed to the outside of the pressure coil. The coil D is connected in series with the former, and wound in the opposite direction. The coils B and D therefore form an astatic electro-magnet which will be uninfluenced by stray magnetic fields. The pole piece N is at one tip cut away to form a tooth T, and when the moving system is in a position corresponding to zero insulation resistance the compensating coil lies over T.

It is essential that there be no controlling force, otherwise the law of the instrument will be altered, and in order to effect this phosphor-bronze wire of .o1 millimetre diameter is used for leading the current into and out of the moving coils. Such fine wire is very springy, and to prevent any danger of its becoming entangled with the instrument in transport, it is wound round the comparatively large aluminium drums shown in Figure 124, the latter indicating the arrangement of the moving system.

Instruments working on the above principles are constructed to measure resistances up to 2000 megohms.

### CHAPTER VIII

## THE DYNAMO—ARMATURE, COMMUTATOR, AND BRUSH GEAR

### PRINCIPLE OF THE DYNAMO

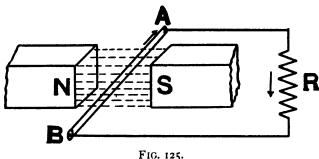
The construction of the dynamo is based upon the principle of electro-magnetic induction discovered by Faraday. This principle affirms that, when a conductor is moved so as to cut magnetic lines of force, an electro-motive force is induced in the conductor, which, if it form part of a closed circuit, will cause a current to flow. The direction in which the current will flow will depend upon the direction of motion of the conductor, and the value of the induced E.M.F. will be proportional to the rate at which the conductor cuts the lines of force.

In a commercial machine the electrical conductors are fixed around the periphery of an iron drum, and so connected that when the drum is centred in bearings between the poles of an electro-magnet and mechanically rotated, an E.M.F. is induced in the conductors as they cut the lines of force, and if the conductors form part of a closed circuit a current flows. A dynamo is thus a transformer of energy. The rotary part carrying the conductors is called the *armature*, and the stationary electro-magnet the *field magnet*.

The simplest mode of generating an E.M.F. by electro-magnetic induction is illustrated in Figure 125. The conductor AB is placed in a magnetic field between the poles N and S, and is connected to the external circuit R. If AB be moved in an upward direction, an E.M.F. will be induced in it and current will flow

through the external circuit in the direction indicated by the arrow; but when the direction of motion is reversed, the current will flow through R in the opposite direction.

Next consider a rectangular loop of wire revolving



in a magnetic field about an axis perpendicular to the lines of force. The arrangement is shown in Figure 126, where the simple armature consists of two con-

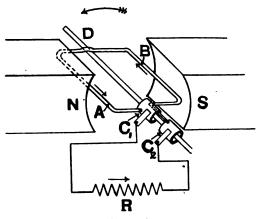


FIG. 126.

ductors A and B supported on the spindle D, and centred between the poles N and S of an electromagnet. The ends of the loop are electrically connected to two insulated metal slip rings C<sub>1</sub> and C<sub>2</sub>, and a circuit is completed through the external circuit R by means of metal contacts or brushes bearing on the

rings. When the armature is rotated uniformly in the direction indicated, the sides A and B of the loop have E.M.Fs. induced in them as they cut through the magnetic field.

It is of importance to remember that the E.M.F. is only induced in that portion of the conductor which lies parallel to the axis of rotation and is under the influence of the magnetic field. Any portion of an armature conductor which is the seat of an induced E.M.F., will hereafter be referred to as an *inductor*.

Referring to Figure 126, at the instant the loop AB is in a vertical plane, the inductors A and B are moving parallel to the lines of force (i.e. no lines of force are cut), so that the value of the induced E.M.F. will be At the instant the loop has been rotated through 90 degrees, A and B will be passing under the centres of the N and S poles respectively, and since they cut the lines of force at right angles, the maximum E.M.F. will be Now the inductors are induced in each inductor. moving across the field in opposite directions inductor B moves up while A moves down), so that the induced E.M.Fs. on each side of the loop will be in opposite directions, as shown by the arrows alongside of the inductors; but A and B are so connected that the E.M.Fs. are cumulative, therefore the E.M.F. across the slip rings will be twice that set up in each inductor, and a current flows through the circuit R from C<sub>1</sub> to C<sub>2</sub>. Continuing the rotation, by the time the loop has moved through 180 degrees, the E.M.F. will again be zero, and at the instant the inductors A and B are passing under the centres of the S and N poles respectively, the induced E.M.F. will again be a maximum, but its direction in each inductor will have reversed, so that the current flows through the external circuit R from C<sub>2</sub> to C<sub>1</sub>, i.e. the direction of the current leaving the armature is also reversed.

During each complete revolution the current reversesin direction twice, and if the inductors rotate with a uniform velocity V in a uniform magnetic field of strength M, the value of the induced E.M.F. at any instant will be equal to the product of the field strength M, the number of inductors C in series, and the vertical component of the velocity at that instant. The latter is equal to V Sin  $\theta$ , where  $\theta$  is the angle through which the coil has rotated from the vertical plane. The electromotive force induced in a coil at any instant will therefore be given by the expression:

 $e = M.C.V Sin \theta C.G.S. units.$ 

In this equation, when  $Sin \theta = 1$ , the value of e is a maximum and equal to MCV, so that denoting this value by  $E_{max}$ , the instantaneous value of the induced E.M.F. is given by  $e = E_{max}$  Sin  $\theta$ . That is the curve connecting E.M.F., and angular displacement of the loop is a simple sine curve, as shown in Figure 127. The change in the direction of the E.M.F. which

occurs when the inductors begin to cut the lines of force in the opposite direction, is shown by the curve crossing the zero line. The current maintained by such an E.M.F. is known as an alternating current, and the

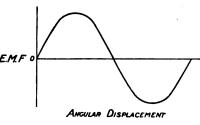
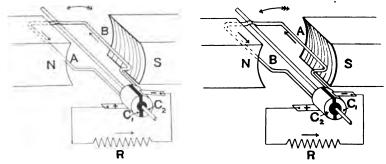


FIG. 127.

arrangement shown for producing it as a simple alternating current generator or alternator.

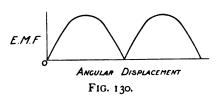
The Commutator.—Next suppose the slip rings to be removed and the ends of the loop AB connected one to each half C<sub>1</sub> and C<sub>2</sub> of a split metal ring as shown in Figure 128, the two halves of the ring being insulated from each other. Such an arrangement constitutes a simple commutator having two segments C<sub>1</sub> and C<sub>2</sub>. If the brushes are so placed that at the instant the induced E.M.F. is zero they slide across from one segment to the other, the current, while reversed in the loop, flows through the external circuit in the same direction. That this is the case will be clear from Figures 128 and 129. In Figure 128 the inductors A and B are under an N and S pole respectively, and the current flows from segment C<sub>1</sub> by way of the positive brush, external circuit R, and

negative brush to the segment C<sub>2</sub>, where it enters the loop and completes its circuit through inductors B and A, as shown by the arrows alongside the latter. When the loop has been rotated so that the inductors A and B are under an S and N pole respectively, the direction of the induced E.M.F. is as shown in Figure 129.



FIGS. 128, 129.—Principle of commutator.

The current now flows through A and B in the reverse direction, but as the segments  $C_1$  and  $C_2$  have also moved through 180 degrees, the current will flow from  $C_2$  to  $C_1$  through the external circuit in the same direction as before. The current in the external circuit is therefore uni-directional, although its numerical value



fluctuates from zero to a maximum as the loop moves from a position midway between the poles to a position under the centre of the poles.

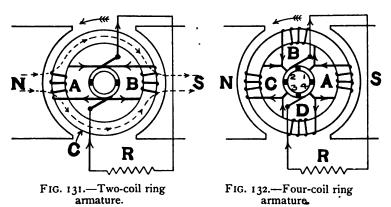
The variation of the

E.M.F. across the brushes with the angular displacement of the loop will be as shown in Figure 130. The arrangement of inductors shown in Figure 129 sends a uni-directional or direct current through the external circuit, and is therefore known as a direct current generator, or simply a dynamo.

The method by which the E.M.F. generated by a dynamo is increased, and the fluctuations eliminated, will now be explained. In a ring armature the winding

consists of a number of convolutions of wire on an iron ring mounted on a shaft. Figure 131 illustrates the principle of an armature of this type. The coils A and B are wound on opposite sides of the iron ring C and connected in parallel at the two commutator segments. The lines of force emanating from the N pole, cross the air-gaps, pass through the iron ring, and enter the S pole in the manner indicated in the figure.

As the armature rotates only those parts of a coil which lie along the outer surface of the core cut the lines of force, so that the sides of the coils passing

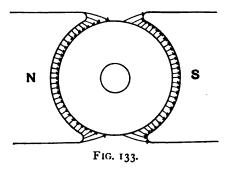


along the inner surface of the ring are inactive, serving only to connect the inductor portions of the coils in series. Suppose the armature to be rotating in the direction indicated, then an E.M.F. will be induced in each coil, causing a current to flow through the external circuit R in the direction shown by the arrow-heads. Both coils have the same number of convolutions, and being connected in parallel, each coil carries one-half of the total current entering the external circuit: that this is so will be apparent by tracing out the path taken by the current from the negative to the positive brush.

A ring armature wound with four coils A, B, C, and D, each placed 90 degrees apart and connected to four commutator segments, is shown in Figure 132. Between

the negative and positive brushes there are two circuits as before, but each circuit consists of two coils connected in series. On entering the armature at the negative brush the current divides, one-half flowing through coil A to segment No. 1, and thence to the positive brush by way of coil B and segment No. 2, where it is rejoined by the other half of the current flowing through the coils D and C.

In Figure 129 the lines of force pass horizontally from pole face to pole face, with the result that the E.M.F. induced in the inductors is a sine function. By the insertion of an iron core (Figures 131 and 132), the distribution of the magnetic flux as cut by the inductors is considerably altered. Referring to Figure 133, the

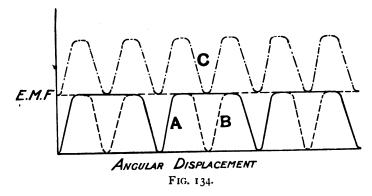


lines of force now pass through the air-gap and enter or leave the core much more radially, and are distributed almost uniformly over the arc embraced by the pole face, the result being that the curve of instantaneous E.M.F. is considerably altered

from that of a sine wave. The actual form of the E.M.F. wave is shown by the curves A and B (Figure 134). The curves have a flat top caused by the inductors cutting the uniform magnetic field under the pole face, and the existence of a weak field or fringe at the edge of the pole face causes the curve to pass gradually from a maximum value to zero.

The instantaneous values of the total E.M.F. in a circuit consisting of two or more coils in series will be equal to the sum of the instantaneous E.M.Fs. induced in each coil. Taking the circuit formed by the coils A and B (Figure 132), the curves A and B in Figure 134 represent the variation in value of the E.M.F. in the two coils respectively. It will be observed that at the instant one E.M.F. is zero the other is at a maximum, the coils being displaced relative to each other by 90 degrees.

On adding the ordinates of the two curves together a third curve C is obtained, which shows the variation in E.M.F. across the brushes with the angular displacement of the armature. From this curve it will be seen that (1) the maximum E.M.F. of the two coils in series is greater than that of a single coil, and (2) the percentage fluctuations of the combined E.M.Fs. are very much less than those of each coil when acting separately. If the fluctuation on either side of the mean value in the case of a single coil be taken as 100 per cent., then the



fluctuations due to the two coils in series are reduced to

about 30 per cent.

The fluctuations of the E.M.F. across the brushes can be still further reduced by winding the armature with more coils and providing a correspondingly increased number of commutator segments. An armature having about 30 coils in series per circuit generates an E.M.F. which is practically free from fluctuations. The current set up by such an E.M.F. is sometimes referred to as a continuous current.

The ring armature was first constructed by Gramme, and in the early days of electrical engineering was the only type employed, but having now become obsolete its construction need not be dealt with in further detail here. The armatures of modern dynamos have their windings placed in slots in the periphery of a cylindrical iron core or drum, and are therefore known as drum armatures. The principles of construction discussed in

the next portion of this chapter refer only to armatures of this type.

#### THE ARMATURE

Construction of Core.—As the iron core carrying the windings rotates, it becomes the seat of induced E.M.Fs., and Foucalt or eddy currents are set up. These currents, according to Lenz's law, flow at right angles to the direction of the lines of force and the planes of the direction of rotation. In Figure 135, if A be the armature core supporting the inductors, then as the armature revolves between the poles N and S, the eddy currents induced in the core will take the paths indicated by the arrows.

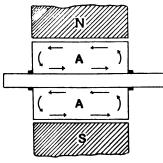


FIG. 135.—Eddy currents in armature core.

Although the induced E.M.F. may be low, yet, owing to the low resistance of the numerous metallic paths, these eddy currents may assume large proportions, with the result that the core becomes heated and energy wasted.

So long as the iron core rotates it will be impossible to prevent the induction of E.M.Fs. in it, but the resulting eddy currents can be

prevented from attaining any appreciable strength by interposing a high resistance in their paths. This is effected by constructing the core of thin discs of iron, each of which is more or less isolated from its neighbour by a thin layer of insulating material, such as paper or varnish. A core built up in this manner is known as a laminated core, and the planes of lamination are at right angles to the axis of rotation and to the inductors.

Although the core be laminated as described, small E.M.Fs. will still be induced in each section, but they will be prevented by the intervening insulation from acting together, so that the eddy currents are reduced. The thinner the laminations the less the quantity of energy wasted.

The material used for the core of armatures is soft

annealed wrought iron or mild steel. The discs are stamped out of sheets the thickness of which ranges between 0.5 and 0.6 millimetre. Up to 1 metre in diameter the discs are cut out in complete rings, each forming one stamping; for larger armatures segments are employed. The thickness of the insulation between the laminations is about 0.05 millimetre, so that, neglecting ventilating ducts, the net length of iron in the core is about 90 per cent. of the gross length.

In armatures of small diameter the sheet-iron stampings are usually threaded directly on the shaft and held in position by a feather running along the length of the

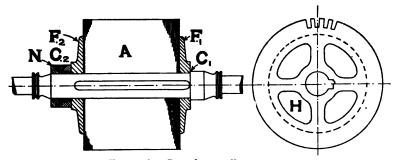


FIG. 136.—Core for small armatures.

core, as shown in Figure 136. At each end of the core are cast-iron end flanges  $F_1$  and  $F_2$ : the flange  $F_1$  is first driven on the shaft and held in position against a collar  $C_1$ . The iron stampings A are then assembled, and after compression the second flange  $F_2$  is fitted on to the shaft and held in position by the screwed collar  $C_2$ , which is prevented from moving by the lock-nut N. Frequently sufficient cross-section of iron is obtained without utilising the full radial depth of the core, and in such cases the laminations are pierced with holes H so as to provide ventilating tunnels for the passage of air through the interior of the armature.

Figure 137 shows the construction of core suitable for armatures of machines up to 200 k.w. The laminations are of sufficient radial depth to give the desired magnetic induction, and are mounted on a cast-iron

spider A, which in turn is keyed to the shaft B. Keyways C are stamped out of the inner periphery of the laminations to fit the arms D which project from the boss of the spider. The latter abuts against a collar E on the shaft and has an end flange  $F_1$ , either cast solid or bolted to it. The laminations after being assembled are compressed by the second end flange  $F_2$ , which is bolted to the spider, thus making the core entirely self-contained. To the end flanges are cast rings G, which

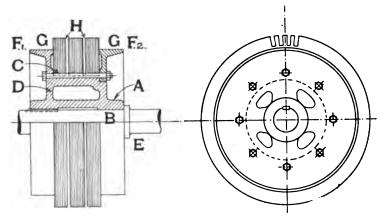
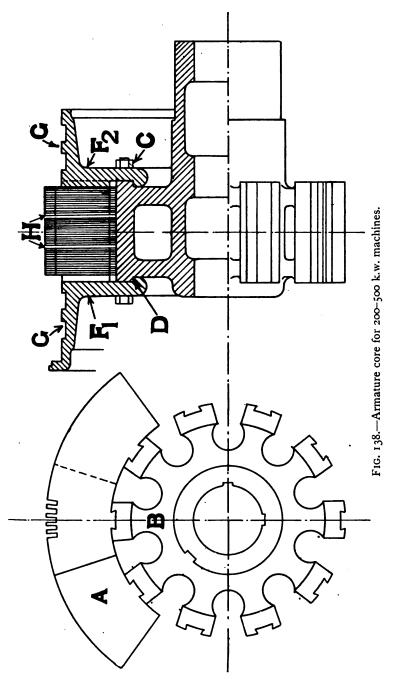


FIG. 137.—Armature core for 100-200 k.w. machines.

serve to support the end connections of the armature winding.

In armatures of still larger diameter it has become the practice, as a matter of convenience, to build the laminations in segments, and the latter are provided with wedge-shaped lugs so that they can be dovetailed to the arms of the spider, thus preventing them from moving radially, due to the action of centrifugal force. The construction of an armature core of this type is shown in Figure 138, where the laminations A are mounted on the arms of the spider B. The segments in any one layer are built up with butt joints, and so arranged that the joints of neighbouring layers do not coincide. The segments are clamped between the end flanges F<sub>1</sub> and F<sub>2</sub> by bolts C passing through holes near the inner edge. The end flanges are extended to form a support for the



end connections of the winding, as shown at G, and are in some cases made in several pieces, each being secured against centrifugal force by engaging beneath a ring on the armature spider as indicated at D.

Figure 139 shows another form of spider suitable for

traction generators of from 700 to 1500 k.w.

In order to provide sufficient ventilation, armatures require to be designed with channels or tunnels to permit of the free passage of air into and through the core. For this purpose the laminations are separated at intervals

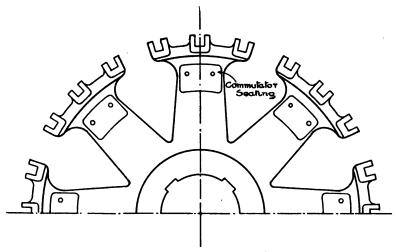


Fig. 139.—Armature spider for 700-1400 k.w. generators.

with distance pieces, so as to form radial air-ducts from the interior to the exterior of the armature core, as shown at H in Figures 137 and 138. In order that the distance pieces may obstruct as little as possible the circulation of the air, they should be made of as skeleton a construction as is consistent with the necessary mechanical strength. The width of the ducts ranges from 10 to 15 millimetres, and the distance between them from 4 to 7 centimetres, depending upon the degree of ventilation required. Figures 140 and 141 illustrate two types of ventilating distance pieces.

In Figure 140 the distance piece consists of small metal projections A fitted into slots punched in the plate

B and riveted over at the back of the plate, thus rendering them quite firm. The plate B usually consists of two or three laminations riveted together. In the type shown in Figure 141 one lamination is used for the space block,

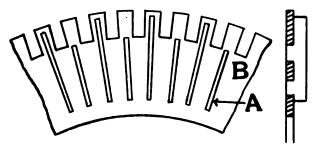


FIG. 140.—Ventilating distance piece.

and small pieces A of the latter are nicked out and turned up at right angles. The first type illustrates the best construction, as it gives support right up to the top of alternate teeth, and so prevents the latter from falling

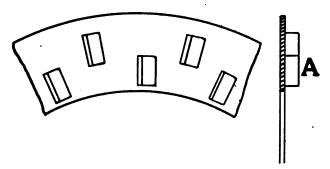


FIG. 141.—Ventilating distance piece.

over and obstructing the passage of air coming from the interior of the armature.

It is desirable that all end flanges, supporting spiders, etc., should as far as possible be kept outside the influence of the magnetic field, otherwise they may become the seat of eddy currents: also all bolts passing through the body of the armature laminations must be either so placed that they cut as few lines of force as possible, or be insulated from the core by fibre tubes, so as to obstruct

the paths that eddy currents generated in them would follow.

Pull on Inductors.—Of the total power expended in driving a dynamo, from 80 to 96 per cent. is absorbed in overcoming the magnetic pull which the inductors experience as they move through the magnetic field. The driving power is transmitted from the shaft through the spider and core to the inductors, where the actual conversion of the mechanical energy supplied to the dynamo into electrical energy takes place.

The force acting on one inductor

= B × i dynes per centimetre of length, where— B = induction density of the field in which the inductor is placed

*i*= the current in C.G.S. units flowing in the inductor. If the inductor be *l* centimetres in length and carry a current of C ampères, then the force acting on each inductor and opposing the direction of rotation of the armature is expressed by

F = B . 
$$\frac{C}{10}$$
 .  $l$  .  $\frac{1}{981}$  grammes  
=  $\frac{B \cdot C \cdot l}{981 \times 10^4}$  kilogrammes.

For example, suppose an inductor having a length of 40 centimetres and carrying a current of 100 ampères is rotated in a magnetic field having an induction density of 8000 lines per square centimetre. The force or pull on the inductor

$$= \frac{8000 \times 100 \times 40}{981 \times 10^4} = 3.2 \text{ kilogrammes.}$$

It will be clear from this example that the inductors of an armature must be supported on the core in such a manner that they are effectively driven through the magnetic field without any possibility of their slipping round the surface of the core. This is, in most cases, effected by the use of slotted armatures, as originally suggested by Pacinotti. The laminations of such armatures have a number of projecting teeth stamped out round the periphery, so that when assembled the

surface of the armature has a series of grooves or slots running from end to end, as shown in Figures 136 to 138. The inductors are well protected with insulation and tightly fitted into the slots, one slot holding two or more inductors.

In some armatures the inductors are placed around the periphery of a smooth core, as shown in Figure 142. In such constructions shallow grooves are milled out longitudinally along the core B, and into these hard wood or fibre strips C are driven, the tops of which are flush with the inductors. These strips or *drivers* thus oppose any slip of the inductors relative to the core,

and are placed at intervals of from 8 to 10 centimetres along the circumference. Their width should be sufficient to withstand the pull of the inductors acting on any one strip, but at the same time they should not be too wide, otherwise the symmetry of

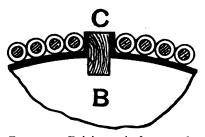


FIG. 142.—Driving strip for smooth core armature.

spacing of the inductors is interfered with unnecessarily.

E.M.F. Equation for a Dynamo.—As already stated, the electromotive force induced in an armature inductor is directly proportional to the rate of cutting lines of force. In Chapter I. the absolute unit of pressure was defined as that generated in an inductor cutting one line of force per second. From this definition the E.M.F generated in the armature of a dynamo can be expressed in terms of the armature winding, armature speed, number of poles, and the flux per pole cut by the armature inductors. Consider a two-pole dynamo: let M denote the flux per pole entering the armature, then the E.M.F. generated in each inductor when the armature makes one revolution per second = 2 M, C.G.S. units, the constant 2 being introduced since each inductor cuts the total flux twice in one revolution. Further, let R denote the speed of the armature in revolutions per minute (R.P.M.) and C<sub>1</sub> the number of inductors in series per circuit, then the E.M.F. generated in each circuit =  $2 \text{ M} \times \frac{R}{60} \times C_1$  C.G.S. units.

Since two inductors constitute one armature turn,  $C_1 = 2$  T, where T is the number of turns in series per circuit; so that for a two-pole dynamo the E.M.F. in volts is expressed by

 $E = 2 \text{ M} \cdot \frac{R}{60} \cdot 2 \text{ T} \cdot 10^{-8}$ .

This formula holds good only for 2-pole machines: but if p denote the number of pairs of field poles, the voltage of any direct-current dynamo is expressed by

$$E = 2 M \cdot \frac{R}{60} \cdot p \cdot 2 T \cdot 10^{-8}$$
.

 $\frac{R}{60}$ . \$\notation\$ may conveniently be considered as one term, since it represents the number of magnetic cycles through which the armature iron passes per second. The letter N is used to denote the quantity  $\frac{R}{60}$ . The general equation for obtaining the voltage of dynamos is

$$E \text{ (volts)} = 4 T N M 10^{-8}$$
.

This formula, if correctly interpreted, is applicable to any type of dynamo. It is important to remember that *T* is the number of turns in series per circuit, and M is not the flux generated in one pole, but that which, after deducting leakage, finally becomes linked with the armature inductors.

Example.—The armature of an 8-pole dynamo is required to generate 550 volts when revolving at a speed of 240 R.P.M. Calculate the magnetic flux M per pole passing through the armature if the latter has 272 slots and 6 inductors per slot. The armature winding has 8 circuits in parallel.

The total number of armature inductors =  $272 \times 6$  = 1632.

Total number of armature turns =  $\frac{1632}{2}$  = 816.

The number of turns per circuit  $(T) = \frac{816}{8} = 102$ .

The number of magnetic cycles per second (N) = R

$$\frac{R \cdot p}{60} = \frac{240 \times 4}{60} = 16.$$

From the E.M.F. equation

$$M = \frac{E \times 10^8}{4 \times T \times N} = \frac{550 \times 10^8}{4 \times 102 \times 16} = 8,400,000 \text{ lines}$$

= 8.4 megalines, where 1 megaline equals 10<sup>6</sup> lines.

Windings.—The number of inductors having been determined by the preceding formula, it remains to consider the different methods of connecting the ends of the inductors of an armature so as to form a symmetrical closed coil winding. According to the method of inter-connecting the inductors windings may be divided into

- 1. Two-circuit or wave-winding.
- 2. Multiple-circuit or lap-winding.

Wave-windings are employed in machines of low output, and are also well adapted for high-speed machines of intermediate output. A characteristic of this type of winding is that there are only two circuits through the armature from positive to negative brushes, independent of the number of pairs of poles or sets of brushes. Each of the two circuits supplies one-half of the total current output.

Multiple-circuit windings are adopted for machines of large output, and are also preferable for slow-speed machines of intermediate output. This type of winding differs from the wave-winding, in that there are as many circuits from positive to negative brushes as the machine has poles: each circuit being in parallel, the current will divide equally between them. Thus in a 6-pole machine giving 600 ampères with a multiple-circuit winding, each circuit will carry 100 ampères.

The inductors of an armature may be considered as arranged in a number of groups or *elements* distributed at equal distances round the periphery of the core, as

shown by the numbered circles in Figures 143 and 144, each circle representing one element. A coil or winding unit is formed by connecting two suitable elements together, and will herein be referred to as that part of the winding which terminates in two commutator segments. In practice an armature coil consists of one to six turns, but so far as the foregoing diagrams are concerned it is immaterial as to how many turns there are in a coil. Each coil will therefore for simplicity be considered as having one turn only, and each side of

the coil considered as a single inductor.

The pitch or spacing of an armature winding is the term which denotes the distance between two separate elements connected together. It is usual to express the pitch of a winding in terms of the number of elements or inductors passed over. For instance, in Figure 143 the inductors are numbered consecutively round the armature, and at the rear end of the winding inductor No. 1 is joined to inductor No. 6, thus forming a loop; the pitch of the winding is therefore 5. At the front or commutator end inductor No. 6 is joined to inductor No. 11, so that the pitch is again 5. Sometimes the front and rear pitches differ by an even number, in which case if  $y_{\rm F}$  and  $y_{\rm R}$  denote the front and rear pitches respectively, the mean pitch is expressed by  $y = \frac{y_F + y_R}{2}$ .

In the case of drum windings all connections from inductor to inductor must be made at the front and rear ends exclusively. It therefore follows that the inductors forming the sides of any one turn must be situated in fields of opposite polarity, so that the electromotive forces generated in the inductors constituting a turn shall act in the same direction round the turn. The width of a, coil or winding element should therefore be approximately equal to the polar pitch, i.e. the distance between Both front and the centres of two consecutive poles. rear pitches will be approximately equal to  $\frac{C}{2p}$ , where C is the total number of inductors and 20 the number of

poles: but the exact values of  $y_F$  and  $y_R$  must be such that the winding closes on itself, and that starting from any one inductor and tracing through the successive inductors in the order of the winding, each inductor should be traversed once, and once only, before the original inductor is reached. Such a winding is said to be *re-entrant*.

Two-Circuit or Wave-Winding.—Let C denote the number of inductors forming a winding, and 2p the number of poles, then the mean pitch is given by

$$y = \frac{C \pm 2}{2p}.$$

Owing to the mechanical arrangement of the end connections both pitches must be odd numbers, so that if y, determined by the above equation, be also an odd number, the front and rear pitches are both made equal to the mean pitch, *i.e.*  $y = y_F = y_R$ . On the other hand, should y be an even number, the front pitch requires to be less or greater than the mean pitch by I, according as the rear pitch is greater or less than the mean pitch by I.

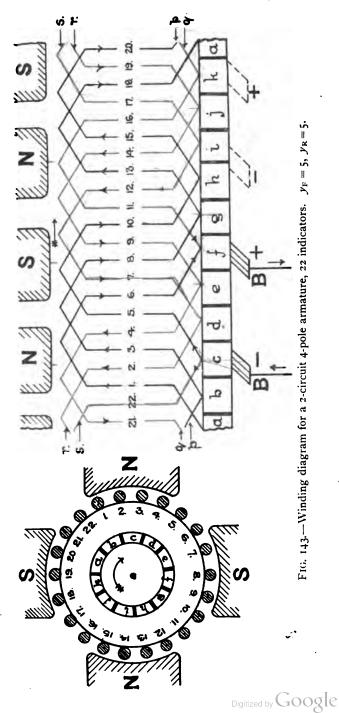
i.e. 
$$y_F = y \pm I$$
  
and  $y_R = y \mp I$ 

As a demonstration of the first case the winding diagram of a 4-pole armature having 22 inductors will be examined. Figure 143 shows the position of the poles and indicates how the 22 inductors are arranged around the armature. To make clear the method of interconnecting the inductors, the winding is represented as being laid out flat, and the eleven commutator segments indicated by the letters a to k.

The mean pitch of the winding  $(y) = \frac{22 \pm 2}{4} = 5$  or 6.

Taking y = 5, then  $y_F = y_R = 5$ .

Starting from commutator segment a, connection is made to the front end of inductor No. 1, and the rear end of the same inductor is connected to an inductor 5 in advance, i.e. to No. 6. Since the front pitch is also 5, the commutator end of inductors Nos. 6 and 11 are connected together at segment f. Similarly the winding is completed as follows:



Rear end.				Front end.				
11 cc	onnected to	16	and	16	connected	to 21 at	segment	ŀ
21	,,	4	,,	4	,,	9	"	e
9	,,	14	,,	14	,,	19	"	j
19	"	2	,,	2	,,	7	**	d
7	,,	12	,,	12	,,	17	,,	i
17	,,	22	,,	22	,,	5	,,	C
5	,,	10	,,	10	٠,	15	,,	h
15	"	20	,,	20	••	3	,,	b
3	,,	8	,,	8	19	13	,,	g
13	,,	18	11	18	••	I	"	a

The winding thus forms a closed circuit. By tracing any two consecutive winding units it will be observed that they have a wavy or zigzag appearance, hence the name wave-winding.

The direction of the induced E.M.F. in each inductor as it passes through its respective field is indicated by the arrows. The current in the inductors under an N pole flows from front to rear, and in the opposite direction when under an S pole.

The positions on the commutator where it is necessary to place collecting brushes can be ascertained from the winding diagram. A positive brush should be placed at any segment of the commutator where two arrow-heads meet; and a negative brush should be placed at those segments where two arrow-heads go in opposite directions through the winding. Thus in Figure 143 the positive and negative brushes B+ and B- are placed 90 degrees apart, and make contact with segments f and c respectively.

By tracing through the winding from the negative to the positive brush, it will be found that the two paths through the armature are along the inductors and in the following order:

$$B = \left\{ \begin{matrix} \text{(Black circuit)} & . & 5 & 10 & 15 & 20 & 3 & 8 & 13 & 18 & 1 & 6 \\ \text{(Red circuit)} & . & 22 & 17 & 12 & 7 & 2 & 19 & 14 & 9 & 4 & 21 & 16 & 11 \end{matrix} \right\} B +$$

With wave-wound armatures only two sets of brushes are necessary so far as the collection of the current is concerned; but in order to reduce the size of the commutator it is usual in machines greater than 15 k.w. to use as many sets of brushes as there are poles.

The fact that two sets of brushes are sufficient for a wave-winding will be evident from Figure 143. there be four sets of brushes arranged as shown. positive brushes, being in contact with segments f and k, are electrically connected through the inductors 11 and Now these two inductors are situated midway between the poles, so that no E.M.F. is induced in them; consequently the above-mentioned inductors simply form a cross-connection between the two positive brushes. Similarly, the two negative brushes are cross-connected by inductors 17 and 22. From this it will be evident that the extra set of brushes in no way alter the distribution of current in the winding, their only function being to increase the brush-contact area with the commutator, and thus assist the first set in collecting current from and delivering current to the commutator segments. When only one set of brushes are used the angle between them will be the same as the angle between any N pole and any S pole. Thus in a 6-pole machine with a wavewinding the positive and negative brushes may be either 60 degrees or 180 degrees apart.

winding the position for degrees apart.

Multiple-Circuit or Lap-Winding.—In a lap-winding the front and rear pitches must both be odd and differ by 2, so that the mean pitch (y) is always an even number, and is made equal to  $\frac{C}{2p}$ , where C and 2p represent the same values as in the formula used for wave-windings. The front and the rear pitches respectively are given by:

 $y_{\rm F} = y \pm 1$   $y_{\rm R} = y \mp 1.$ 

Since the mean pitch  $y\left(=\frac{C}{2p}\right)$  requires to be an even number, the inductors C must be so chosen that this condition is fulfilled. The front and rear pitches are in opposite directions, so that if the latter be considered positive the former is considered negative.

Figure 144 shows the winding development of a 4-pole lap-wound armature having 24 inductors and 12 commutator segments lettered from a to l.

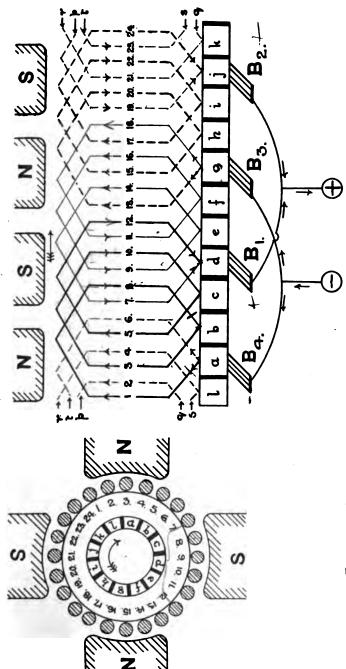


Fig. 144.—Winding diagram for a 4-circuit 4-pole armature, 24 indicators.  $y_F = 5$ ,  $y_R = 7$ .

The mean pitch =  $y = \frac{C}{n} = \frac{24}{4} = 6$ , so that  $y_F = y - 1$  = 5 (-), and  $y_R = y + 1 = 7$  (+).

Inductor No. 1 is connected at the front to commutator segment a, and at the rear to inductor No. 8. Since the front pitch is negative, i.e. in the opposite direction to the rear pitch, and equal to 5, inductor No. 8 is connected to No. 3 at segment b. Similarly, inductor No. 3 is connected to No. 10 at the rear, and No. 10 connected to No. 5 at commutator segment c. The rest of the winding is merely a repetition of the steps described, and after passing over all the inductors the winding re-enters itself at a. It will be observed that in tracing any two consecutive winding units the second unit laps over the first; hence on account of this overlapping the winding is called a lap winding.

The arrow-head on each inductor indicates the direction of the induced E.M.F., and by adopting the same rule as before, positive brushes  $B_1$  and  $B_2$  require to be placed at segments d and j, while negative brushes  $B_3$  and  $B_4$  are placed at segments g and g. Brushes of similar polarity are connected together, and to one or other of the terminals marked + and -.

By tracing through the winding from the negative to the positive terminals, the four paths through the armature will be along the inductors and in the following order:

$$(-) \begin{cases} B_{4} \begin{cases} \begin{cases} \text{black full} \\ \text{line} \end{cases} & \text{i} & 8 & 3 & \text{io} & 5 & 12 \\ \text{red full} \\ \text{line} \end{cases} \end{cases} \begin{cases} 6 & 23 & 4 & 21 & 2 & 19 \end{cases} B_{1} \\ B_{3} \begin{cases} \begin{cases} \text{black dotted} \\ \text{line} \end{cases} & 13 & 20 & 15 & 22 & 17 & 24 \\ \text{red dotted} \\ \text{line} \end{cases} \end{bmatrix} B_{2}$$

Four sets of brushes, *i.e.* two positives and two negatives, are necessary, because a lap-winding has as many circuits as poles. In a lap-wound armature the angle between each set of brushes is the same as the angle between two consecutive poles. For instance, in

the example under consideration there are 4 poles, and the brushes are set 90 degrees apart.

So far as relates to the winding diagrams in Figures 143 and 144, it has been assumed that each winding unit consists of two inductors, *i.e.* constitutes one armature turn. Winding units having 2, 3, or 4 turns are frequently employed for machines generating high voltages, and it will be readily seen that, using the same commutator, the number of inductors can be doubled (and therefore also the E.M.F. of the dynamo doubled) by substituting for each 1-turn winding unit a unit consisting of two turns, *i.e.* four inductors. In Figure 145 is shown the development of a 3-turn

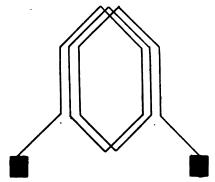


FIG. 145.—Three-turn wavewinding unit.

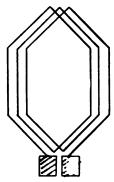


FIG. 146.—Three-turn lap-winding unit.

winding unit (i.e. a winding having three turns per commutator segment) for a wave-winding. In Figure 146 is shown a similar development for a lap-winding having 3 turns per winding unit.

The method of developing such a winding would be similar to those already described, but instead of assigning numbers to individual inductors, numbers would be assigned to the group of inductors forming the sides of the winding units.

Examples of Drum-Windings.—Figures 147 and 148 show typical drum-winding diagrams. In these figures the armature inductors are represented by short radial lines, and the connecting lines inside represent the end connections at the commutator end, and those on the

outside the connections at the rear end. The commutator is placed in the centre, and for the sake of convenience the brushes are drawn inside the commutator. Such diagrams form the most convenient method for the study of drum-windings.

Figure 147 shows a 6-pole wave-winding with 62

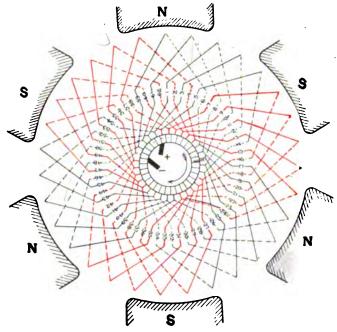


FIG. 147.—Winding diagram for 2-circuit 6-pole armature, 62 inductors.  $y_F = 11$ ,  $y_R = 9$ .

inductors. In this example  $y = \frac{62-2}{6} = 10$ . Since y is even

$$y_F = y + I = II$$
 and  $y_R = y - I = 9$ .

The winding diagram shows two paths in parallel between the brushes.

Figure 148 is an example of a 6-pole lap-winding having 60 inductors. The mean pitch  $(y) = \frac{60}{6} = 10$ ,

so that  $y_F = 10 + 1 = 11$ , and  $y_R = 10 - 1 = 9$ . There are six paths in parallel between the brushes, of which there are therefore six sets.

Multiplex Windings.—Armature windings, so far discussed, have had a single or simplex winding, but they may also be wound with two or more independent

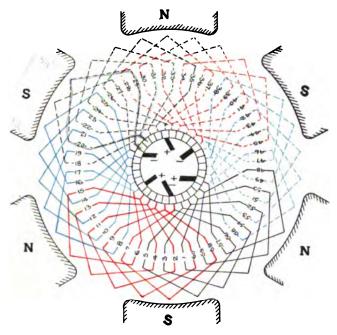


FIG. 148.—Winding diagram for 6-circuit 6-pole armature, 60 inductors.  $y_F = 11$ ,  $y_R = 9$ .

windings. Figure 149 shows a 6-pole lap-wound armature having 60 inductors and two independent windings. Each winding has 30 inductors, and the armature might have been provided with two commutators, say one at each end of the armature. Instead of this, the number of commutator segments is doubled, and the two sets of inductors intercalated with one another.

Referring to the figure, odd-numbered commutator segments belong to one winding, while even-numbered segments belong to the second or red winding. With such a winding the brushes must be of sufficient width to overlap at least 2.5 commutator segments, so as to collect current from the two windings simultaneously. Such a winding is known as a *duplex winding*, and if wave-wound there would be four circuits in parallel between the brushes. The 6-pole duplex lap-winding

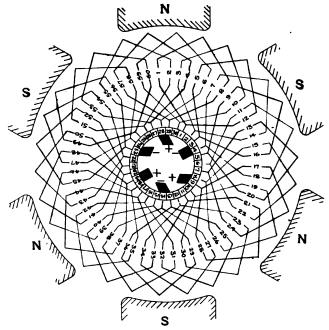


FIG. 149.--Winding diagram for a 6-pole duplex lap-winding, 60 inductors.

shown in the figure has 12 circuits in parallel from negative to positive brushes.

A triplex winding consists of three independent windings with three sets of commutator segments similarly intercalated, the three windings being put in parallel by using brushes of sufficient width to bridge at least 3.5 segments.

Multiplex windings are extensively used on the Continent, but are only used to a limited extent in Britain and America. These windings are of an advantage where large currents are to be collected at the commutator, because, as will be explained later when

discussing commutation, they materially conduce to effecting this operation sparklessly. The formulæ for such windings is necessarily more intricate than that for simplex windings, and their treatment is beyond the intended scope of this book.\*

intended scope of this book.\*

Equalising Connections.—With lap-wound armatures of large output it becomes practically impossible to avoid small differences of pressure between the various circuits that are in parallel, with the result that the current does not divide equally between them. Local currents are thus caused to flow through certain parts of the winding and the conductors which connect brushes of similar polarity. As a result of these local currents the armature becomes excessively heated and serious sparking ensues. Small differences of pressure between the various circuits may be produced by inaccurate centring of the armature or unequal quality of iron in each pole, with the result that the flux entering or leaving certain poles may be less than at others. When the sections of the armature winding pass these poles, they will not generate equal E.M.Fs., with the result that abnormal currents flow in the other sections.

It is now customary in lap-wound armatures of large output to use *equalising connections*. These are of low resistance, and form cross-connections between those parts of the armature circuits which should be at the same potential, so that any local currents due to the above-mentioned differences of pressure are prevented from flowing through the brushes and causing sparking.

The equalising connections are of copper, and generally made in the form of rings fixed on insulated supports to the core of the armature. To be effective, eight or ten independent rings are necessary, and each is in connection with the armature winding, at points spaced out at distances apart equal to twice the polar pitch.

Armature Construction, by Hobart and Ellis (Whittaker & Co.); Design of Dynamos, by S. P. Thompson (E. & F. N. Spon).

<sup>\*</sup> Those wishing further information on this subject are referred to the following books:

In Figure 150 is shown the development of a 6-pole lap-wound armature having 36 inductors, and for simplicity only three equalising rings are shown, the latter, and their connections to the armature winding, being indicated by red lines. Ring No. 1 is connected to the three points A spaced 120 degrees apart, i.e. twice the polar pitch. Each part of the winding embraced between the 120 degrees is divided into three equal parts, as indicated by B and C. The three points marked B should be at the same potential, and are connected to ring No. 2. Similarly the other points marked C are

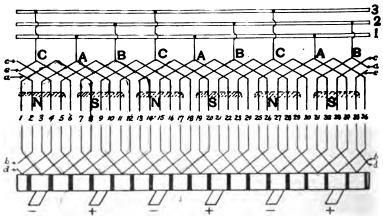


FIG. 150.—Six-pole lap-winding showing connections to equalising rings, 36 inductors.

connected to ring No. 3. In practice each part of the winding embraced between the points A A would be divided into eight or ten equal parts, and the points spaced equi-distantly apart would be connected to eight or ten rings in a similar manner as indicated above.

In the figure, connection is made to the equalising rings at the rear end of the winding, but the more usual practice is to make connection, between the equalising rings and the winding, at commutator segments.

In a wave-winding the inductors belonging to any one circuit are distributed under all the poles, so that equal electromotive forces are induced in each armature circuit, and there is no appreciable tendency to produce unequal distribution of current in the winding.

Arrangement of the Inductors in Slots.—In the preceding winding diagrams it is more convenient to represent the inductors as being spaced equi-distantly around the periphery of the core. In the actual application of such diagrams the winding is generally arranged in two or four layers, with two, four, or more pairs of inductors in each slot, the usual convention being that odd numbers represent upper and even numbers lower inductors. Thus if the inductors in the winding diagram in Figure 144 be arranged four in a slot, the actual location of each inductor will be as shown in Figure 151. The best mechanical design in the arrangement of the end connections is secured by always connecting an upper to a lower inductor. Such an

arrangement makes it necessary that the front and rear pitches, in any class of drumwinding, should be odd numbers. In the latter figure, inductor No. 1

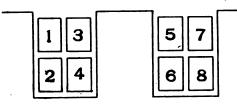


FIG. 151.—Conventional method of numbering armature inductors.

placed in the top of the first slot is connected at the rear to inductor No. 8 in the bottom of the second slot, which in turn is connected at the front to inductor No. 3 in the top of the first slot.

Cross-Section of, and Method of insulating Inductors.

—Inductors and end connections should be of highconductivity annealed copper, prepared electrolytically.

Where the sectional area of each inductor does not exceed
o. 15 square centimetre, solid wire of circular cross-section
may be used. Wire of larger sectional area is difficult
to bend, so that an armature turn requires to be made of
two or more loops connected in parallel, the sum of the
areas of cross-section giving the requisite equivalent
sectional area of a single inductor. By this arrangement
a large amount of slot space is wasted by interstices
between individual wires, so that in order to reduce
the size of slots to a minimum the general practice
is to use inductors of rectangular cross-section when

the area of any one inductor exceeds 0.3 square centimetre.

Wires of circular cross-section are insulated with a double cotton covering when used for low-voltage windings, but for pressures greater than about 230 volts the insulation is in the form of a braided cotton covering. The thickness of insulation ranges from 0.2 to 0.3 millimetre, depending upon the voltage. With inductors of rectangular cross-section the insulation takes the form of a single or double cotton covering with an external covering of braided cotton, the total thickness varying from 0.4 to 0.6 millimetre. In order to enhance the insulation all insulated conductors used for armature

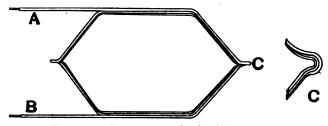


FIG. 152.—Former-wound coil of three turns.

windings are varnished or soaked in shellac and then baked in a hot chamber.

Former-wound Drum Armatures. — When the inductors of an armature consist of wire of circular cross-section former-wound coils are invariably used. These have been adopted for—(1) small machines wherea number of winding units can be conveniently grouped together; and (2) high voltage machines in which a winding unit consists of several turns. The wires forming such a coil are wound together on a former of special shape, and each coil is efficiently insulated before being placed on the armature core. The coils are perfectly symmetrical and interchangeable, and are specially suited for slotted armatures.

The shapes into which the coils are formed are various. Coils of the shape shown in Figure 152 are more frequently used, and windings composed of such coils are technically known as barrel windings. The

coils are wound on a former shaped to the exact dimensions required: the wire at the top of one side leads at the bend C on to the wire at the bottom of the other, thus allowing the ends A and B to project from the tops of each side. For a lap-wound armature both of the ends project from the centre of the widest portion of the coil, while in a wave-winding (Figure 153) the ends are led away in opposite directions for connection to the respective commutator segments.

If there be more than one winding unit per slot, two or more may be wound together. The coil in Figure 153 consists of three winding units. After being formed the coil is wrapped round with special varnished tape,

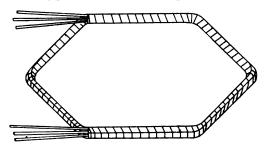


FIG. 153.—Former-wound coil consisting of three winding units.

soaked in shellac and finally baked. Figure 154 shows two former-wound coils in situ.

Bar-wound Drum Armatures.—In this style of winding, a winding unit is invariably a complete loop consisting of two inductors and end connections of rectangular cross-section. Figure 155 shows the shape of such a loop used for a lap-winding. The two sides A and B are bent in different planes, so that the side B can be placed in the bottom of a slot and the side A in the top of another. After shaping, each loop should be well taped, especially at the bend C, and the whole treated with shellac varnish.

Where the inductors are of large sectional area each loop is composed of two separate bars, A and B (Figure 156). After each part is placed in position copper clips C are passed, at the rear, over the bare

ends E. The electrical contact is then completed by soldering.

Insulation of Slots.—The core slots are lined with insulating material before placing the inductors in

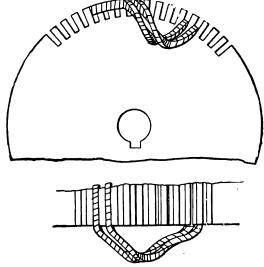


FIG. 154.—Former-wound coils on core.

position. The slot lining requires to be relatively thick, compared with the insulation round each inductor. This is because the core must be insulated from the full

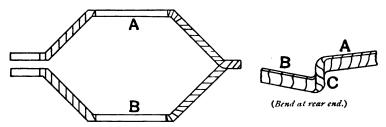


FIG. 155.—Loop for bar-wound armature.

voltage of the machine, while the voltage between any one inductor and its neighbour is only a small fraction of the full voltage.

Press-spahn and micanite are the insulators generally used, and the former requires to be specially treated

to render it moisture-proof. These materials can be obtained in almost any thickness, but it is preferable to use two or three layers of thin material in making up the slot lining to the required thickness. Thus suppose a slot requires to be lined with press-spahn to a thickness

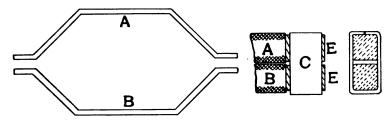
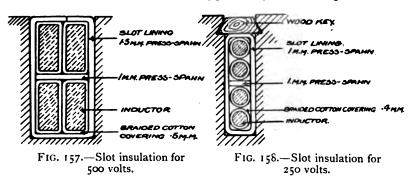


Fig. 156.—Loop for bar-wound armature.

of 0.75 millimetre, then three layers, each 0.25 millimetre thick, would be used, as it is more flexible and has a somewhat higher disruptive strength than single sheets of equivalent thickness. Figures 157 and 158 illustrate two methods, according to the cross-section of the inductors, of insulating the slots.

The sectional area of copper only forms a portion of



the total sectional area of a slot, and the ratio of the former to the latter is known as the *space factor*. The higher the voltage generated the lower the space factor, and in present-day machines it ranges from 0.5 or 0.4 in 550-volt generators to 0.6 or 0.7 in 230-volt and 100-volt generators.

Methods of Retaining the Inductors against Centri-

fugal Force: (1) Low and Medium Speed Machines.— When the winding of an armature has been completed several bands of binding wire require to be wound circumferentially round it to hold the inductors securely in place. The tendency for them to fly out of the slots, due to the action of centrifugal force, is thus counteracted. Non-magnetic steel wire of Nos. 18 to 22 S.W.G. and well tinned, is the material generally used for binding. Referring to Figure 159, a band M of mica strip is first fastened round the armature, and over this the binding wire B is wound under considerable tension to form a belt varying in width from 1 to 3 centimetres. Bands wider

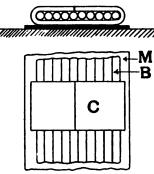


FIG. 159.—Binding wire band.

than this are liable to become heated, due to the eddy cur-Tumuniamum rents induced in them. Along circumference the band, and at intervals of about 20 centimetres, small strips C of sheet copper about 1.5 centimetres wide are in-The ends of the troduced. strips, after the band has been wound, are turned over so as to form clips, as shown in the The convolutions of figure.

the band thus formed are finally soldered together throughout their entire length. Such bands are placed at intervals of about 7 centimetres along the length of the armature.

The end connections of drum armatures are supported on rings or projections cast with the end flanges as shown at G in Figures 137 and 138, and the end bands firmly compress the end connections on to the supporting rings. The latter should be covered with one or two layers of press-spahn held on with tape, thus protecting the insulation on the conductors from mechanical injury.

At places where strips are used the binding wire adds 1.5 to 2.0 millimetres to the radius of the armature, and the mechanical clearance between the armature and the pole face must be reckoned from the overall radius.

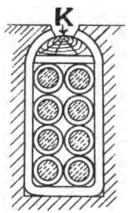
certain constructions, during the building of the core batches of laminations of slightly smaller diameter are interposed at intervals along the core length; these form hollow circumferential grooves of sufficient depth to allow of the binding wire and clips being finished flush.

In armatures of over 1.5 metres diameter the eddy currents which would be induced in the bands necessary to secure the winding would produce excessive heating. In such cases the inductors are held in place by driving beech-wood keys into grooves stamped in the tops of the slots, as shown in Figure 158. This arrangement has the disadvantage that the slots, for the same number and size of inductors, require to be deeper, and the emission of heat from the inductors is obstructed. Except for very large machines, the use of wooden keys should be

avoided; but when used they must be thoroughly dried, and made water-

proof by suitable treatment.

(2) High-Speed Machines.—The construction of armatures for high speeds, such as occur in turbine-driven dynamos, presents certain mechanical difficulties owing to the high stresses set up by the centrifugal forces of the rotating parts. To retain the inductors in position against the action of centrifugal force the best mechanical design would be obtained by placing them in completely closed slots. This, however, is impossible, owing to the increased inductance of the winding being very conducive to sparking.



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being very conducive to sparking. The majority of high-speed dynamos have semi-enclosed slots, as shown in Figure 160, the inductors being held in position by beech-wood keys K.

In some cases, where the speed is not excessive, open slots of the type shown in Figure 158 are sufficient. Where the inductors are held in place by wood-keys, the latter communicate the centrifugal force of the inductors to the teeth, which therefore must be of

sufficient mechanical strength to withstand the conse-

quent stresses.

An armature tooth is subjected to a radial stress due to (1) its own centrifugal force, (2) the centrifugal force of the inductors in any one slot, and (3) the magnetic pull on the tooth.

The centrifugal force of the inductors in any one slot

is expressed by

 $F_1 = 0.0000112 \ M_1 \ R_1 \ N^2 \ kilogrammes$  where

M<sub>1</sub> = Weight, in kilogrammes, of inductors lying in a slot.

 $R_1$  = Mean radius of gyration of mass  $M_1$ .

N =Speed of armature in revolutions per minute.

Similarly, the centrifugal force of a tooth of mass M<sub>2</sub> kilogrammes, and revolving at N revolutions per minute with a mean radius of gyration of R<sub>2</sub> centimetres, is expressed by

 $F_2 = 0.0000112 \text{ M}_2 \text{ R}_2 \text{ N}^2 \text{ kilogrammes.}$ 

If B denote the pole face density in lines per square centimetre, and A the area (in square centimetres) of iron per tooth at armature surface, then the magnetic pull on a tooth is expressed by

$$F_{3} = \frac{B^{2}A}{8\pi \times 981 \times 1000} \text{ kilogrammes}$$
or  $F_{3} \approx B^{2}A \times 4 \times 10^{-8} \text{ kilogrammes}.$ 

The total radial stress on a tooth therefore =  $F = F_1 + F_2 + F_3$  kilogrammes. This force F has to be resisted in tension at the root of the tooth. If  $\alpha$  denote the width of a tooth at root, and  $\ell_n$  the net length of iron parallel to the armature shaft, then the stress at the tooth root is expressed by

$$S = \frac{F}{a \times l_n}$$
 kilogrammes per square centimetre.

The value of S should not exceed 600, this being the average working value for wrought iron in tension, after allowing for a factor of safety of 5.

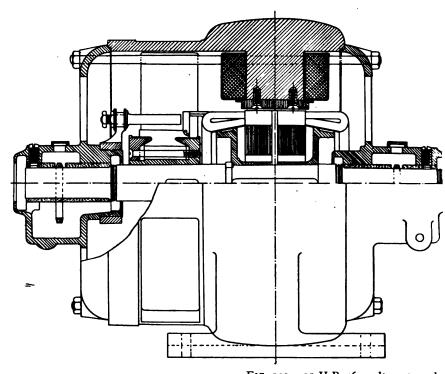
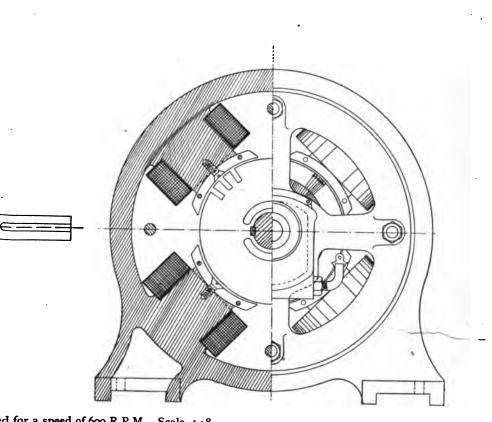


FIG. 232.—15-H.P. 460-volt motor, de



ed for a speed of 600 R.P.M. Scale, 1:8.

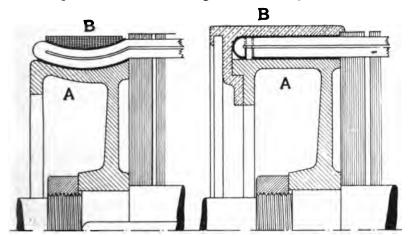
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The end connections of high-speed armatures must also be specially supported against the action of centrifugal force: the two more prevalent methods are shown in Figures 161 and 162. In Figure 161 the end connections are supported on a special shaped end flange A, which is curved on its surface. The surface of the support is insulated with micanite, press-spahn, and tape: the end connections are firmly compressed on it by an end band B of steel wire wound over a thin mica ring, which prevents the binding wire cutting through the



FIGS. 161, 162.—Methods of supporting the armature end connections of turbine-driven dynamos.

insulation of the end connections. The maximum stress on the binding wire occurs at the centre, and the curved surface of the support enables the thickness of the steel band to be greatest at this part, so as to counteract the increased strain.

The second method of supporting the end connections is shown in Figure 162, where they are kept in position by a cylindrical metal end cover B, which is bolted to the supporting flange A. The end connections are insulated from the latter and the end cover by means of micanite and press-spahn. The end covers are either of phosphor-bronze, manganese-bronze, or nickel steel.

The thickness of the end cover B ranges from 2 to 4 centimetres.

If F<sub>1</sub> and F<sub>2</sub> denote the centrifugal forces due to the end connections and covers respectively, then the total internal load acting on one half of the ring =  $\frac{F_1 + F_2}{2}$ . By a well-known law of mechanics, the force tending to burst the covers at two sections on the same diameter

$$= \frac{F_1 + F_2}{2} \times \frac{\text{mean diameter}}{\text{mean semi-circumference}}$$
$$= \frac{F_1 + F_2}{2} \times \frac{2}{\pi} = \frac{F_1 + F_2}{\pi}.$$

If a denote the area of cross-section of the cover and S the stress set up in it, then the moment of resistance Since the latter is equal to  $\frac{F_1 + F_2}{\pi}$ , the value  $= S \times 2a$ . of S is expressed by

 $S = \frac{F_1 + F_2}{2 \pi a}$ 

The thickness of the cover should be such that the value of S does not exceed the safe working stress of the metal. For phosphor-bronze and manganese-bronze the safe working stress is usually taken at about 650 kilogrammes per square centimetre; this allows for a factor of safety of 5.

Example.—From the following data of a 33-k.w. dynamo calculate the number of inductors required for an armature having a wave-winding.

Number of poles

Voltage at terminals = 550 volts. Full load current = 60 ampères.

Magnetic flux in armature

per pole at no load = 3.45 megalines. = 660 R.P.M.Armature speed

 $N = \frac{Rp}{60} = \frac{660 \times 2}{60} = 22.$ 

The turns per circuit are given by
$$T = \frac{E \times 10^8}{4 \cdot N \cdot M} = \frac{550 \times 10^8}{4 \times 22 \times 3.45 \times 10^6} = 180.5.$$

Inductors per circuit =  $180.5 \times 2 = 361$ .

The armature is wave-wound, so that there will be two circuits in parallel, and the total number of armature inductors =  $361 \times 2 = 722$ .

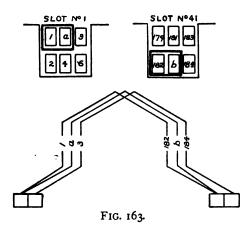
In this particular armature there were 121 slots; 117 containing 6 inductors, and 4 containing 5 inductors, i.e.  $722 = (117 \times 6) + (4 \times 5)$ .

In the four slots containing 5 inductors there would be a vacant space. This could be filled up with wood strips of the same section as the inductors; but the usual practice is to fill the slots with the full number of inductors, and, when making connection to the commutator segments, to join two loops in parallel. The loops thus joined only form two inductors, so far as the winding is concerned. The loop in which the sides are only used to fill up the slots is known as a dummy coil.

In the example under consideration the commutator had 361 segments, so that there is one armature turn per winding unit. The mean pitch =  $\frac{722+2}{4}$  = 181, and since y is odd,  $y_F = y_R = 181$ .

Figure 163 indicates how the inductors are arranged

in the slots. Since  $y_R = 181$ , inductor No. 1, in the top laver of the first slot, is connected at the rear to inductor No. 182 placed in the bottom of the fortyfirst slot. Inductor No. 182 is joined at the commutator end to inductor No. 363 (i.e. 182 + 181) in the top of eighty-first slot.



One dummy coil is that formed by the middle top inductor a in the first slot, and the middle bottom inductor b in the forty-first slot. The loop ab is connected in parallel, at the respective commutator segments, to the loop formed by inductors 1 and 182. The two

left-hand inductors at the top of the first slot are taken together and considered as inductor No. 1. Similarly the two left-hand inductors at the bottom of the forty-first slot are considered as inductor No. 182. This shows clearly the relation of the dummy coil to the rest of the winding.

Example.—As an example of a lap-winding, consider an armature having the following constants:

Number of poles = 4.

Maximum induced E.M.F. = 224 volts.

Magnetic flux in armature per pole = 4.0 megalines.

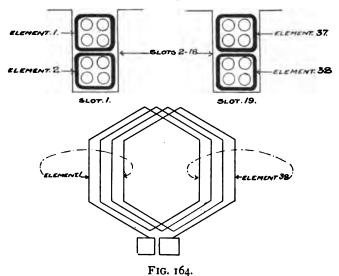
Armature speed = 600 R.P.M.

$$N = \frac{600 \times 2}{60} = 20.$$

Turns per circuit =  $T = \frac{224 \times 10^8}{4 \times 20 \times 4.0 \times 10^6} = 72$ .

Inductors per circuit = 144.

Since the armature is lap-wound there will be four



circuits in parallel, so that the total number of inductors  $= 144 \times 4 = 576$ .

The armature had 72 slots, each containing 8 inductors. There were 72 commutator segments, and

each winding unit consisted of a former-wound coil of 4 turns, i.e. each side or element has 4 inductors, as shown in Figure 164.

For spacing purposes the winding is considered as made up of  $\frac{576}{4}$  = 144 elements; two elements are placed in each slot, odd-numbered elements at top and even-numbered elements at bottom.

The mean pitch =  $\frac{C}{n} = \frac{144}{4} = 36$ , so that  $y_R$  and  $y_F$  are 37 + and 35 - respectively. The arrangement of the inductors in the slots is shown in Figure 164, the inductors belonging to each element being grouped together. Referring to the winding diagram, the front end of element 1 is joined to the first commutator segment, and at the rear end is connected to element 38, since  $y_R = 37$ . Elements 38 and 3 are connected together at the second commutator segment.

## THE COMMUTATOR

Commutators are of various designs, but broadly all are of one of two types, namely, those in which the component parts are held together by insulated metal end rings, or those in which the parts are held together by steel rings shrunk on over them.

To the first type belong those in which the peripheral speed does not exceed 20 metres per second, and in most cases is less than 14. Those of the second type are for high-speed dynamos, such as are direct coupled to steam turbines and have peripheral speeds of from 30 to 40 metres per second. All commutators are built up of segments of high-conductivity, hard-drawn, drop-forged copper of tapered section, insulated from each other by mica, the whole forming a cylindrical structure as shown in Figure 165.

Commutators for Low and Medium Speeds.—The structure thus formed is clamped inside a pair of tapered steel rings A and B, the inner one A of which is cut. Pressure is then applied to force the ring A into B, thus drawing the component parts of the commutator tightly

together. The pressure is in most cases applied when the segments have been heated to a temperature of about 150° C., so as to exclude any superfluous cementing material which may have been used as an adhesive for the mica laminæ in forming the strips to the requisite thickness. When cold, the grooves V are turned out, and into these correspondingly shaped steel clamping rings are fitted, and insulated from the commutator by mica rings shaped to suit. The V-shaped clamping rings are finally drawn up and permanently held by bolts, incidentally double wedging together the parts of

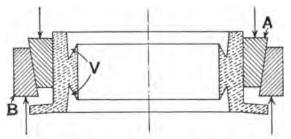


FIG. 165.—Method of building a commutator.

the cylinder forming the commutator, so that on withdrawal of the temporary external clamping rings a selfcontained structure remains.

The mechanical strength of the commutator depends greatly upon the design of the clamping rings, and their dimensions must be such that sufficient resistance is offered to prevent the dislocation of the segments, which might be caused by the contraction and expansion of the commutator with varying temperatures. The diameter of a commutator is generally about 0.75 of the diameter of the armature, and for mechanical reasons the breadth of a segment at the periphery should preferably not be less than 4 millimetres. In order to allow ample wearing depth of copper it is customary to increase the radial depth of the segments by about 100 per cent. over that required for mechanical rigidity and electrical conductivity.

When the segments of a commutator pass under a brush sparking is liable to occur, and almost every insulating material except mica would carbonise and so become conductive. For this reason mica only is employed to insulate adjacent segments. Besides being incombustible mica is non-hygroscopic, so that it does not deteriorate when a commutator is exposed to dampness: it is mechanically strong and can withstand the high compression to which it is subjected when it forms part of a commutator. Further, mica has a remarkably fine and uniform cleavage, and is easily divided up into thin sheets of uniform thickness.

Since there is only a very small pressure (equal to that generated in one coil connected between two segments) between adjacent segments, so far as insulation is concerned, the thickness of the intervening mica strip need only be a small fraction of a millimetre, but

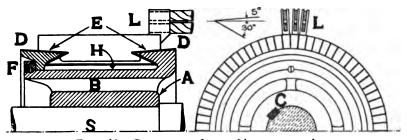


FIG. 166.—Commutator for machines up to 30 k.w.

sparking might then cause small nodules of copper to bridge over the intervening insulation. To prevent this the thickness of the insulation is usually about 0.7 of a millimetre.

It is of great importance that the mica used should wear at approximately the same rate as the copper segments, and for fulfilling this condition green-shaded or amber-coloured flexible Canadian mica is found to be the most suitable. As it is commercially almost impracticable to obtain mica sheets of larger dimensions than about 10 centimetres square, the insulating strips for long commutators are formed of a number of laminæ cemented together with shellac in such a manner that the joints in adjacent segments do not coincide.

Figure 166 shows a suitable construction of commutator for machines up to about 30 k.w. The cast-

iron spider A is provided with four tunnels B to ventilate the inside of the commutator, bored internally to fit the shaft S, and held in position by a key C fitted into a keyseat on the shaft. The V-shaped clamping end rings D, one of which is cast with the spider A, fit into the V-grooves turned in either side of the commutator. Complete insulation of the segments from the supporting structure is obtained by conical mica rings E moulded or built up to the required taper. The thickness of these rings ranges from 2 millimetres for 100-voltarmatures to 4 millimetres for 1000 volts. The pressure on the clamping rings is applied and maintained by the nut F, and the latter, after the rings are finally tightened, is prevented from slacking back by means of a set-pin.

The apices of the clamping rings are rounded off to

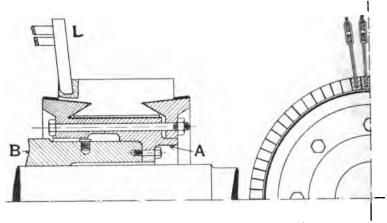


FIG. 167.—Commutator for 30-200 k.w. machine.

provide draw for the wedging action previously mentioned. Between the inner periphery of the segments and the spider A is a small air-space H. This reduces the possibility of any of the segments coming into contact with the spider. Experience has demonstrated that clamping rings having a double taper best prevent dislocation of the segments. The total angle is generally about 35 degrees, and is divided into 30 degrees below the horizontal and 5 degrees above, as indicated in the figure. By means of the double taper the segments are held endwise and centred round a circle defined by the diameter of the apices of the rings. As the clamping rings and commutator expand or contract the segments are concentrically maintained.

The commutator shown in Figure 167 is of suitable design for machines of from 30 to 200 k.w. The commutator spider A is bolted direct to the end of the armature spider B, and is therefore free from the shaft, so that

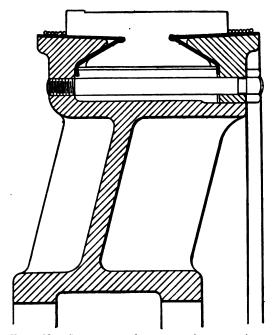


FIG. 168.—Commutator for 200-500 k.w. machines.

the armature and commutator are entirely and separately self-contained. This forms an excellent mechanical arrangement, and no displacement of the armature winding relative to the commutator can possibly take place.

In Figure 168 is shown a commutator suitable for machines of from 200 to 500 k.w. The commutator is built on an armed spider, which is subsequently mounted on an extension of the armature spider, the commutator spider being held in position by means of a key sunk into a key-seat on the spider.

For large generators of 500 k.w. and upwards the best mechanical construction and ventilation is obtained by mounting the commutator on a spider which can be bolted to the arms of the armature spider, as shown in Figure 169. Each arm of the former has a projecting seat A, to which, after facing, the commutator spider S is bolted. (The armature spider in Figure 139 shows

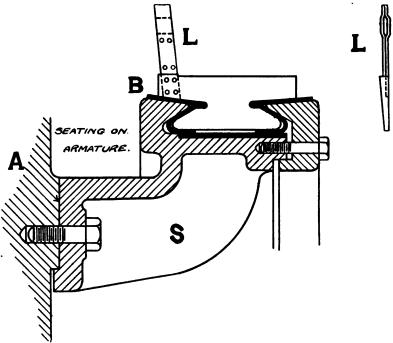


FIG. 169.—Commutator for 500-1400 k.w. generator.

the projecting seats.) In commutators of this size the V-clamping rings are in some cases constructed in sections, each separately bolted to the spider. This facilitates the removal of a faulty segment without disturbing the rest of the commutator.

Connections from the armature windings to the commutator segments are made by soldering the armature conductors into lugs projecting radially from the back of the commutator. In small commutators the lug and segment are forged in one piece. At the top of

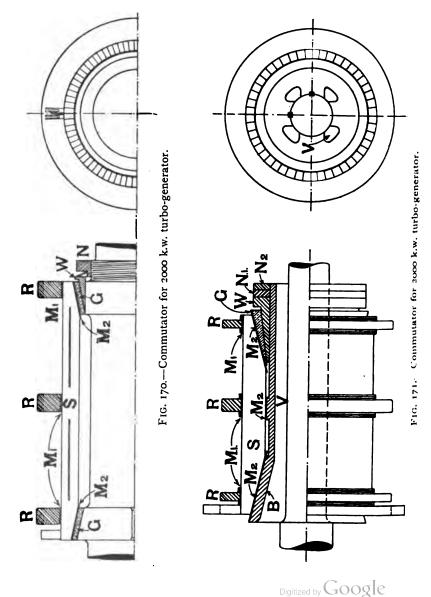
the lug a groove is slotted, into which the conductors are brought out straight and soldered, as shown at L in Figure 166. For large commutators the lug invariably consists of two strips riveted together and fixed to the segment, as shown in Figure 169. The segment has a recess in it equal to the thickness of the lug L, and the latter is riveted as shown at B, and finally brazed or soldered. At the upper end, the strips forming the lug are separated and made to embrace the ends of the armature coils as shown. In Figure 167 the lug L, formed by two strips of copper riveted together, is fixed into a groove cut in the end of the segment and then soldered or brazed.

Commutators for High Speeds.—The ordinary commutator construction, which has just been described, for peripheral speeds not exceeding 20 metres per second, is inadequate when the speed is as high as 30 to 40 metres per second. In order to present sufficient radiating surface, commutators for high-speed dynamos have great axial length compared with their diameter, so that if the ordinary V-shaped clamping rings at each end of the commutator were used the centrifugal forces would tend to cause the long segments to bulge outwards. Hence special constructions are necessary, and the general practice is to provide the segments with retaining members, in the form of steel rings, along their length, usually disposed one at each end and one in the middle.

Figures 170 and 171 show the construction of two high-speed commutators. These may be taken as typical of the best standard practice. The copper and mica segments are assembled in the same manner as before, but instead of the ordinary V-rings the segments S are retained in position by steel rings R shrunk on outside, with an intervening layer of mica insulation  $M_1$  to prevent the rings from short-circuiting the segments. At each end, the interior of the commutator is bored tapered.

The design in Figure 171 is that usually adopted for units of 2000 k.w. and upwards. The commutator is fitted on a cast-iron spider B of the shape shown, and

provided with ventilating tunnels V through which air is driven by cup-shaped blades at the outer end of each. At the armature end the spider is cast with a taper, to fit the taper to which the interior of the commutator is bored; at the other end the commutator is fitted with a tapered gun metal bush G. To insulate the segments



from the spider and bush G the surfaces on which the segments would bed are covered with a sleeve of mica M<sub>2</sub>. After the commutator is slipped on into position it is forced tight against the tapered seat on the spider by means of the wedge ring W and nut N<sub>1</sub>, the latter being secured by the lock nut N<sub>2</sub>.

Commutators of comparatively small diameter are usually built up on the lines of design shown in Figure 170. The commutator is fitted at each end with a tapered gun-metal bush G, and the latter is insulated from the segments with a layer of mica M<sub>2</sub>. Collars are turned on the shaft at intervals corresponding to the axial pitch of the bushes: the one at the armature end being tapered and that at the other end parallel. The commutator is slipped on into position and forced tightly home on the collar seats by means of the wedge ring W and the spring nut N.

As a further precaution against the action of centri-

fugal force, commutator segments are sometimes of the cross-sectional formation shown in Figure 172, which ensures an entire circumferential interlocking of the assembled segments.

Owing to the centrifugal force to which they are subjected the lugs are best forged in one piece with the seg- FIG. 172.—Method ments, and connection is made to the armature coils in the manner shown in Figure 166.



of locking the segments of high-speed com-

The radial wearing depth of commutators provided in good practice has initially 100 per cent. margin over the depth required for mechanical rigidity and electrical conductivity. A limited number of segments with narrow annular slots formed in them, as shown in Figure 170, afford an indication when the radial depth has been worn down to the permissible minimum.

The stress on the commutator shrinking rings is **expressed** by

$$S = \frac{F_1 + F_2}{2\pi a}$$
 kilogrammes per square centimetre,

where—

F<sub>1</sub> = centrifugal force of all the commutator segments. F<sub>2</sub> = centrifugal force of the rings due to their own weight.

a =area of cross-section of all the rings.

The value of F<sub>1</sub> can be obtained from the formula

 $F_1 = 0.0000112 \text{ MRN}^2 \text{ kilogramme.}$ 

In order to arrive at the value of  $F_2$ , let m denote the weight in kilogrammes of the shrinking rings per cubic centimetre; then the centrifugal force of the rings per unit mass =  $f = 0.0000112 \, m \, \text{R} \, \text{N}^2$  kilogramme. Since  $2\pi R a$  denotes the volume of the rings, their total centrifugal force is expressed by

$$F_2 = 0.0000112 \cdot m \cdot RN^2 \times 2\pi Ra$$
 kilogrammes.  
=  $f \times 2\pi Ra$ .

The rings being always of cast steel, the safe working stress may be taken as 1100 kilogrammes per square centimetre, so that having calculated F<sub>1</sub> and F<sub>2</sub>, the sectional area of all the rings is expressed by

$$a = \frac{F_1 + F_2}{2\pi S} = \frac{F_1 + F_2}{2\pi \times 1100} = \frac{F_1 + F_2}{7000}$$
 square centimetres.

The usual practice is to make the middle ring of 50 per cent. greater sectional area than either of the two end rings.

The bending moment on one commutator segment is

expressed by

$$B = \frac{F_3 \times l}{8}$$
, where—

F<sub>3</sub> = centrifugal force of that portion of a single segment which lies between two shrinking rings.

l = distance between the centres of the rings.

If b denote the average breadth of segment and d the depth, then the modulus of section =  $Z = \frac{b \times d^2}{6}$ .

The bending stress on one segment =

$$S = \frac{B}{Z} = \frac{F_3 \times l}{\underbrace{8 \times bd^2}_{6}} = \frac{F_3 \times l}{1.33 \times bd^2},$$

which for copper should not exceed 600 kilogrammes per square centimetre. The minimum depth of segment should therefore be such that this value is not exceeded.

### Brush Gear

Brushes and Brush-holders.—Brushes for collecting current from the commutator were at one time entirely made of copper gauze or metal leaves compressed together. Metal brushes had two inherent faults: first, the soft copper bars of the commutator and the soft metal brushes did not wear well mechanically, so that great difficulty was experienced in maintaining a smooth commutator surface; second, owing to their low-contact resistance sparkless commutation could not be obtained from no-load to full-load with fixed brush position, for reasons which are explained in the next chapter.

Brushes are now invariably made of hard blocks of graphitic carbon, although for turbo-dynamos specially constructed metal brushes are sometimes used. Carbon brushes wear well mechanically and give to the commutator a tough glassy surface, and so reduce wear. In machines having a commutator peripheral speed of more than 15 metres per second, the friction loss due to carbon brushes may assume considerable proportions, and to reduce it to a minimum the carbons are sometimes boiled in paraffin wax.

Besides supporting the brush, the brush-holder has also to press it firmly against the commutator, and at the same time give sufficient flexibility to enable it to ride over any slight eccentricity of the commutator without reducing the efficiency of contact.

Brush-holders for carbon brushes are of two types. The first, or *hammer type*, is shown in Figure 173, and is designed to take a taper-shaped carbon block, which

bears radially on the commutator. The frame of the brush-holder consists of two cast brass or aluminium cheeks A, which at the brush end terminate in V-shaped jaws, in which the carbon block C is firmly gripped by

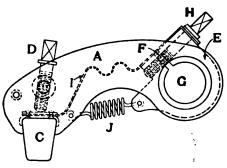


FIG. 173.—Hammer type of brush-holder.

a set-screw D. The brass clamping part E of the holder can move through a small angle independent of the cheeks A, and is split at F so that it can be clamped to the spindle G by means of the set-screw H. A copper lead I assists in con-

ducting the current from the brush to the spindle, and the electrical connection between the brush and the jaws is augmented by copper plating the top of the former. The pressure on the brush is uniformly applied by means

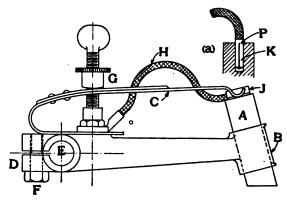


FIG. 174.—Box type of brush-holder.

of a spring J, the tension of which can be adjusted by the angular movement of the clamp E.

Figure 174 illustrates the second or box type of brushholder, the frame of which is of brass or steel-bronze. The brush A is a rectangular block free to move radially up and down in the guide-box B, and is pressed down by the spring C bearing on the top of it. The brass clamping part D is split as in the previous type, and is clamped to the brush spindle E by means of the set-screw F. The tension of the spring is adjusted by the milled nut G. Current is led from the brush to the clamp by means of a flexible fine copper wire H, technically known as a pig-tail. The pig-tail is soldered to the clamp J which is fixed over the top of the brush, the latter having been previously coppered. In some cases the pig-tail is soldered to a brass split-pin P (shown at a), which is driven into a small hole K in the top of the carbon,

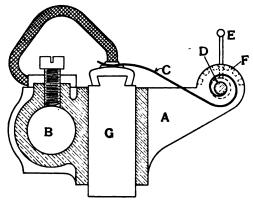


FIG. 175.—Box type of brush-holder.

the sides of the hole being coppered in order to ensure good electrical contact.

Figure 175 shows another form of brush-holder of the box type. The brush-holder A is attached to the spindle B at one end, and the tension of the spring C is controlled from the other end. The free end of the spring rests on the brush G as before, but the other end is coiled once round and fixed to a small drum D pivoted between the sides of the brush-holder. The drum can be rotated through a small angle in either direction by means of the lever E attached to the spindle of the drum. There are five notches F on the frame of the holder in which the lever can be held. As the lever is moved over the successive notches the drum either winds up or uncoils the spring, thus adjusting the tension.

Figure 176 shows a brush-holder suitable for the metal brushes used for collecting current from the commutators of turbine-driven dynamos. The brush-holder is entirely of brass. It consists of a movable part A which swings on the brush-spindle E, and a fixed part B which is clamped to E by means of a set-screw. The brush D is composed of fine brass wire enclosed in a brass gauze envelope, and is soldered into a solid brass block K, which in turn is fixed to the feed-screw nut G. Passing through the centre of the movable part of the

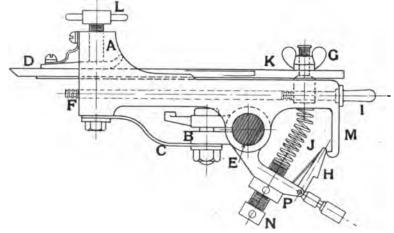


Fig. 176.—Brush-holder for turbo-generator.

holder is a feed-screw spindle F, which engages with a worm turned in G so that the brush D can be moved towards or away from the commutator by turning the handle I. When the brush has been moved into the correct position it is clamped to the holder by means of the set-screw L. A copper flexible C assists in carrying current from the part A to the part B. H is a hold-off catch operated by an insulated handle. When in the position shown it engages with a lug M projecting from the movable part A, and so presses the brush against the commutator. When H is moved towards the spring J it disengages the lug M and allows the tension of the spring J to cant the brush-holder, and thereby lift the brush off the commutator. The pressure with which

the brush bears on the commutator depends on the tension of J, and can be adjusted by means of the set-screw N, which in turn is locked by the nut P.

Brush-holder Rings. — The spindles, to which the brushes are clamped, are fixed to arms projecting from a cast-iron ring which is mounted concentric with the commutator, and so arranged that it can be given a small angular displacement. Where the diameter of commutator does not exceed about 0.8 of a metre the usual practice is to mount the ring (sometimes called the brush-

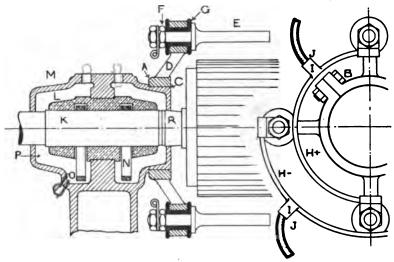
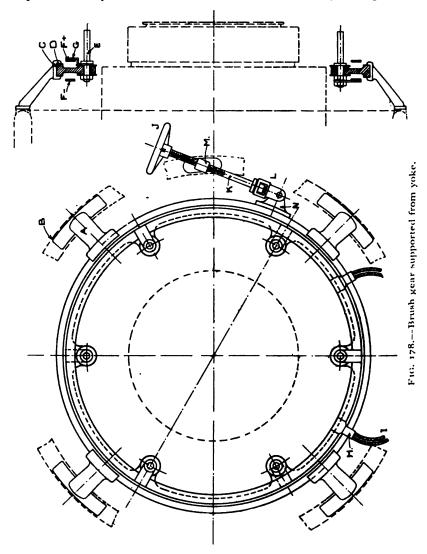


FIG. 177.--Brush gear supported on bearing.

rocker) on the bearing next to the commutator. This arrangement is shown in Figure 177, which shows a section and end-view of a four-armed brush-rocker. The ring A is made in two parts, bolted together so as to fit on a path C turned on the surface of the bearing. The ring carries four arms D, placed 90 degrees apart, from each of which there projects over the commutator a brass brush-spindle E. The latter are provided with keyways and bolted to the top of the arms by nuts F, but are insulated therefrom by means of vulcanite bushes and washers G. The brush-holders are firmly clamped on to these spindles. Brush-spindles of similar polarity are

connected together by copper connectors H + and H -, and for effecting the connection the brush-spindles project 1.5 to 3 centimetres beyond the nuts F. To the cross-connectors are cast sockets I, into which the flexible cables J are sweated for connection to the terminals of the machine. Once the correct brush-position has been experimentally determined the rocker is securely clamped.



In large machines the rings carrying the brush-gear are supported by brackets bolted to the magnet yoke, as shown in Figure 178. The brackets A are of cast-iron and bolted to machined seats B on the yoke. The under side of the brackets has a turned groove C into which the ring D fits. The latter may be of various sections, and in the case shown is of I section. The brushspindles E are spaced along the circumference of the ring and bolted in the manner shown, the spindles being insulated from the ring by vulcanite bushes in a similar manner to that shown in the previous figure. opposite sides of the ring are mounted on insulating supports connectors F + and F - of stout copper strip. These serve to cross-connect brush-spindles of the same polarity, connection with the brush-spindles being made by copper lugs G, which are riveted or brazed to the connectors. To each connector is cast or bolted a terminal H, into which the flexible cables I, connecting the brushes to the terminals of the machine, are soldered.

To the lower part of the right-hand side of the ring is bolted a bracket N, which is connected by the link L to the screwed spindle K. The screw of the spindle engages in a worm M fixed to the magnet frame, so that when the spindle is rotated by operating the handle J the brush-ring is given angular motion. This addition to the brush gear now appears almost unnecessary, as all direct-current machines are required to work with a fixed brush position.

# SHAFT AND BEARINGS

Shaft.—Armature shafts are invariably of mild steel and require to be of sufficient stiffness to resist the combined stresses set up by (1) the bending moment due to the weight of the armature and commutator; (2) the twisting strains due to continuous transmission through it of the energy supplied by the prime mover to the armature inductors; and (3) any unbalanced magnetic pull on the armature core produced by the unequal distribution of the magnetic field. The method of calculating the diameter of shafts is discussed in various text-books on mechanics. The following formula is found to give a

diameter of shaft of sufficient stiffness to withstand the stresses due to the fluctuating load of a dynamo:

$$d = 18\sqrt[3]{\frac{\text{H.P.}}{\text{R}}}.$$

where-

d =The diameter of the shaft in centimetres at any part underneath the armature or commutator.

H.P. = Horse-power transmitted by the shaft.

R = Speed of the shaft in revolutions per minute.

The armature spider considerably increases the stiffness at the centre, and in cases where the armature is coupled to the prime mover by a coupling projecting from the armature core (as shown in Figure 213) the shaft is entirely relieved of the driving strain, and has only to withstand the bending moment due to the weight of the armature and commutator. Every case must, however, be considered on its merits; for instance, in a machine having a very small air-gap the shaft would require to be exceedingly stiff in order to reduce to a minimum the bending liable to occur through unbalanced magnetic pull set up by inequalities in the strength of the several fields. Armature shafts are usually turned of larger diameter at the middle than at the ends, to allow for diminution of cross-section due to the key-ways.

Bearings.—The bearings and pedestals for supporting armature shafts are similar to those employed for other types of machinery, and a typical dynamo bearing is shown in Figure 177. The shaft K revolves in a split brass bush L: the latter is prevented from turning by the cap M. In order to facilitate the removal of the armature, and to provide a means of adjusting for wear, the bearings are generally in two parts, held together by bolts. Two circumferential slots are cut in the upper half of the bush so as to allow two brass rings N to rest upon the shaft. The lower parts of these rings dip into the oil well O, and as the shaft revolves it carries the rings with it, and in this way a continuous automatic lubrication of the bearing is effected.

Each end of the bearing is provided with a hooded

chamber P, in which the oil oozing from the ends of the brasses is caught and returned to the oil well. At the end nearest the armature the shaft is provided with an oil thrower R, by turning buttress-shaped recesses in that part of the shaft covered by the hood. The oil which oozes out from the end of the brass is thus thrown off the shaft by the action of centrifugal force, and so prevented from creeping along to the armature or commutator.

#### CHAPTER IX

THE DYNAMO—FIELD MAGNETS, MAGNETIC CIRCUIT, ARMATURE REACTION, COMMU-TATION, COMMUTATION POLE MACHINES, AND EXAMPLES OF COMPLETE MACHINES

## FIELD MAGNETS

Types of Field Magnets.—For 2-pole dynamos the field magnets are generally in the form of a horseshoe with straight limbs and two exciting coils, as shown in Figure 179. The composite magnet has forged iron or steel limbs L and a cast-iron yoke Y, both limbs and

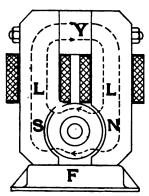


FIG. 179.—Magnetic circuit of a 2-pole dynamo.

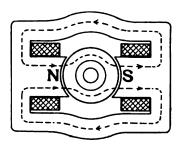


Fig. 180.—Magnet circuit of a 2-pole iron-clad dynamo.

yoke having a rectangular cross-section. The whole machine, *i.e.* armature and field magnets, is supported on a cast-iron bed-plate, so that it becomes necessary to attach, to the magnet poles, feet or brackets F made of some non-magnetic material such as gun-metal. Should

the non-magnetic feet be omitted a closed magnetic circuit would be formed through the bed-plate of the machine, and the bulk of the lines of force would pass from pole to pole by way of the bed-plate, instead of through the armature as required. The vertical depth of the feet must be such as to avoid excessive leakage of lines of force into the bed-plate, and should therefore be commensurable with the total radial length of air-gap. Figure 180 shows the magnetic circuit of an iron-clad 2-pole dynamo. The poles are placed horizontally, and the yoke is divided and passes above and below the armature.

The 2-pole type of field magnet is well suited for high-speed generators, but for lower speeds commercial considerations preclude its general use for large sizes owing to the costliness of the necessarily massive magnet

To meet this poles. contingency, when the speed of the armature is low, its diameter is increased, and instead of a single horseshoe field magnet, an iron ring, with many pairs of poles grouped round its periphery, is employed. This is the form of the field magnet of a modern multipolar machine. which each pair poles, with its portion

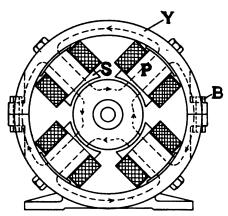


Fig. 181.—Magnetic circuit of a 4-pole dynamo.

of the armature, constitutes a unit. By increasing the number of these units the output of the machine is increased.

The magnetic circuit of a 4-pole machine is shown in Figure 181. This, it will be observed, is in reality only a multiplication or development of the principle of the 2-pole iron-clad machine in the previous figure. The circular yoke Y of the field magnet frame is usually divided on a horizontal diameter, the faces of the upper

and lower halves being accurately machined and held together by bolts B. The inward projecting poles P are either bolted or cast to the inner surface of the magnet ring. To prevent too sudden a variation of magnetic flux in the armature teeth when approaching or receding from the poles, the latter are fitted with extensions S known as pole shoes.

In Figures 179 to 181 the path taken by the main magnetic flux is indicated by the dotted lines and its direction by the arrow-heads.

Excitation of Dynamos.—According to the method of exciting their field magnets, dynamos are classified as: (1) Separately excited; (2) shunt-wound; (3) serieswound; and (4) compound-wound.

Separately excited Dynamos.—As the name implies, these are dynamos in which the magnet coils are supplied

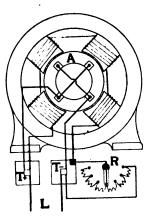


Fig. 182.—Shunt-wound dynamo.

with current from an independent source, to distinguish them from self-excited machines, in which the exciting current is obtained from the armature. Separately excited dynamos are only employed for special purposes; as, for example, the low-voltage generators used for electroplating, and dynamos used as boosters.

Shunt-wound Dynamos.—The field coils of a shunt machine consist of a large number of turns of comparatively fine wire connected across the armature ter-

minals, the resistance of the field coils being such that the excitation current ranges, according to the output, from 1 to 6 per cent. of the total current. In Figure 182 is a diagram for the connections for a shunt dynamo. The brushes for collecting the current from the armature A are connected to the main terminals T + and T -, whence connection is made by the leads L to the external circuit. The shunt circuit is shown in red, and the four magnet coils are connected in series: one end of the winding is

connected to T+ and the other to T- through the regulating resistance R, which is used for regulating the field current. It will be observed that the field winding and the external circuit are connected in parallel or shunt at the terminals T+ and T-: hence the name shuntwound dynamo.

The ready building up of the voltage of a self-exciting dynamo depends upon the property of residual magnetism; that is, the field magnets after being once excited retain an appreciable amount of magnetism. This residual magnetism ensures a small number of lines of force always being linked with the armature inductors, so that when the armature is rotated a small E.M.F. is induced in it.

In the case of a shunt dynamo (Figure 182) the magnet coils are connected across the armature terminals T + and T -, so that the small E.M.F. due to residual magnetism sets up a small current, which leaves the armature at the positive brush, flows through the magnet coils, and enters the armature at the negative brush. The current sent through the field coils in this way increases the strength of the field in which the armature The E.M.F. consequently induced will send a still larger current through the field coils. Action and reaction thus succeed one another in this manner until the field magnets become saturated, beyond which an increase in the exciting current does not produce an appreciable increase in the magnetic field. The resistance of the shunt circuit may, however, be so high that the E.M.F. ceases to increase before the saturation point is reached; that this is so will be made clear after studying the characteristic curves of dynamos which are dealt with in the next chapter.

Series-wound Dynamos.—In a series dynamo the magnet coils are connected in series with the external circuit, so that the exciting current is the same as that which passes through the external circuit. The required number of ampère-turns is obtained by winding the coils with comparatively few turns of wire of sufficient cross-sectional area to carry continuously the main current. A diagram of the connections for a series dynamo is

shown in Figure 183. The field winding and armature A are connected in series at the common terminal T, while the other end of the field winding and the other armature lead are connected to T - and T + respectively. The latter form the main terminals of the machine, and through them connection is made by the leads L to the external circuit. From the diagram it will be clear that before a current can pass through the magnet coils for excitation purposes the external circuit must be closed.

Compound-wound Dynamos.—A machine of this class is simply an ordinary shunt dynamo having an additional

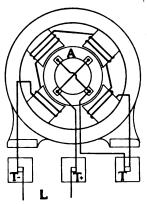


Fig. 183.—Series-wound dynamo.

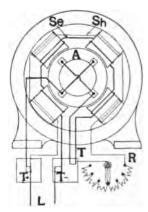


FIG. 184.—Compound-wound dynamo.

magnet winding connected in series with the external circuit for regulating, under varying loads, the pressure on the armature terminals. A diagram of the connections is shown in Figure 184: the shunt winding Sh is connected, through a variable resistance R, across the armature A at the terminals T+and T-. The series winding Se is in series with the external circuit. T+ and T- are the main terminals of the machine, through which connection is made to the external circuit by the leads L.

For constant potential systems of distribution, shunt or compound dynamos are always employed. Series dynamos were at one time largely used for arc-lighting, but have now very limited applications.

Field-magnet Coils.—Field-magnet coils are either spool wound or former wound. The first are wound on a flanged spool of metal or fibre, the shape being such that the spool fits tightly on to the magnet core and is held in position by the pole shoes E, as shown in Figure 190. When of metal the spool or bobbin requires to be insulated. Press-spahn or thin sheets of fibre are usually applied before winding operations are commenced. thickness of the insulation depends upon the voltage for which the machine is designed, and for 600-volt machines is from 2 to 3 millimetres. In compound dynamos this method of winding the magnet coils is invariably adopted; the series winding occupies about 30 per cent. of the axial length of the spool, and is preferably placed below the shunt coils, as shown in Figure 190, the two coils being well insulated from each other. In small machines the series winding is usually wound over the shunt coils, but this retards considerably the radiation of heat from the latter.

In Figure 188 is shown a former-wound coil, which is first wound on a flanged wooden former to hold the wires together during winding. Such coils have strong pieces of tape laced in between the layers to bind them together, and, after winding, the coils are soaked in an insulating varnish and finally covered with strong cotton tapes. The coils must be proportioned so as not to heat beyond a safe limit, and with coils of short axial length it becomes necessary to pile up the winding conically, as shown in Figure 189, thus affording an increased radiating surface. In order to facilitate ventilation, the series coils of compound-wound generators are often supported in such a manner as to leave a space or air-way between them and the shunt coils.

Space Factor.—The value of the space factor of a magnet coil depends upon the shape of the cross-section of the wires. The general practice is to employ wires of circular cross-section for shunt windings, in which case the space factor is determined chiefly by the relative thickness of the wires and their insulating covering. The amount of bedding of the wires of

adjacent layers also affects the space factor to a small extent. Suppose a coil to be wound so that there is no bedding of the wires, as shown in Figure 185. Let  $d_1$  and  $d_2$  denote the diameter of the wire when bare and when insulated. The winding space allotted to each wire  $= d_2^2$ , and that actually occupied by the copper

$$=\frac{\pi d_1^2}{4}$$
, so that the space factor

$$= \frac{\text{section of copper per wire}}{\text{section available per wire}} = \frac{\pi d_1^2}{4d_2^2} = 0.78 \frac{d_1^2}{d_2^2}.$$

For example, suppose a wire of No. 19 S.W.G., having a double cotton covering (D.C.C) insulation, in

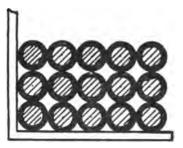


FIG. 185.—Shunt-winding with no bedding.

which the diameter of the wire when bare and when insulated is 1.017 millimetres and 1.22 millimetres respectively, be wound as shown in Figure 185, then the space factor

$$= 0.78 \times \frac{1.017^2}{1.22^2} = 0.54.$$

It has been found by experience that in wires of

small diameter, such as are used for shunt coils, the bedding of the wire rarely increases the space factor by more than 2 or 3 per cent., so that the value given by the above formula, in the absence of a value obtained from actual experience, should be used. The shunt coils of standard dynamos up to 600 volts have space factors ranging from 0.45 to 0.55, and in subsequent calculations 0.5 is taken as being an average value.

# MAGNETIC CIRCUIT

For convenience in calculating the ampère-turns required to set up a definite magnetic flux through each unit of the magnetic circuit, the latter is divided into the following parts:

- Armature Core.
- 2. Armature Teeth.
- 3. Air-gap.
- 4. Magnet Core and Pole Shoes.
- 5. Yoke.

Armature Core.—As already stated, the armature core is constructed of sheet iron or steel laminations, the radial depth of which should be such that the average flux density has a value of between 9000 and 12,000 lines per square centimetre. As seen from the curve in Figure 191, armature laminations can be economically worked at a flux density of 16,000 lines per square centimetre; but in order to keep the iron losses (i.e. hysteresis and eddy currents) within certain limits the flux density in armature cores is usually only from 60 to 75 per cent. of that which would be adopted if the armature iron were not subject to these losses. With multipolar machines it is important to bear in mind that after crossing the air-gap and entering the armature the flux from an N pole passes along two diverging paths towards adjacent S poles, as indicated in Figure 181.

The magnetic length of the core is the length of the mean magnetic path which lies between the roots of the teeth and the inner periphery of the stampings. Since the armature stampings are insulated from each other by paper or varnish, the magnetic sectional area is less than the gross sectional area by an amount varying from 15 to 30 per cent., depending upon the thickness of the said insulation and the number of

ventilating ducts.

Armature Teeth.—The teeth of armatures require to be worked at a flux density of from 19,000 to 23,000 lines per square centimetre. The lines of force do not pass radially from the pole face to the armature surface, but spread out at the ends of the pole face, as shown in Figure 186. The result of this spreading is that the number of teeth forming the path by which the lines of force pass from the pole face to the armature, is increased by about 10 per cent. The magnetic area of a tooth is the product of the mean width and the net length of armature core.

In calculating the flux density in the teeth it may be assumed that all the flux enters the armature by way of the teeth. The flux density calculated on this assump-

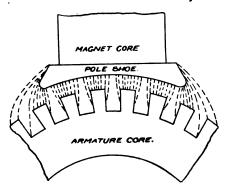


FIG. 186.—Distribution of flux in air-gap with slotted armature.

tion is known as the apparent flux density. The permeability sheet iron at the high induction densities occurring in the teeth of armatures is many times greater than that of air, with the result that the total flux in the armature does not enter by way of the teeth, as assumed in calculating

the apparent flux density; but a considerable proportion enters the armature by the parallel paths, of higher magnetic reluctance, offered by the slots, ventilating ducts, and insulation between adjacent armature laminations.

The relation between the total lines  $M_1$  transmitted by a combined tooth and slot and those  $M_2$  transmitted by a tooth alone, may be derived as follows:

Let a = mean width of a tooth.

b =width of slot.

 $l_n$  = net length of armature iron parallel to the shaft.

d = depth of slot.

 $\eta$  = net length of iron  $\div$  gross length of core.

The cross-section of iron per tooth =  $a \times l_n$ , and the cross-section of each slot =  $\frac{b \times l_n}{\eta}$ .

Since the flux also enters the core by way of ventilating ducts and insulation between the core plates, the area of cross-section of the latter per slot

$$=\frac{a\times l_n}{\eta}-a\times l_n=al_n\left(\frac{1}{\eta}-1\right)$$

The cross-section of the non-iron path per tooth therefore

$$= \frac{b \times l_n}{\eta} + a l_n \left( \frac{1}{\eta} - 1 \right)$$
$$= \frac{l_n \left( b + a - \eta a \right)}{\eta}.$$

Let the flux  $M_1$  entering the armature per tooth divide, so that  $M_2$  lines enter by a tooth and  $(M_1-M_2)$  by air space and insulation, then if  $\mu$  denote the permeability of the teeth

$${
m M_2} \propto {{
m area~of~cross~section~of~teeth} imes \mu \over {
m depth~of~tooth}}$$
  ${
m M_2} \propto {{a l_n} \times \mu \over d}$ .

Similarly, for the flux in non-iron part per tooth

$$M_1 - M_2 \propto \frac{l_n \left(b + a - \eta a\right)}{d\eta}$$
.

The ratio

$$\frac{M_2}{M_1 - M_2} = \frac{al_n \mu \times \eta d}{dl_n (b + a - \eta a)} = \frac{a\eta \mu}{b + a - \eta a}$$
or  $M_1 a \eta \mu = M_2 (b + a - \eta a + a \eta \mu)$ ,
$$i.e. \frac{M_2}{M_1} = \frac{b + a - \eta a + a \eta \mu}{a \eta \mu}.$$

On an average the ratio of net length to gross length of core = 0.75, so that substituting this value for  $\eta$ ,

$$\frac{M_2}{M_1} = \frac{1.33b + 0.33a + a\mu}{a\mu}$$

If  $B_1$  denote the real tooth density, and  $B_2$  the apparent tooth density, then since  $\frac{M_2}{M_1} = \frac{B_2}{B_1}$ ,

$$\frac{B_2}{B_1} = \frac{1.33b + 0.33a + a\mu}{a\mu}.$$

The value of  $\mu$  corresponding to any particular value of  $B_2$  may be obtained from a permeability curve, and

knowing a and b the corresponding value of  $B_1$  can be

computed.

The method is shown graphically in Figure 187, where the abscissæ represent apparent tooth density and the ordinates real or corrected values. The latter

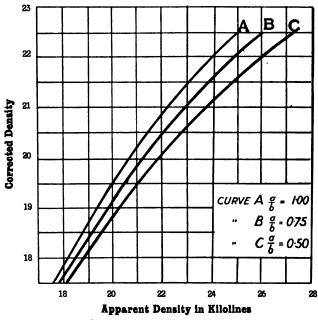


Fig. 187.—Curves of corrected tooth density.

depend upon the ratio of width of tooth to width of slot, and three curves are given where the value  $\frac{a}{b}$  equals 1, 0.75, and 0.5. In practice the ratio  $\frac{a}{b}$  lies between 1 and 0.5, and for intermediate values of  $\frac{a}{b}$  the corrected tooth density can be estimated with an accuracy sufficient for all practical purposes.

Air-gap.—The flux density in the air-gap ranges from 6000 to 9000 lines per square centimetre, and the simplest method of determining it is to take the average density over the pole face, i.e. the total flux entering or

leaving the armature per pole, divided by the surface area of the pole face. The actual area of exposed iron on the surface of the armature is less than that of the pole face due to the slots between the teeth, but on the other hand there is a spreading of the lines of force when passing from pole face to armature, and it is usual in practical calculations to assume that these two effects counteract each other.

The ampère-turns required to send the flux across an air-gap are obtained from the formula

$$H = 1.25 \frac{CT}{l}$$
, i.e.  $CT = 0.8Hl$ 

where—

CT = Ampere-turns per pole.

H = Induction density in the air-gap.

l = Length of air-gap.

From this formula it will be seen that the greater the length of air-gap the larger the magneto-motive force required to send the flux through the air-gap, so that it would appear that the length of air-gap should be reduced to the mechanical limit. As will be shown later, the effects of armature reaction on the main field increase inversely as the length of air-gap. A compromise must therefore be made between these two considerations, and experience shows that air-gap lengths should not be less than half the width of a single tooth. In multipolar machines the length of air-gap ranges from 0 5 to 1.2 centimetres for machines in which the armature diameter is between 0.7 and 5.0 metres.

Magnet Cores and Pole Shoes.—Magnet cores are made of cast steel, wrought-iron forgings, or sheet iron or steel, and the induction density ranges from 14,000 to 16,000 lines per square centimetre. Figures 188 to 190 illustrate three types of magnet cores, all of which are extensively used. In Figure 188 the magnet core C and yoke Y are cast in one piece, while in Figure 189 the magnet core C, of circular cross-section, is cast separate, and after being machined is bolted to a seating

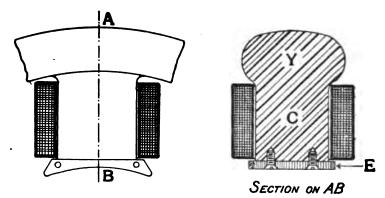


FIG. 188.—Magnet core and yoke cast solid.

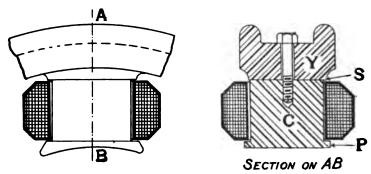


Fig. 189.—Magnet core bolted to yoke.

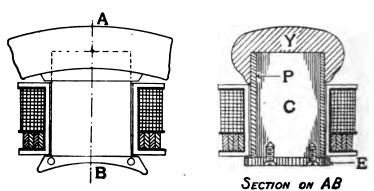


FIG. 190.—Magnet core laminated and cast into yoke.

S cast on the yoke. In the third type (Figure 190) the magnet core C is built up of sheet-iron laminations

riveted together between two end plates P and cast into the yoke Y. The magnet core is of rectangular cross-section, and in some designs is left without polar extensions, in which case the flux density in the core must be reduced to about 12,000 lines per square centimetre, so as to prevent an uneconomically high

air-gap density.

Pole shoes are usually of steel, and may be cast in one piece or built up of laminated sheets, preferably the latter in large machines, for reasons stated below. In the design shown in Figure 189 the pole shoe P can conveniently be cast in one piece with the magnet core, the field coils being placed over the core before it is bolted to the yoke. The pole shoe E in Figures 188 and 190 is laminated; the stampings are cut to the shape shown, and then riveted together between two stout end plates. The pole shoe is fixed to the magnet core by set-screws, the field coils being slipped on before the core is finally secured. The coils are held in position by the pole shoes.

Pole shoes are liable to have eddy currents induced in them due to unequal distribution of the flux, which extends in a marked degree to the pole face, as shown in Figure 186. As the armature teeth move under the pole face the tufts of flux change from one position to another, with the result that eddy currents are induced. In large machines the loss of energy and heating due to this cause may become so great that lamination of

the pole shoes is necessary.

In machines of ordinary design the span of the pole face or the length of polar arc ranges from 0.68 to 0.72 of the polar pitch, and 0.7 may be taken as an average value. When, however, commutation poles (see u.s., Figure 210) are fitted, considerations of magnetic leakage necessitate a shorter polar arc, which generally ranges from .55 to .65 of the polar pitch. The radial length of pole shoe varies from 2 to 4 centimetres, and in virtue of this length being so small, it is customary to include it in the length of the magnet core. Experience shows that this leads to no appreciable inaccuracy. In designing a dynamo the diameter of

the armature is approximately determined in the manner described on page 447, and from this the area of pole face is settled, the gross length of the pole face being made equal to the gross length of the armature core. Then assuming a maximum flux density of from 8000 to 9000 lines per square centimetre in the air-gap, the total flux entering the armature from each pole face can be determined.

The axial length of the magnet core will depend upon the space necessary for the field winding, and a value is first assumed from experience with other machines. The dimensions of field coils must be such that the radiating surface is sufficient to prevent the temperature rise exceeding a pre-determined limit. The method of estimating the temperature rise is indicated in Chapter XII.

Yoke.—Magnet rings or yokes are generally of cast iron or steel, and the cross-sectional area is such that the flux density does not exceed 8500 or 15,000 respectively. From these figures it will be seen that with two machines having the same electrical and magnetic constants, but one having a cast-iron yoke and the other a cast-steel, the cross-sectional area of the latter will be approximately half of the former. In calculating the ampère-turns to send the flux through the yoke the magnetic length is the mean length of path, and it should be remembered that the flux in each section of the yoke in a multipolar machine is only one-half that of the flux per pole.

In calculating the number of ampère-turns per pole required to send a given flux through the magnetic circuit, use is made of such curves as are shown in Figure 15. The parts of the curves used in dynamo calculations for cast iron and cast steel are reproduced in Figure 191, along with the curve for armature laminations. A separate magnetisation curve for the high densities occurring in armature teeth is given in Figure 192

Coefficient of Magnetic Leakage.—As explained in Chapter III. lines of force will pass between surfaces which are at different magnetic potentials: consequently

in all dynamos the total flux in the magnet core does not pass through the armature, but a certain proportion leaks across from one pole to another by way of the air, as depicted in Figure 193. The ratio of the total flux generated to the useful flux in the armature has been called the coefficient of magnetic leakage, or the

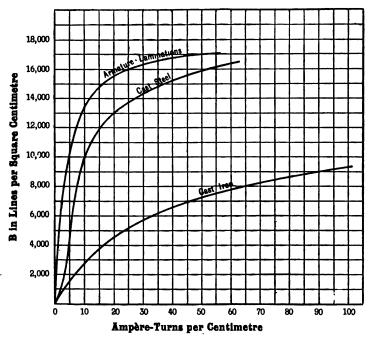


FIG. 191.—Magnetisation curves used in dynamo calculations.

dispersion coefficient, as suggested by Prof. S. P. Thompson, and is given by the equation

$$v = N_m/N_a$$
.

The flux set up in any one unit of the magnetic circuit is a maximum in the yoke, and gradually diminishes, until at the armature surface it is reduced to the useful flux that becomes linked with the inductors. In practical calculations it is convenient to assume that the useful flux passes through the armature core, teeth, and air-gap, and that all the leakage of lines of force

takes place at the pole face, thus allowing the total flux generated to pass through the magnet core. This assumption considerably simplifies calculations relating

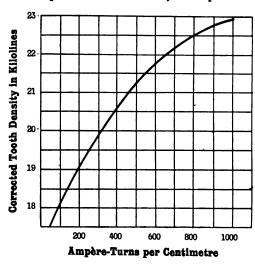


FIG. 192.—Ampère-turns for armature teeth.

to the magnetic circuit, and experience shows that the results obtained are of sufficient accuracy for ordinary work.

Leakage lines of force necessitate an increased section of the yoke and magnet core beyond that actually necessary to carry the useful flux; and an increase in the section of the magnet core means that

each turn of the field winding must be correspondingly increased. It therefore becomes important to design magnetic circuits with the minimum amount of leakage,

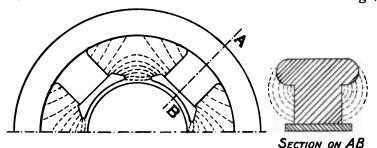


Fig. 193.—Magnetic leakage from multipolar magnet.

so that a given output can be obtained with the minimum of materials.

The extent of magnetic leakage depends upon—(1) The shape of the magnet core; (2) the length of air-gap; and (3) the induction density in the magnet core.

On account of the smaller surface area magnet cores of circular cross-section have less leakage than a rectangular pole having the same sectional area. The greater the length of air-gap the greater the reluctance of the magnetic circuit, and consequently also the greater the tendency for the flux to take alternative paths. By increasing the flux density in the magnet core the reluctance of this portion of the circuit increases while the leakage paths through the air remain constant, with the result that the leakage lines of force are increased.

The dispersion coefficients vary with different types of machines, and the actual values employed in practice are usually determined from experiment. The values of the dispersion coefficients for multipolar machines range from 1.3 in small machines and those in which the poles are close together, to 1.1 in very large machines.

Example of Calculation relating to the Magnetic

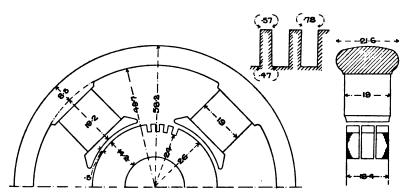


FIG. 194.—Magnetic circuit for example.

Circuit.—An example will now be worked to illustrate the application of the foregoing principles. In Figure 194 is given a dimensioned drawing of the magnetic circuit of a 33-k.w. shunt-wound 4-pole dynamo, the armature details of which are given in the example on page 274.

At no load the magnetic flux per pole passing through the armature equals 3.45 megalines. At full load the internal pressure drop due to armature and

brush resistance is 22 volts, so that to maintain a constant terminal E.M.F. of 550 volts the flux per pole at full load is given by

$$M = \frac{E \times 10^8}{4 \times T \times N} = \frac{(550 + 22)10^8}{4 \times 181 \times 22} = 3.6 \text{ megalines.}$$

It is required to determine the ampère-turns per pole necessary to overcome the reluctance of the magnetic circuit (1) at no load, and (2) at full load. The method of procedure is as follows:

### Armature Core

The area of cross-section of iron =  $\{18.4 - (2 \times 1)\} \times 0.9 \times (24 - 11.8) = 180$  square centi-

The mean length of path taken by the flux as measured from drawing = 15 centimetres.

Flux density at no load =  $\frac{3.45 \times 10^6}{2} \times \frac{1}{180} = 9.6$  kilolines per square centimetre.

From Figure 191 ampère-turns per centimetre of

length = 4.5.

Flux density at full load =  $\frac{3.6 \times 10^6}{2} \times \frac{1}{180} = 10.0$  kilolines per square centimetre.

Ampère-turns per centimetre of length = 5.4. Ampère-turns at full load =  $15 \times 5.4 = 80$ .

### Armature Teeth

Number of teeth per pole =  $\frac{121}{4}$  = 30.3.

In the machine under consideration the polar arc is 0.69 of the polar pitch, so that after allowing 10 per cent. for fringing the number of teeth under one pole =  $30.3 \times 0.69 \times 1.1 = 23.$ 

Mean area of cross-section of iron in one tooth

=  $\{18.4 - (2 \times 1)\} \times 0.9 \times 0.52 = 7$  square centimetres.

Area of cross-section of all the teeth under the polar  $arc = 7 \times 23 = 161$  square centimetres.

Length of teeth = 2 centimetres.

$$\frac{\text{Mean width of tooth}}{\text{Width of slot}} = \frac{a}{b} = \frac{0.52}{0.78} = 0.67.$$

Apparent tooth density at no load =  $\frac{3.45 \times 10^6}{161}$  = 21.5 kilolines per square centimetre.

Corrected tooth density at no load (Figure 187) = 20.1

kilolines per square centimetre.

From Figure 192 the ampère-turns per centimetre of length = 320.

Ampère-turns at no load = 320 × 2 = 640.

Apparent tooth density at full load =  $\frac{3.6 \times 10^6}{161}$  = 22.4 kilolines per square centimetre.

Corrected tooth density at full load = 20.7 kilolines

per square centimetre.

Ampère-turns per centimetre of length = 425. Ampère-turns at full load =  $425 \times 2 = 850$ .

### Air-gap

Circumference at air-gap =  $\pi \times 2 \times 26 = 163$  centimetres.

Length of polar arc =  $\frac{163}{4} \times 0.69 = 28.1$  centimetres.

Width of pole face = gross width of armature = 18.4 centimetres.

Area of cross-section of air-gap = area of pole face =  $18.4 \times 28.1 = 517$  square centimetres.

Length of air-gap = 0.5 centimetre.

Average flux density at no load =  $\frac{3.45 \times 10^6}{517}$  = 6.7 kilolines per square centimetre.

Ampère-turns at no load =  $0.8Hl = 0.8 \times 6700 \times 0.5 =$ 

**2**680.

Average flux density at full load =  $\frac{3.6 \times 10^6}{517} = 7.0$  kilolines per square centimetre.

Ampère-turns at full load =  $0.8 \times 7000 \times 0.5 = 2800$ .

### MAGNET CORE

This is of circular cross-section and made of cast steel.

Area of cross-section =  $\frac{\pi \cdot 19^2}{4}$  = 285 square centimetres.

Length of core (including pole shoe) = 19.2 centimetres.

The dispersion coefficient for this machine was 1.2, though, strictly speaking, it would be greater at full load than at no load, due to an increase in the flux.

Flux density at no load =  $\frac{3.45 \times 10^6}{285} \times 1.2 = 14.6$ kilolines per square centimetre.

From Figure 191 the ampère-turns per centimetre of length = 33.

Ampère-turns at no load =  $33 \times 19.2 = 630$ . Flux density at full load =  $\frac{3.6 \times 10^6}{285} \times 1.2 = 15.2$ kilolines per square centimetre.

Ampère-turns per centimetre of length = 43. Ampère-turns at full load =  $43 \times 19.2 = 820$ .

# Yoke

Also of cast steel.

Area of cross-section =  $21.6 \times 8.5 = 183$  square centimetres.

Mean length of path taken by flux as measured from drawing = 44 centimetres.

Flux density at no load =  $\frac{3.45 \times 10^6}{2} \times 1.2 \times \frac{1}{183} = 11.3$ kilolines per square centimetre.

Ampère-turns per centimetre of length = 13.

Ampère-turns at no load =  $13 \times 44 = 570$ . Flux density at full load =  $\frac{3.6 \times 10^6}{2} \times 1.2 \times \frac{1}{183} = 11.8$ 

kilolines per square centimetre.

Ampère-turns per centimetre of length = 15. Ampère-turns at full load =  $15 \times 44 = 660$ .

The ampère-turns per pole necessary for each component part of the magnetic circuit at no load and full load respectively are set forth in the following table:

Part.					No-load père-turns.	Full-load ampère-turns.
Armature	e			70	80	
Armature	th	•		640	850	
Air-gap . Magnet c		re .			2680	2800
	ore				630	820
Yoke .			•		570	6 <b>6</b> 0
			Total	•	4590	5210

When the armature is on open circuit, 4590 ampèreturns are sufficient to provide a flux of 3.45 megalines through the armature and maintain a terminal E.M.F. of 550 volts; but as the load increases the excitation must also be increased in the same proportion, until at full load the ampère-turns necessary to provide a flux of 3.6 megalines, generate a total E.M.F. of 572 volts and maintain a constant terminal E.M.F. of 550 volts, are 5210. These 5210 ampère-turns provide the necessary flux at full load on the assumption that the flux is evenly distributed over the respective cross-sections, but such is only the case when the armature is on open circuit. As is explained later, the magnet coils require to give an additional number of ampère-turns in order to counteract the demagnetising and distorting effects of the armature when the latter supplies current. particular machine the field ampère-turns necessary to overcome armature reaction are 660 (as given on page 328), so that the total calculated ampère-turns per pole at full load = (5210 + 660) = 5870, as against 4590 at no load.

If the dynamo be shunt-wound, then in practice each shunt coil would be designed to give a maximum of 6000 ampère-turns, thus compensating for any slight increase in the reluctance of the magnetic circuit due to an increase in the length of air-gap or variation in the composition of the iron. Attention is here directed to the fact that

of the total ampère-turns required at full load nearly 50 per cent. are utilised in overcoming the air-gap reluctance.

Calculation of Shunt Coils.—There are several useful methods available for calculating the size of wire required for the shunt field coils, two of which are given below:

Method 1.—To determine the size of wire required when the ampère-turns, volts per coil, and the mean length of one turn are known—

Let  $\rho$  denote the specific resistance of copper in ohms per centimetre cube, CT the ampère-turns per coil, V the available volts per coil, and L the mean length of one turn. The resistance of each coil is expressed by

$$R = \frac{V}{C} = \frac{\rho \times L \times T}{a}$$

where-

T = turns per coil.

a =area of cross-section of the wire.

C = current in coil in ampères.

Now 
$$a = \frac{\pi d^2}{4}$$
, so that  $\frac{V}{C} = \frac{\rho \times L \times T \times 4}{\pi d^2}$ .

Therefore the diameter of the wire in centimetres is expressed by  $d = \sqrt{\frac{4 \times \rho \times L \times CT}{\pi V}}$ .

Example.—Apply this formula to the above shunt winding, which has to give 6000 ampère-turns at full load. The bobbins on which the coils were wound were of such dimensions that the internal diameter of the winding was 20 centimetres, and the radial depth of winding 5 centimetres.

Mean diameter of winding = 20 + 5 = 25 centimetres. Mean length of one turn =  $\pi \times 25 = 79$  centimetres.

Suppose that at full load 30 volts are absorbed by the shunt regulating resistance (R, Figure 182), then the

available volts per coil =  $\frac{550 - 30}{4}$  = 130.

The specific resistance of copper at 60° C. (i.e. the probable working temperature of the coil) equals 0.000002 ohms per centimetre cube.

The diameter of wire then

= 
$$d = \sqrt{\frac{4 \times 0.000002 \times 79 \times 6000}{\pi \times 130}} = \sqrt{0.0093}$$
  
= 0.096 centimetre.

From Appendix I. it will be seen that No. 20 S.W.G., having a diameter of 0.0915 centimetre, is the nearest size of wire to that found by calculation. The wire in this case was triple-cotton covered, thus giving an overall diameter of 0.122 centimetre.

The shunt winding spools for this machine had an axial length of 17 centimetres, so that the turns per layer =  $\frac{17}{0.122}$  = 140, and since the radial depth is 5

centimetres, the number of layers =  $\frac{5}{0.122}$  = 41; say 43 after allowing for bedding.

The total turns on bobbin =  $140 \times 43 = 6000$ .

Therefore the shunt current =  $\frac{6000}{6000}$  = 1 ampère.

The resistance of a coil should now be calculated, and should approximately be equal to

$$\frac{V}{C} = \frac{130}{1} = 130$$
 ohms at 60° C.

Calculated resistance

= R = 
$$\frac{\rho \times l \times 4}{\pi d^2}$$
; but  $l = L \times T = 79 \times 6000$ ,  
so that R =  $\frac{0.000002 \times 79 \times 6000 \times 4}{\pi \times 0.0915^2}$  = 140 ohms.

Had the resistance of the winding thus calculated been greater than that given by  $\frac{V}{C}$  by say more than 8 per cent., the coil would have required to have been wound with a larger size of wire.

Method 2.—Another method largely used in practice is to make use of the formula

$$W = \frac{0.000176 \times L^{2} \times (CT)^{2}}{K},$$

where-

W = Watts per shunt spool at 60° C.

L = mean length of one shunt turn in metres.

CT = ampère-turns per spool.

K = kilogrammes of copper per shunt spool.

This formula is derived as follows:

Let l = length of wire, in metres, forming the winding. s = area of cross-section of wire in square centimetres.

 $\rho$  = specific resistance of copper at 60° C., then the resistance of the winding is expressed by

$$R = \frac{\rho \times l \times 100}{s} = \frac{0.000002 \times l \times 100}{s},$$
*i.e.*  $s = \frac{0.0002}{R}.$ 

Multiplying both sides the equation by l

$$sl = \frac{0.0002 \times l^2}{R}.$$

Further, let L = mean length of 1 turn in metres, T = number of turns in the winding, C = current in ampères,

then

$$l = LT$$
,  
and  $sl = \frac{0.0002 \times L^2 \times T^2}{R} = \frac{0.0002 \times ^2L \times C^2 \times T^2}{C^2R}$ .

Now  $sl \times 100 = \text{volume}$  of copper in cubic centimetres, and  $\frac{sl \times 100 \times 8.9}{1000} = \text{mass}$  per shunt spool in kilogrammes = K.

 $C^2R$  = watts per shunt spool at 60° C. = W. CT = ampère-turns per shunt spool.

Therefore

$$K = \frac{sl \times 100 \times 8.9}{1000} = \frac{0.0002 \times L^{2} \times (CT)^{2} \times 100 \times 8.9}{1000 \text{ W}},$$
i.e. 
$$W = \frac{0.0002 \times L^{2} \times (CT)^{2} \times 100 \times 8.9}{1000 \times K}$$

$$= \frac{0.000178 \times L^{2} \times (CT)^{2}}{K}.$$

The procedure for calculating the size of wire for the field winding of the above example is as follows:

Cross-section of shunt spool winding =

radial depth  $\times$  axial length =  $5 \times 17 = 85$  square centimetres.

Space factor of shunt spool = (say) o. 5.

Cross-section of copper in shunt spool= $85 \times 0.5$ = 42.5.

Volume of copper in shunt spool =  $42.5 \times L = 42.5 \times 79$ = 3350 cubic centimetres.

Since I cubic centimetre of copper = 0.0089 kilogrammes, the kilogrammes of copper in shunt spool =  $3350 \times 0.0089 = 29.5$ .

Watts per shunt spool

$$= \frac{0.000178 \times 0.79^{2} \times 6000^{2}}{29.5} = 134 \text{ watts.}$$

Ampères per shunt spool (assuming as before that 30 volts are absorbed by the shunt-regulating resistance)

$$= \frac{\text{watts per spool}}{\text{volts per spool}} = \frac{134}{130} = 1 \text{ ampère.}$$

Turns per shunt spool = 
$$\frac{6000}{1}$$
 = 6000.

Sectional area of copper per turn

cross-section of copper on shunt spool winding turns per spool

$$=\frac{42.5}{6000}$$
 = 0.007 I square centimetre.

Diameter of bare wire = 0.095 centimetre.

Thus the size of wire determined by this method is the same as that determined by the first.

# ARMATURE REACTION

In order to get sparkless commutation the brushes require to be placed in such a position that the armature turns between the commutator segments under the brushes are approximately on a geometrical neutral axis, *i.e.* a radius of the armature which bisects the angle contained by the radial axes of two adjacent poles, as represented by the line ob (Figure 199). It is necessary to distinguish

this geometrical neutral axis from the axis of commutation, which is a radius of the armature passing through points of contact of the brushes, as indicated by the line COC (Figure 199). In the foregoing diagrams, for the sake of simplicity of statement, the armature inductors are represented as being placed equidistantly apart upon the armature core and connected radially to their commutator segments. In actual drum armatures the connections to the commutator segments are made at the centre of the end connections (see Figures 147 and 148), so that the true axis of commutation, in a machine whose number of poles is 2p, is displaced  $\frac{90^{\circ}}{2p}$  relative to

the brushes, but in both

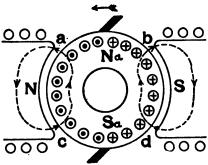


Fig. 195. – Magnetic field due to armature.

2 - pole and multipolar machines the axis of commutation refers to the position of the coils undergoing commutation, and not to the corresponding position of the brushes.

Figure 195 represents the armature of a 2-pole dynamo in which the axis of commutation is coincident with the geometrical

neutral axis. When the armature supplies current the inductors on either side of the brushes will have currents flowing in them in opposite directions. The inductors marked with a dot are supposed to carry current flowing towards the reader, while those marked with a cross carry current in the opposite direction.

Each inductor may be imagined as connected across—in a plane at right angles to the plane of the geometrical neutral axis—to a corresponding inductor on the opposite side of the armature. The latter becomes an electro-magnet, the coils of which magnetise the core in a direction parallel to the plane of the geometrical neutral axis, as indicated by Na and Sa, which extend along the entire length of the core. The

lines of force set up by the armature pass through the core on either side of the neutral axis, and emanating from the upper part pass through the poles and enter again at the lower part, as shown in the figure.

Cross Ampère-turns.—The path taken by the

magnetic flux set up by the field magnets is shown in Figure 196, from which it will be observed that at a and d the lines of force in the air-gap due to the armature current are in the opposite direction to the field magnet lines of force, while at b and c they are in the same direction. If the arrow indicates the

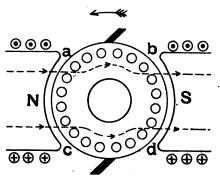


Fig. 196.—Magnetic field due to field magnets.

direction of rotation of the armature, then the pole tips a and d, which are approached by the armature inductors as they move through the interpolar gap, are referred to

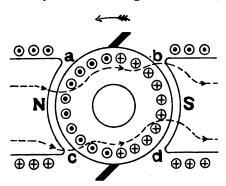


FIG. 197.—Magnetic field of a dynamo distorted by armature field.

as the leading pole tips, distinguish from the trailing pole tips c and b from which the inductors recede when entering the interpolar space. superimposing the two magnetic fields, combined field shown in Figure 197 is obwhich tained, sents the resultant distribution of flux as

actually occurring in a dynamo supplying current.

The result of the reaction of the armature current is that the main flux is distorted in the direction of rotation, and the flux density in the air-gap under the trailing pole tips is increased, while the flux density in

the air-gap under the leading pole tips is diminished. Since the flux produced by the armature current is in a direction at right angles to the main flux it is termed a cross-flux, and the ampère-turns which produce it are

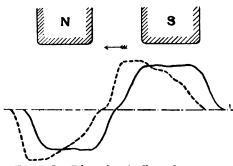


FIG. 198.—Distortional effect of armature.

known as the cross ampère-turns of the armature. In Figure 198 the line curve shows the distribution of flux in the air-gap of a 4-pole machine when the armature current was and the dotted curve shows

flux distribution for the same machine when the armature carried the full-load current, the ordinates of the curve representing the strength of the magnetic flux.

From these curves it will be observed that the plane

of neutral flux has become distorted, so that in order to obtain perfect commutation the brushes require to be moved forward through an angle  $\theta$  (Figure 199) in the direction of rotation. The angle between the commutation and the geometrical neutral axis is known as the angle of lead or lag, according as the angular displacement of the brushes is

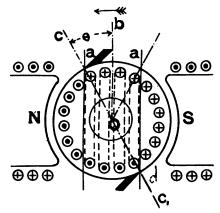


FIG. 199.—Demagnetising and cross ampère-turns of 2-pole armature.

coincident with, or opposite to, the direction of rotation. In a dynamo the brushes are given lead, while in a motor they are given lag, or backward lead as it is sometimes called.

Demagnetising Ampère-turns.—The effect of giving

lead to the brushes of a dynamo can be studied from Figure 199, the direction of the currents in the armature and field coils being indicated by the crossed and dotted circles. The inductors can be divided into two groups by the lines a a, which are drawn perpendicular to the direction of the magnetic flux of the field magnets and pass through the forward tips of the two brushes. The angle a o a therefore equals twice the angle of lead, i.e.  $2\theta$ . Each group of inductors can be imagined as connected together across the ends of the armature so as to form two sets of windings, the imaginary end connections of the coils within the zone a a alone being shown.

The ampère-turns included between the lines a a act in the opposite direction to the ampère-turns on the field coils, and as they neutralise to a certain extent the action of the field-turns, they are known as the demagnetising or back ampère-turns of the armature. The second zone of ampère-turns, made up by the inductors outside the zone a a, have simply a cross magnetising effect, as is the case with all the ampère-turns when the neutral and commutation axes are coincident. Should the brushes be given an angle of lead of 90 degrees, the armature will be incapable of generating current; but if in this position current be sent through the armature, the effect of armature reaction would be purely demagnetising, there being no component tending to cause distortion.

Armature Reaction in Multipolar Machines. — Multipolar dynamos can similarly have their armature ampère-turns divided into groups, each group either having a distorting or demagnetising effect on the main field, as shown in Figure 200, where the brushes are at an angle  $\theta$  in advance of the geometrical neutral axis OA.

The value of the demagnetising ampère-turns of the armature per pole is found by multiplying half the number of inductors within the angle 2  $\theta$  by the current flowing in each, and is expressed by

$$AT = \frac{I}{q} \times \frac{C}{2} \times \frac{2\theta}{360},$$

where—

I = full-load armature current,

q = number of circuits through armature,

 $\dot{C}$  = total number of armature inductors.

Similarly with an angle of lead  $\theta$ , the value of the cross ampère-turns of the armature

 $=\frac{I}{q}\times\frac{C}{2}\times\left(\frac{360^{\circ}}{2p}-2\theta\right)$ , where 2p is the number of poles.

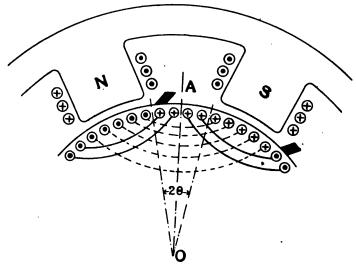


FIG. 200.—Demagnetising and cross ampère-turns of a multipolar armature.

Field Ampère-turns to overcome Armature Reaction.

—The demagnetising ampère-turns which are set up by the armature must be counteracted by an equal number of ampère-turns on the field coils.

In dynamos where the armature teeth are nearly saturated, the effect of distortion is to decrease the permeability of the teeth, so that the main flux is diminished and consequently the induced E.M.F. of the armature. The field ampère-turns must therefore be further increased to compensate for the diminution in the effective flux passing through the armature resulting from armature reaction. The increased field ampère-

turns to overcome this distortion effect are rather difficult to calculate, but experiments have shown that they are a function of the total distorting ampèreturns and the ampère-turns for the teeth and airgap.

Let D denote the total distorting ampère-turns per pole, F the field ampère-turns for overcoming the latter, and G the ampère-turns required for the teeth and air-

gap. As the results of tests on various types of machines it has been found that, for the usual values of flux density in the F armature teeth and D air-gap, if the ratio F/D be plotted as a function of the ratio D/G, the points will lie approximately along the shown in Figure 201. This curve can therefore be employed for determining the value of F.

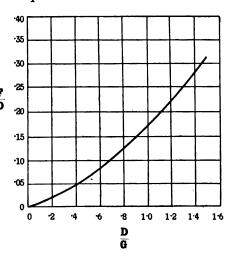


FIG. 201.—Curve for calculating the influence of distorting ampèreturns.

Example. — The

brushes of the 33-k.w. dynamo previously referred to have a fixed lead of 7 degrees. It is required to find the number of ampère-turns per pole to counteract the effects of armature reaction.

Full-load current (I) = 60 ampères.

Number of circuits in parallel (q) = 2.

Total number of inductors (C) = 724.

The demagnetising ampère-turns per pole at full load

$$=\frac{60}{2}\times\frac{724}{2}\times\frac{14}{360}=430.$$

Additional ampère-turns per pole at full load to overcome armature demagnetising action = 430. The total ampère-turns per pole at full load

$$= \frac{60}{2} \times \frac{724}{2} \times \frac{1}{4} = 2700.$$

Hence the demagnetising ampère-turns of armature

= 
$$430 \times \frac{100}{2700}$$
 = 16 per cent.

Distorting ampère-turns per pole at full load = D = 2700 - 450 = 2270 = 84 per cent. of total.

Ampère-turns required for teeth at full load = 800 (vide p. 315).

Ampère-turns required for air-gap at full load = 2950 (vide p. 315).

Ampère-turns required for teeth and air-gap = G = 800 + 2850 = 3650.

The ratio D/G = 2270/3650 = 0.63.

From Figure 201 the ratio  $\frac{F}{D} = 0.1$ .

The field ampère-turns to overcome distortion  $= F = 0.1 \times D = 0.1 \times 2270 = 230$ .

Therefore total field ampère-turns to overcome armature reaction = 430 + 230 = 660.

From this example it will be seen that the armature reaction increases the amount of copper required in the field-magnet coils, and also the amount of iron in the magnetic circuit, owing to the resultant increase in the length of the magnet core; this in turn tends to increase the amount of magnetic leakage, and therefore the cross-section of the magnetic circuit.

In modern dynamos it is required that they shall deliver, without undue sparking, any load up to a percentage considerably in excess of their full-rated output with the brushes in a fixed position. To satisfy this requirement the brushes are set with a permanent angle of lead varying, according to the output of the machine, from 6 to 15 per cent. of the angular distance between two successive geometrical neutral planes. The method of determining the necessary angle of lead of the brushes is discussed when dealing with commutation, and within the limits given above the demagnetising ampère-turns

vary between 12 and 30 per cent. of the total. Until a few years ago it was looked upon as a matter of course that the brushes of any dynamo should be shifted forward in proportion to the load; but a better understanding of the theory of commutation has made it possible to design machines in which the above requirements as to fixed brush position can be adhered to.

Methods of reducing Armature Reaction.—The distortion of the magnetic field can be reduced by increasing the length of air-gap and by so dimensioning the teeth and slots that the former are highly saturated by the field flux. This procedure, besides increasing the reluctance in the path of the cross-magnetic flux of the armature, also increases the reluctance offered to the main flux, so that the main ampère-turns must be augmented. This will then make the field ampère-turns strong in comparison with those of the armature, with the result that the distortional effect of the armature is reduced. There is, however, a limit to the length of air-gap which is reached when the increased cost of copper on the field magnets outweighs the advantage of further reduction in the distortion effects.

In Figure 195 it was shown that the cross-flux due to the armature passes through the poles in a direction at right angles to the main flux; consequently a high

reluctance may be introduced in the path of the cross-flux by forming a long narrow slot, parallel to the axial length of the magnet core, along its centre, as shown at A in Figure 202. This will have but a small effect on the main flux. while an additional air-gap is introduced into the path of the crossflux.

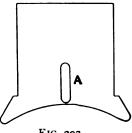


FIG. 202.

The best method of counteracting armature reaction is by means of a compensating winding on the main poles, which acts in the opposite direction to the cross ampère-turns of the armature. This is dealt with in the latter portion of this chapter.

Number of Poles required for a Machine of given output.—As a consequence of armature reaction it becomes not only desirable but necessary to limit the armature strength to such an amount at full load as shall not greatly interfere with the distribution and amount of the magnetic flux set up by the field magnets. With such values of flux density and air-gap length as have been previously recommended, experience shows that the best results are obtained from machines in which the armature strength at full load does not exceed from 5500 to 9000 ampère-turns per pole, when the output ranges from 100 k.w. or less, to 1500 k.w. respectively.

If T be the number of turns per circuit through the armature, and I the total current output of the machine, then in a lap-wound armature T equals the number of armature turns per pole, the number of circuits through the armature being the same as the number of poles. Further, if p denote the number of pairs of poles, the current flowing in each circuit of the armature equals  $\frac{I}{2p}$ , and therefore  $T \times \frac{I}{2p}$  gives the number of ampère-turns per pole. Let  $AT_a$  denote the maximum permissible value of the armature ampère-turns at full load, then the number of pairs of poles required for a lap-wound armature is given by

$$T \cdot \frac{1}{2p} = AT_a.$$

From the E.M.F. equation  $T = \frac{E \times 10^8}{4 \times \frac{R}{60} \times M}$ , so that

$$\frac{E \times 10^8}{4 \times R \cancel{p} \times M} \times \frac{I}{\cancel{2}\cancel{p}} = A T_{\cancel{n}}.$$

Let d and l denote the diameter and length of armature respectively, and r the ratio of the length of polar arc to polar pitch; then the total pole face area

$$=\pi d\times r\times l.$$

Further, if B<sub>a</sub> denote the average flux density in the

air-gap at full load, then M the flux per pole entering the armature is expressed by

 $M = \frac{\pi d \times r \times l \times B_a}{2p}$ . Substituting this value of M in the above equation

$$\frac{E \times 10^8 \times 2p \times 60}{4 \times R \times p \times \pi d \times r \times l \times B_a} \times \frac{I}{2p} = AT_a.$$

The number of pairs of poles is therefore expressed by

$$p = \frac{E \times I}{R \times d \times l} \times \frac{1}{B_a \times AT_a \times r} \times \frac{10^8 \times 60}{4\pi}.$$

In low and medium speed machines the flux density  $B_a$  in the air-gap does not usually exceed 8500 lines per square centimetre, and the ratio of polar arc to polar pitch is in most cases equal to 0.7, so that substituting these values of  $B_a$  and r in the above equation

$$p = \frac{E \times I}{R \times d \times l} \times \frac{I}{AT_a} \times \frac{10^8 \times 60}{8500 \times 0.7 \times 4\pi}$$
$$= \frac{E \times I \times 80000}{R \times d \times l \times AT_a}.$$

From this equation it will be observed that the number of poles is inversely proportional to  $(d \times l)$ , the component parts of which may be determined in a manner discussed on page 447.

In order to keep the armature iron losses in turbodriven dynamos within reasonable limits, the flux density in the air-gap is limited to about 7000 lines per square centimetre, and as the average ratio of pole pitch to polar arc may be taken as 0.6, the number of pairs of poles is expressed by

$$p = \frac{E \times l \times 110000}{R \times d \times l \times AT}.$$

Example.—A dynamo has to be designed to give an output of 440 ampères at 500 volts (i.e. 220 k.w.). If the armature is 90 centimetres in diameter, 30 centi-

metres in length, and makes 380 revolutions per minute, determine the number of poles.

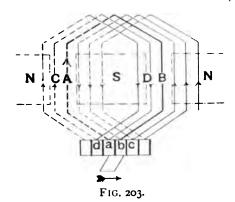
For this size of machine the armature ampère-turns per pole (AT<sub>a</sub>) should be limited to about 6000, so that the number of pairs of poles is approximately given by

$$p = \frac{500 \times 440 \times 80000}{380 \times 90 \times 30 \times 6000} = 2.9.$$

Taking the nearest integer p = 3, i.e. the machine will have 6 poles.

#### COMMUTATION

Commutation is that process whereby the current in an armature coil, as it passes from one side of the axis of commutation to the other, is reduced to zero, and



a reversed current built up equal in value to the current in the circuit of which it is about to become a part. This process must take place in such a manner that no appreciable sparking occurs between the brushes and commutator segments.

In Figure 203 is

shown a portion of a lap-winding. For the sake of simplicity it is assumed that the width of contact of the brushes on the circumference of the commutator is equal to the width of a segment. Thus each brush only short circuits one armature coil at a time. In an actual machine the brushes have an arc of contact sufficient to bridge over three or four segments. The armature rotates from left to right as indicated by the arrow, so that when the commutator segments a and b are on the left-hand side of the brush the current in the coil AB is flowing through it towards the brush, as

indicated by the arrow-heads on the coil CD. Once in every revolution the coil AB will be short-circuited under the brush, and when the segment B passes from underneath it the coil thus short-circuited will be carrying a current in the reverse direction, but still flowing towards the brush. During the small interval of time in which a coil is under the brush the previous existing current should diminish to zero, and a reversed current of equal strength be established. This change in the direction of the current is depicted in Figure 204; the width of the shaded part represents the time during

which the coil is short-circuited under the brush, and the ordinate 2A the change in the value of the current.

Reactance Voltage. — When the current flowing in a circuit is suddenly altered a change is produced in the number of lines of force linked with that circuit, and any change in the

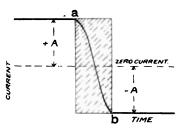


FIG. 204.—Diagram of perfect commutation.

number of lines of force is accompanied by an induced E.M.F. This induced E.M.F. tends to oppose the change in the value of the current, and is known as the E.M.F of self-inductance. The phenomenon as a whole is called self-induction. The number of lines of force linked with a circuit when carrying unit current is called the *coefficient of self-inductance*. The henry or practical unit of self-inductance equals 109 absolute units.\*

From this it will be seen that the reversal of the current in the short-circuited coil is accompanied by a change in the magnetic flux linked with the coil, and consequently an electromotive force is induced in it which tends to oppose the reversal of the current. This counter E.M.F. is termed the reactance voltage, and is expressed by the formula

$$V = 2 \pi n L C$$
.

<sup>\*</sup> Those wishing to further study the subject of self-induction are referred to text-books on Alternating Currents.

where---

n = periodicity of reversal (i.e. the number of complete cycles per second).

L = inductance (in henrys) per coil or commutator segment.

C = current per circuit.

This formula is based upon the assumption that the current in the short-circuited coil is a sine function, i.e. the curve a b (Figure 204) is supposed to represent half a sine curve, and the current is treated as reversing like an ordinary alternating current. Such an assumption is probably far from correct, but nevertheless it affords a basis upon which all machines may be similarly calculated, and its value has been found to be a sufficiently good criterion for the quality of commutation. The shape of the current and time curve is influenced by such considerations as shaping of the pole tips and armature interference, but up to the present there is no reliable experimental data on this subject.

For determining the value of n, let s denote the peripheral speed of the commutator in metres per second, l the length of the arc of brush contact in centimetres: then the time during which any one coil is short-circuited by the brush =  $\frac{l}{100 \text{ s}}$  seconds. During this time the current in the coil goes through one-half of a complete cycle (see Figure 204), so that the average periodicity of reversal in complete cycles per second is expressed by

$$n = \frac{100 \text{ s}}{2l}.$$

The inductance (L) per coil is given by the product of the number of lines of force (M), per ampère of current, linked with each turn, and the number of turns (t) squared, i.e.

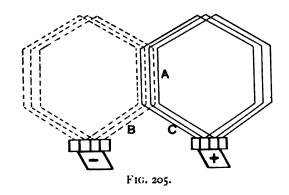
L=M .  $\emph{t}^{2}/\text{10}^{8}$  henrys.

With a view to forming a basis for estimating the value of L, Hobart\* performed a series of experi-

<sup>\*</sup> Journal of Institution of Electrical Engineers, vol. xxxi. pp. 170-217 (1901).

ments, and with present-day types of machines, where the depth of a slot is about three times the width, has shown that there will be set up on an average (1) 4 lines of force per ampère per centimetre of embedded length, and (2) 0.8 lines of force per ampère per centimetre of free length. The embedded length is that portion of the coil lying in a slot, and the free lengths are the end connections, and included with them should be those portions of the inductors not strictly iron-clad, i.e. the length of inductor corresponding to ventilating ducts and insulation between laminations.

If there be m turns short-circuited under one brush,



then the lines of force per centimetre of embedded length, linked with any one of the short-circuited coils, will be due to 2m turns; whereas the lines of force per centimetre of free length are set up by m turns. That this is so, will be evident from Figure 205. In the embedded portion, the inductors short-circuited under the positive brush lie near to or in the same slot as those inductors simultaneously short-circuited by the negative brush, as shown at A; consequently there will be a mutually inductive action. The two corresponding groups of end connections B and C are located separately. The method of calculating L is set forth in the following example.

Example.—Calculate the reactance voltage at full load of an armature having the following constants:

Diameter of commutator = 0.45 metres. Speed = 660 R.P.M.

Number of commutator segments = 357.

Length of arc of brush contact
Mean length of one turn

Effective length of core

= 0.65 centimetres.
= 152 centimetres.
= 14.8 centimetres.

Turns per commutator segment = 1.

Full load current = 60 ampères.

Number of armature circuits = 2.

Peripheral speed of commutator (s)

$$= \pi \times 0.45 \times \frac{660}{60} = 15.5 \text{ metres per second.}$$

Periodicity of reversal (n)

$$= \frac{100 \times 15.5}{2 \times 0.65} = 1190.$$

Embedded length per turn

= 2 × effective length of core =  $2 \times 14.8 = 29.6$  centimetres.

Free length per turn

= mean length of one turn -29.6 = 152 - 29.6

Lines per ampère-turn of embedded length

 $= 29.6 \times 4 = 118.$ 

Lines per ampère-turn of free length

 $= 122.4 \times 0.8 = 98.$ 

Maximum number of coils short-circuited under one brush

= Length of arc of contact Width of segment+insulation

$$= \frac{0.65}{\pi \times 45} = 1.65.$$

357

Number of turns short-circuited per brush

=  $1.65 \times 1 = 1.65$  (taking nearest integer) = 2.

Lines per ampère for embedded length

 $= 118 \times 2 \times 2 = 472.$ 

Lines per ampère for free length

 $= 98 \times 2 = 196.$ 

Total lines linked with the short-circuited coil per ampère = 472 + 196 = 668.

$$=\frac{668}{10^8}$$
 = 0.0000668.

Current per circuit (C)

$$=\frac{60}{2}$$
 = 30 ampères.

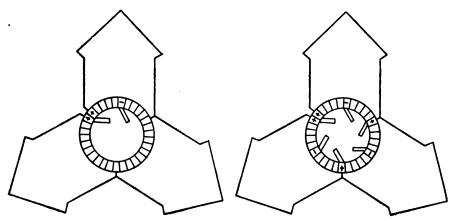
Reactance voltage

$$= V = 2 \pi n \tilde{C}L$$

$$= 2 \pi \times 1190 \times 0.00000668 \times 30$$

= 1.5 volts.

Reactance Voltage of a 2-Circuit Winding.—The value of the reactance voltage of a 2-circuit winding



FIGS. 206, 207.—Reactance voltage of 2-circuit windings.

depends upon the number of sets of brushes employed. To illustrate the case of a 6-pole armature, consider Figure 206, which is a diagram showing those-inductors, of the winding represented in Figure 147, temporarily undergoing short-circuit at the positive brush. The coil short-circuited by the positive brush consists of 3 turns (i.e. 6 inductors) in series, and if V denote the reactance voltage per turn the reactance voltage per coil equals 3V.

Next suppose that the commutator is fitted with as many sets of brushes as there are poles, *i.e.* 6. Under such conditions each pair of inductors is short-circuited

by the cable which connects brushes of similar polarity, as shown in Figure 207. There are now three independent circuits, each consisting of one turn, and the reactance voltage per commutator segment is reduced to V; consequently the commutation will be much better than that obtained when only two sets of brushes are fitted.

Reversal of the Current by a Reversing E.M.F.—In order to effect sparkless commutation the brushes may be set in such a position that during the time the coil AB (Figure 203) is short-circuited it is cutting a magnetic flux in such a direction that a reversed E.M.F. is induced in it: this latter E.M.F. should be sufficient to first reduce to zero the current previously existing in the coil, and then—still in opposition to the reactance voltage—to induce a current in the coil in the opposite direction, which at the instant the short circuit is removed shall have attained a strength equal to that of the current in the circuit which the coil is about to enter.

At no load there will be no current to reverse, and hence no reactance voltage to overcome, so that perfect commutation is obtained when the short-circuited coil is in neutral field, *i.e.* when the axis of commutation is coincident with the geometrical neutral axis. But when the armature supplies current it is necessary to move the brushes forward by an amount depending on the load, so that the short-circuited coil shall be cutting the fringe of the flux in the air-gap under the leading pole. (In Figure 203 the coil AB is shown short-circuited when nearer to the leading pole than to the trailing pole, *i.e.* the short-circuited coil is entering the fringe of the former's field.)

It will now be clear that as the armature current increases a stronger field will be necessary to commutate this stronger current and overcome the correspondingly greater reactance voltage. But, as has already been explained, this stronger current flowing through the armature distorts the neutral magnetic field into a position in advance of the brushes, so that in order to bring the short-circuited coil into a sufficiently strong

reversing field the brushes require to be given a greater angle of lead than that which would be necessary if there were no distortion. This increased angle of lead will in turn increase the demagnetising effect of the armature, so that finally a load will be reached at which sparkless commutation becomes impossible, owing to the absence of a sufficiently strong reversing field to commutate the current.

Position of the Brushes.—With machines of present-day design, the practice of permitting different brush positions for different loads has been abandoned, and there must be a fixed brush position at all loads. With electro-magnetic commutation described above, perfect commutation can only occur at some intermediate value of the load. The usual practice is to set the brushes with as much forward lead as is possible, without incurring sparking at no load, and to limit the output of the machine, if thermal considerations permit, to that load which does not produce sparking when the brushes are in this position.

At no load, half load, and full load the variation of current in the short-circuited coil will be somewhat as shown in Figure 208. At no load the reversing field will build up an induced current to the strength represented by -C, with the result that as the segment leaves the brush the current falls abruptly to zero. This sudden cessation of current in an inductive circuit sets up an E.M.F. between the brush and commutator segment, which tends to produce a spark at the point of separation. This latter E.M.F. may be called the *sparking E.M.F.*, and should not be confounded with the reactance voltage already referred to.

At half load the tendency to spark is eliminated, as the electromotive force set up by the reversing field is of just sufficient strength to reverse the direction of the current and overcome the reactance voltage.

At full load the coil is in a weak reversing field—the latter having been distorted due to the increased armature reaction—so that as the segment is about to leave the brush the reversed current has not attained a strength equal to that of the circuit which the coil is about to

enter. Hence, at the moment of leaving the brush there is an abrupt change in the current from a value — B to a value — 2A, which in turn gives rise to a sparking E.M.F., and the former should be of such a strength that the latter does not produce appreciable sparking.

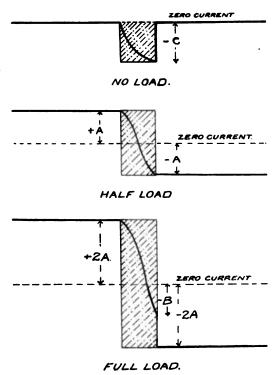


FIG. 208.—Diagram of commutation.

It must be understood that the variation of current in the short-circuited coil may not be exactly as shown, but, in the absence of more definite data, these diagrams may convey to the student an idea of what is likely to occur.

From this reasoning it will be clear that the less the inductance of each coil the greater can be the change in the strength of the short-circuited current at the instant the segment passes from underneath the brush, and consequently the greater will be the limiting output of the machine in so far as sparking is concerned. Now

the inductance is proportional to the square of the number of turns, so that for low-reactance voltages it is necessary to have few turns per commutator segment. For moderate-sized machines one or two turns per commutator segment is considered good practice.

An examination of the various quantities involved in the reactance voltage formula will show the desirability of large diameters and small core lengths from the commutation standpoint. This is due to a combination of several features. With a large diameter a larger number of commutator segments is possible, and, consequently, for a given number of armature inductors a smaller number of turns per segment can be employed, giving a small inductance per coil. Shorter core lengths also tend to a reduction in inductance by reason of the shorter lengths of conductors embedded in the iron.

Since the frequency of commutation is inversely proportional to the length of brush arc, it will be evident that the width of brush should be as large as practicable. This, however, is limited by the number of segments it is permissible to cover. If the brush can only bridge across two segments at a time, then it short-circuits one coil, and the lines linked with the coil are due only to the current flowing in its own turns. If, on the other hand, the brush can bridge over three segments, it short-circuits two coils, and the lines linked with one coil are due to the current flowing in the turns of both coils. Thus the width of a brush is limited in that it is not desirable to cover more than three segments in order to keep down the inductance of the short-circuited turns. In ordinary cases the frequency of commutation ranges from 200 to 800, though in some machines it may be much higher than this, as was the case in the numerical example considered.

When carbon brushes are used, the limiting values of reactance voltage for sparkless commutation may be taken as ranging from 1.5 volts in small machines to 4 volts in machines of 500 k.w. or more; but the liability of a machine to spark will depend greatly upon

the type of brush employed. Again, machines of most recent design are fitted with commutation poles, and they may permit of the armature having a reactance voltage

as high as 20.

Advantage of a High-Resistance Brush.—Figure 209 is a diagram of connections showing three armature coils A, B, and C, connected by commutator lugs to segments a, b, c, and d. The coil B is shown under the brush D, and the direction of the current in the coils on each side of the brush is as indicated by the arrow-heads. Suppose the armature to revolve from right to left. At the instant the coil B is short-

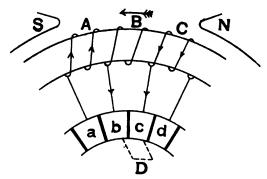


FIG. 209.—Effect of high-resistance brush in forcing commutation.

circuited it is carrying a current of the value, say, +I, and flowing in the direction shown in the coil C. This current must first be reduced to zero, and the change can be accelerated by short-circuiting the coil with a brush of high-contact resistance. The building up of a reversed current to a value -I is also accelerated by a high-resistance brush in the following manner:

When the commutator has moved round so that the brush is in the position shown, the area of contact of the latter with the trailing segment b is reduced, consequently the increased resistance thereby introduced between the coil A and the brush tends to divert the current in the lug of segment b to the alternative path formed by the coil B and segment c, *i.e.* the high resistance offered by the diminished area of brush con-

tact tends to reverse the current in the short-circuited coil, or it forces commutation.

Owing to the greater contact resistance of carbon over metal, brushes of hard graphitic carbon are now invariably used, although metal brushes are often preferred for high-speed turbine-driven dynamos. A more complete discussion of the relative advantages of metal and carbon brushes is given in Chapter XII., under the heading of Commutator Losses.

With electro-magnetic commutation, where the brushes are adjusted to give perfect commutation at somewhere near half load, carbon brushes tend to counteract the possibility of sparking at no load and full load, due to the excess and deficiency respectively in the strength of the reversed current.

Forced Commutation.—Another procedure is to design a machine to have a low-reactance voltage and resort to forced commutation, i.e. where the current does not die down to zero by the action of a reversing E.M.F. in the short-circuited coil, but is merely throttled by the decreasing area of contact between segment and brush, as described above. Carbon brushes must necessarily be used, and they are fixed in positions at the geometrical neutral axes. For forced commutation it is preferable to have as small a leakage field as possible in the interpolar space, so as to diminish the strength of the circulating currents in the short-circuited coils. This can be best obtained by having a narrow air-gap and a polar arc of about 65 per cent. of polar pitch.

At all loads the current will not have reversed and risen to a strength equal to that of the circuit which it is about to enter when the short-circuited coil passes from underneath the brush. The consequence is that an abrupt change in the current takes place, and in all such cases there will be a tendency to produce a spark. The sparking E.M.F., resulting from this sudden change in the current, is, however, curtailed by designing the armature to have a low reactance, and a useful criterion is that the reactance voltage, as determined in the manner previously described, should not exceed from 2 to 2.5 volts.

## COMMUTATION POLE MACHINES

In large dynamos for steam turbine speeds the reactance voltage per segment cannot be maintained within practical limits by the ordinary methods of design. Thus in all such machines where the output was limited by the question of sparking, and not the consideration of temperature, it soon became obvious that to obtain satisfactory commutation, recourse had to be made to some form of compensating winding, either on the armature or field coils, or to auxiliary magnetic poles placed between the main poles.

W. B. Sayers in 1892 proposed the introduction of compensating coils in the armature winding: the coils between any two segments to be so placed that they moved under a main pole, while the armature coil between those segments was undergoing commutation, and had induced in them a voltage equal and opposite to the reactance voltage. Owing, however, to the large

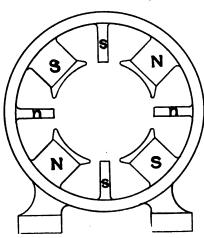


FIG. 210.—Field-magnet frame with commutation poles.

amount of inactive copper involved and the somewhat complicated nature of the winding, this method was not adopted to any considerable extent.

The employment of auxiliary poles has since proved to afford a more satisfactory solution of the commutation problem, and has now a widely extending field of application. The auxiliary poles ns, generally called commutation poles,

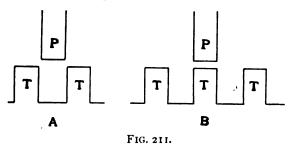
are fixed midway between the main poles NS, as shown in Figure 210, and their exciting coils connected in series with the armature, which will rotate in a counter-clock direction. In special cases, where it is not at all times desirable to pass the full main current through the auxiliary

coils, the latter are shunted by means of an adjustable low resistance commonly called a diverter.

Dimensions of Commutation Poles.—The commutation poles may be either of cast steel or built up of sheet-steel laminations bolted on to a machined seating on the yoke exactly in the centre of the interpolar space, as shown in Figure 210.

Polar Arc.—The length of the polar arc is such that during the whole period a coil is short-circuited by the brush it cuts the flux of the auxiliary pole, and as the short-circuited coil is about to pass from under the brush, it moves in a sufficiently strong reversing field to set up a current equal in strength to the current in the circuit it is about to become a part of.

A machine having a narrow commutation pole arc



has the advantage over a machine with a larger pole arc, in that it will have a comparatively small leakage coefficient, and, in addition, there will be a larger space between the auxiliary and main field coils, thus, owing to improved air circulation, a lower temperature rise is ensured. So far as the commutation of the current is concerned, it is essential that the pole arc be not too narrow, otherwise rapid fluctuations in the strength of the auxiliary field will result. That this is the case will be made clear from Figure 211, where the auxiliary pole arc is represented as being equal to the slot width. The magnetic reluctance of the path of the auxiliary flux will vary considerably as the armature teeth T pass under the pole P, being considerably greater in position A than in position B. In the former position the value of the flux will be much less than in the case of the latter, and part of the coils which are undergoing commutation will lie outside the influence of the auxiliary field. Under such conditions it will be impossible to obtain fair results, particularly with high-speed machines.

These bad features are improved or made worse as the radial depth of air-gap is increased or decreased, the flux variation being less, and the fringing effect greater, the longer the air-gap. As a rule, machines having a very narrow commutation pole arc are liable to hunt or flash over at the brushes, due to the consequent increase in the maximum voltage between adjacent commutator segments which occurs when there is a sudden variation in the load. Even at constant loads commutation will be accompanied by undue sparking, resulting in every third segment or so, according to the number of segments per slot, being blackened. Usually two or three segments are simultaneously under the brush, and the polar arc should cover as many slots as are carrying short-circuited inductors. practice is to have a 30 to 40 per cent. larger polar arc than this, and so allow for any distortion of the auxiliary flux which is liable to occur with varying loads.

Professor Arnold recommends a polar arc equal to at least twice a slot pitch. The arc of the commutation pole must not, however, occupy too great a percentage of the interpolar gap, if magnetic leakage, and, consequently, the copper on the auxiliary poles, has to be kept within reasonable limits. On an average the arc of the auxiliary pole occupies between 35 and 40 per cent. of the interpolar arc. The higher the reactance voltage the wider should be the auxiliary pole arc, and the greater the number of teeth covered by the latter.

Pole Shoe Length.—The axial length of the commutation pole shoe will depend upon the value of the reactance voltage, and hence also upon the flux density employed in the air-gap. It is better to reduce the axial length as much as possible, and thereby reduce magnetic leakage. In practice the axial length of the pole shoe ranges from 50 to 75 per cent. of the axial length of the armature core. When the average value of the flux per centimetre of armature periphery has

been determined, the length of pole shoe is settled by dividing the value obtained by the flux density most suitable for the conditions. The average flux density in the air-gap under the commutation pole generally ranges from 5000 to 8000 lines per square centimetre.

Area of Cross-section of Pole Core.—From a knowledge of the width of polar arc, axial length of pole shoe, permissible flux density (B) in the air-gap, and the dispersion coefficient for the auxiliary poles, the value of the flux in the pole core can be estimated. Since the reactance voltage increases directly with the armature current, the reversing field due to the auxiliary pole should also increase at the same rate. In order to effect this it is essential that the auxiliary poles do not reach their saturation value before full load is attained, otherwise there will be insufficient reversing E.M.F. and sparking will ensue. The crosssection of the pole core should therefore be dimensioned with a view to fulfilling this condition. To observe this latter consideration the flux density in the pole core at full load should not exceed 14,000 lines per square centimetre. In order to reduce the surface area from which leakage can take place, and also the length of copper per mean turn, it is advisable to have pole cores of circular cross-section. This is, however, not always possible owing to the lack of space.

Flux entering the Air-gap from Commutation Pole. —Let  $M_1$  denote the flux in air-gap per centimetre of armature periphery and S the peripheral speed of the armature in centimetres per second, then the E.M.F. induced in an inductor as it moves under the auxiliary pole =  $M_1 \times S \times 10^{-8}$  volts. If the coil short-circuited have t turns in series, then the E.M.F. induced in each short-circuited coil due to the auxiliary flux =  $M_1 \times S \times 2t \times 10^{-8}$  volts.

This induced E.M.F. must be sufficient to neutralise the reactance voltage, the mean value of which is expressed by

 $e = \text{reactance voltage} \times \frac{2}{\pi}$ 

(If an alternating E.M.F. varies as a sine function, then its mean or average value = maximum value  $\times \frac{2}{\pi}$ . For proof the student is referred to a text-book on Alternating Currents.)

The commutation field must be of such a strength

that the following equation is satisfied:-

$$e = M_1 \times S \times 2t \times 10^{-8},$$
i.e. 
$$M_1 = \frac{e \times 10^{-8}}{2t \times S}.$$

The flux leaving the face of each auxiliary pole and entering the air-gap =  $M = M_1 \times \text{width of pole arc.}$ 

The flux required to be generated in the pole core

 $= M \times dispersion coefficient.$ 

By assigning a suitable value to B, the flux density in the air-gap, the length of *embedded inductor* lying under the auxiliary pole is expressed by  $l_1 = \frac{M_1}{B}$ . The axial length of auxiliary pole shoe = gross length of inductor cutting the commutation flux

= 
$$l = l_1 \times \frac{\text{gross length of armature core}}{\text{effective length of armature core}} \times \frac{I}{I.I}$$

The constant 1.1 is introduced to allow for fringing at pole shoe ends.

Ampère-turns for Commutation Poles.—The ampère-turns on these poles should be such that they provide at all loads (1) a magneto-motive force of sufficient strength to counteract the armature magneto-motive force causing distortion; and (2) a reversing field of sufficient strength to neutralise the reactance voltage of the coils undergoing commutation, the brushes being fixed in the geometrical neutral axis. The total ampère-turns required for the auxiliary poles is equal to the armature ampère-turns per pole plus the ampère-turns necessary to send the flux through the auxiliary magnetic circuit. The latter consist of

the pole core, air-gap, and teeth, directly under the pole, the ampère-turns for which are calculated by the ordinary method. In practice it is customary to allow 30 to 40 per cent. more ampère-turns on the auxiliary winding than the armature ampère-turns per pole, and to experimentally adjust the auxiliary winding on test to give the best commutation results.

In calculating the magnetic circuits of commutation pole machines, it must be remembered that the coefficient of magnetic leakage of the main poles is considerably increased, the reluctance of the leakage paths being greatly reduced, due to the presence of the auxiliary poles; hence the main flux will have a dispersion coefficient of about 1.35 as compared with 1.2 for machines of ordinary design. To reduce this leakage to a minimum, the polar arc is made from 5 to 7 per cent. less. The leakage from the auxiliary poles is even greater than this, and a dispersion coefficient of 1.4 is usually allowed for.

Commutation poles, although essentially the outcome of the high-speed practice which marked the advent of the steam turbine, have been extensively adopted for both high- and low-speed machines of various outputs, and in some cases quite indiscriminately and needlessly. Dynamos should, as a general rule, be fitted with commutation poles when the reactance voltage is greater than 6 volts per commutator segment, and particularly in cases of high peripheral commutator speed, where there is a tendency to spark due to possible vibration of the brushes.

For correctly designed machines of moderate speed and output, having satisfactory commutation constants within the thermal limits of output, there is nothing to be gained by the use of auxiliary poles, which in such cases only add needlessly to the cost, and actually decrease the efficiency.

Example.—From the following data relating to a 1000-k.w. turbo-dynamo, determine the dimensions of the auxiliary pole, and also the flux generated in the latter at full load.

Speed of armature in R.P.M. = 1000.

External diameter of armature core = 100 centimetres.

Gross length of armature core  $(l_e) = 50$ Effective ,, ,,  $(l_e) = 36$ 

Number of slots = 160.

Tooth pitch at periphery = 1.97 centimetres.

Width of a slot = 1.0

Inductors per slot = 4.

Diameter of commutator = 51 centimetres.

Number of commutator segments = 324. Armature turns per segment = 1.

Length of arc of brush contact = 2 centimetres.

Reactance voltage at full load = 20 volts.

Periphery of commutator =  $\pi \times 5$  I = 160 centimetres. Width of segment and insulation at periphery of commutator =  $\frac{160}{324}$  = 0.5 centimetre.

Segments covered by brush =  $\frac{2}{0.5}$  = 4.

Number of inductors per brush being simultaneously commutated = 8.

There will be 4 under a S pole and 4 under a N pole. Maximum possible number of slots under a pole holding inductors undergoing commutation = 3.

Minimum number of teeth to be spanned by the

auxiliary pole arc = 3.

Minimum length of pole arc required =  $1.97 \times 3 = 5.9$ .

Allow an additional length of 35 per cent.

Therefore length of auxiliary pole arc = 8 centimetres. Peripheral speed of armature

= 
$$\pi \times 100 \times \frac{1000}{60}$$
 = 5200 centimetres per second.

Turns per commutator segment =  $\iota$ . Mean reactance voltage at full load

= 
$$20 \times \frac{2}{\pi}$$
 = 12.7 volts.

Flux in air-gap per centimetre of armature periphery

$$= M_1 = \frac{12.7 \times 10^8}{2 \times 1 \times 5200} = 122,000$$
 lines.

Decide on a flux density of 6000 lines per square centimetre, then the length of *embedded inductor* lying under the auxiliary pole =  $l_1 = \frac{122000}{6000} = 20.4$  centimetres.

Length of pole shoe = gross length of inductor lying under the auxiliary pole

= 20.4 
$$\times \frac{50}{36} \times \frac{1}{1.1}$$
 = 25 centimetres.

Flux entering air-gap per pole =  $M_1 \times$  width of pole arc = 122000  $\times$  8 = 966000 lines.

Flux to be generated in pole core

=  $966000 \times \text{dispersion coefficient}$ =  $966000 \times 1.4 = 1.35 \text{ megalines}$ .

Make axial length of pole core = 20 centimetres and width of pole core = 5 ,,

This allows of a flux density in auxiliary pole core of 13,500 lines per square centimetre at full load.

Compensating Winding on Main Poles.—Another method of overcoming armature reaction and providing

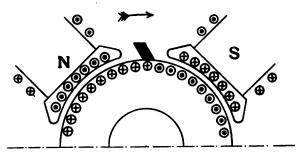


FIG. 212.—Compensating winding on main poles.

a reversing field for commutation, is by the use of a compensating winding on the main poles, as shown in Figure 212. This winding is wound in slots in the pole face, the former lying parallel to the armature shaft. The coils of the winding are connected in series with the armature, and so carry a current varying with

the load and therefore with the cross magneto-motive force of the armature. The current flows through the compensating winding in such a direction that its magneto-motive force opposes the cross ampère-turns of the armature, as will be seen by the crossed and dotted circles in the figure, which shows a section through the poles and armature in a plane at right angles to the axis of the shaft. The ampère-turns of the compensating winding range from 1.2 to 1.3 times the cross ampère-turns of the armature.

Since this compensating winding is arranged opposite the armature surface and distributed over almost the entire air-gap, the cross ampère-turns of the armature are completely neutralised, with the result that there is no distortion of the main magnetic flux. This principle has been applied to turbo-dynamos by several manu-

facturers.

## FLASH-OVER LIMIT IN TURBO-DYNAMOS

The output of slow- and medium-speed dynamos is limited by considerations of temperature rise and commutation, but in turbine-driven machines there is another limitation, namely, the liability of a machine to "flashover" at the commutator from one set of brushes to another. Troubles due to flashing over have become very serious in the case of high-voltage machines. The flashover limit is quite distinct from that of sparking, as not a few turbo-generators which had excellent commutation properties have proved to be failures on account of their tendency to arc round the whole commutator. At one time these occurrences were attributed to insufficient insulation between the shrinking rings and the commutator segments. This may in some cases have been the cause, but the more important factor now appears to be an excessive P.D. between adjacent commutator segments.

In slow-speed machines the flash-over limit is about 60 volts per segment, but owing to other considerations the maximum voltage between commutator segments seldom exceeds 50 per cent. of this value. In the case

of high-speed turbo-dynamos experience dictates 40 volts to be taken as the safe limit, though in some machines this value has been slightly exceeded. Owing to the small diameter of commutator employed in high-speed machines the number of commutator segments is small, and the safe voltage per segment required by flash-over considerations may quite easily be exceeded. The extent to which the flash-over limit affects the dimensions of the armature, and the value of the flux in the air-gap will now be examined.

When an inductor of length l centimetres moves through a field of intensity B lines per square centimetre at a velocity of v centimetres per second, the E.M.F. induced in that inductor =  $Blv10^{-8}$  volts. If  $l_a$  denote the length of armature core,  $B_{rmax}$  the maximum flux density in the air-gap, and v the peripheral speed of the armature in centimetres per second, then the maximum E.M.F. induced in each armature inductor

= 
$$B_{gma.x.} \times l_a \times v \times 10^{-8}$$
 volts.

In turbo-dynamos there is, as a rule, 1 turn (i.e. 2 inductors) per commutator segment, in which case the maximum E.M.F. between two adjacent commutator segments is expressed by

$$e_{max} = B_{emax} \times l_a \times 2 \times v \times 10^{-8}$$
 volts.

In turbo-driven dynamos the peripheral speed of the armature is, for mechanical considerations, limited to about 75 metres per second. Since the maximum voltage between two adjacent commutator segments must not exceed 40 volts, a speed of 75 metres per second makes

$$B_{gmax.} \times l_a = \frac{40 \times 10^8}{2 \times 75 \times 100} = 267,000.$$

Case 1.—Machines with Commutation Poles.—In the case of machines with commutation poles it may be assumed that, on an average, armature distortion at full load causes  $B_{emax}$  to exceed  $B_{emax}$  by about 15 per cent.,

in which case 
$$B_{gmean} \times l_a = 267,000 \times \frac{100}{115} = 230,000$$
.

7000 lines per square centimetre may be taken as an average value of  $B_{g\,mean}$ , so that the greatest permissible length of armature, independent of its diameter

$$=\frac{230,000}{7000}$$
 = 33 centimetres.

In the case of machines with commutation poles, the ratio of pole arc to pole pitch (i.e. r) may be taken as 0.6, so that the total number of lines entering or leaving the armature

$$= 2pM = \pi d_a \times 0.6 \times B_{gmcan} \times l_a = 0.43 d_a \times 10^6,$$

where---

p = number of pairs of poles,

 $\dot{M} = flux per pole,$ 

 $d_a = \text{diameter of armature.}$ 

It will thus be seen that the flash-over limit restricts the number of lines of force entering or leaving the

armature, of a given diameter, to  $0.43d_a \times 10^6$ .

Case 2.—Machines with a Compensating Winding.—In machines fitted with a compensating winding (for instance, those described on pp. 358 to 361) the armature distorting force is almost neutralised at all loads, with the result that  $B_{gmax} = B_{gmean}$ . In such machines, assuming  $B_{gmean} = 7000$ , the permissible length of armature attains a value of  $\frac{267,000}{7000} = 38$  centimetres. Since the value of r in such machines is about 0.7, the total number of lines entering or leaving the armature is restricted to

$$\pi \times d_a \times 0.7 \times 267,000 = 0.58 \ d_a \times 10^6.$$

In machines of the same output and voltage, and having the same values of  $l_a$ ,  $d_a$ , and 2pM, the liability to flash-over depends solely upon the amount of armature distortion. In machines fitted with a compensating winding there is practically no armature distortion, and the designers of these machines state that no flash-over difficulties are experienced.

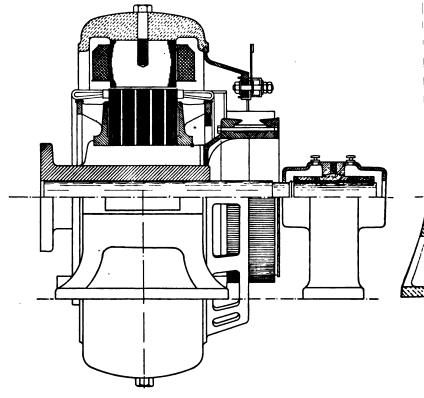
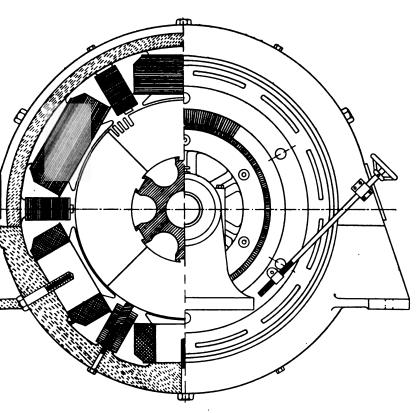


FIG. 213.—Mechanical construction of a 220-k.w. 530/440



t generator. Armature speed, 380 R.P.M. Scale, 1:15.

[To face page 355.

In dynamos with commutation poles armature reaction is not so neutralised, and flash-over, if occurring at all, generally occurs when there is a sudden overload thrown on the machine. The resulting increase in the armature current causes  $B_{gmax}$  to increase, and therefore also the value of  $e_{max}$ . When flash-over occurs, the latter has, of course, exceeded the safe limit.

The above limits of armature core length and flux entering or leaving the armature hold good only for peripheral speeds of 75 metres per second. The limit values of  $l_a$  and 2pM for a range of peripheral speeds between 50 and 75 metres per second are given in Table XIV. It will be observed that the lower the speed the greater can be the values of  $l_a$  and 2pM.

TABLE XIV
LIMIT VALUES OF 1a AND 2pM FOR TURBO-DYNAMOS

Peripheral speed in metres per second.	Machines with commutation poles.		Machines with compensating windings.	
	la.	2 <b>⊅</b> M.	l <sub>a</sub> .	2 <i>p</i> M.
75	33	$0.43d_a \times 10^6$	38	$0.58d_a \times 10^6$
70	36	$0.47d^a \times 10^6$	41	$0.63d_a \times 10^6$
65	39	$0.51d_a \times 10^6$	41	$0.68d_a \times 10^6$
60	42	$0.55d_a \times 10^6$	48	$0.74d_a \times 10^6$
55	45	$0.59d_a \times 10^6$	52	$0.80d_a \times 10^6$
50	50	$0.65d_a \times 10^6$	57	$0.88d_a \times 10^6$

## Examples of Complete Machines

Slow-speed Dynamo. — Figure 213 shows the mechanical construction of a 220-k.w. 530/440-volt 6-pole shunt-wound generator, the armature of which is driven at a speed of 380 R.P.M. The magnet yoke is fitted with commutation poles, and the design

may be taken as typical for slow- and medium-speed machines giving an output of from 150 to 500 k.w.

The armature is built up on a six-armed spider, the boss of which is keyed to the shaft. One end of the boss terminates in a coupling by means of which the armature is bolted to the prime mover; this, as already stated, relieves the shaft of the driving stresses. armature laminations are mounted on the arms of the spider and held between two end flanges, to each of which is cast a skeleton ring for supporting the end connections of the winding. The left-hand end flange abuts against lugs projecting from the arms of the spider, while the other is held in position by keys driven into each arm. The core is provided with four ventilating ducts. The armature is lap-wound, and those parts of the end flanges on which the end connections rest are insulated with press-spahn as indicated.

The commutator spider is in two parts, one of which is bolted to the arms of the armature spider. The V-shaped rings, between which the commutator is retained, are cast in one with each portion of the spider. The two members of the spider are held together by bolts and insulated from the commutator by the ordinary V-shaped mica rings. Connection is made to the ends of the armature windings by lugs projecting from the segments. Directly below the supporting ring at the commutator end of the armature are 10 equalising rings, each of which is connected to those commutator lugs which should be at the same potential.

The yoke of the field magnets is of cast steel, and to the lower half of the ring are cast feet by means of which the yoke is bolted to the bedplate. The yoke, at each face, is cast with overhanging rims, the one at the commutator end being turned to receive a skeleton cast-iron ring for supporting the brush gear. The brush spindles are insulated from their supporting rings by vulcanite bushes and washers, spindles of the same polarity being connected to one of two connectors, from which leads go to the machine terminals.

The main poles are built of sheet-iron laminations, and bolted to machined seatings on the yoke. The

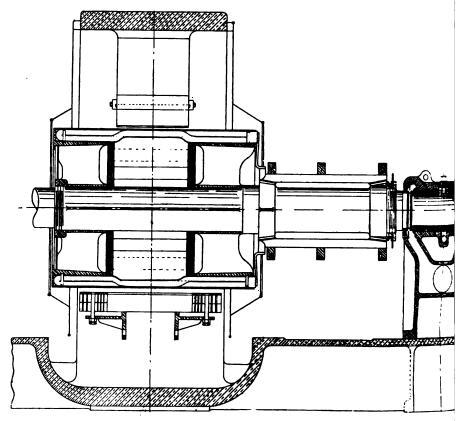
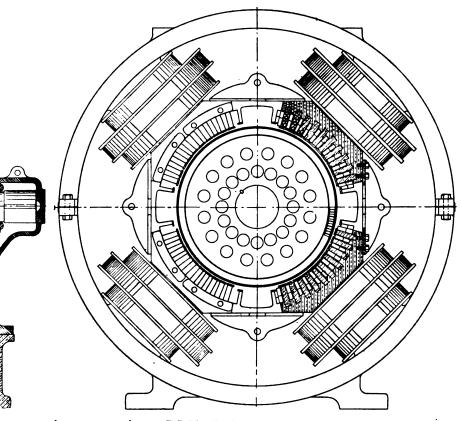


FIG. 214.—Mechanical construction of a 1000-k.w. turb



nerator. Armature speed, 1000 R.P.M. Scale, 1:25.

[To face page 357.

laminations are stamped with projections at their lower end, so that when assembled the latter form polar extensions, and serve to support the winding spools. The auxiliary poles are of cast steel, and are also bolted to machined seatings on the yoke.

High-speed Dynamos.—Type 1.—Figure 214 shows the mechanical construction of a 1000-k.w. turbine-driven 4-pole dynamo. The armature laminations, pierced with numerous ventilating tunnels, are mounted direct on the shaft. The end flanges are of brass, and designed so as to support the end connections of the winding. The end flange at the commutator end abuts against a turned collar on the shaft, and the other one is forced home by a nut screwed on to the shaft, thus making it compress the laminations together. The latter end flange is keyed to the shaft, and the nut is prevented from turning by fixing it to the end flange with a set pin. To the end flanges are attached blades, which act as a fan in driving air through the interior of the armature.

The armature winding is placed on the surface of the core, and prevented from moving relative to the latter by brass drivers fastened into the core at each end, as shown in Figure 142. The entire winding is held against centrifugal force by binding wire. The placing of the winding on the surface of the core ensures a lower reactance voltage than would be the case with a winding enclosed in slots. This will of course permit of better commutation. The commutator is mounted direct on the shaft, and its construction is identical with that shown in Figure 170.

The magnet core is of cast steel, and divided along a horizontal diameter, the upper and lower halves being bolted together. The lower half of the yoke is provided with feet for bolting to the bedplate. The steel magnet cores and their polar extensions are cast solid and bolted to the yoke. Each exciting coil is wound in three sections of different overall dimensions. This, as will be seen from the drawing, considerably increases the cooling surface of each coil.

The machine is provided with a compensating winding fixed to the main poles and connected in series with

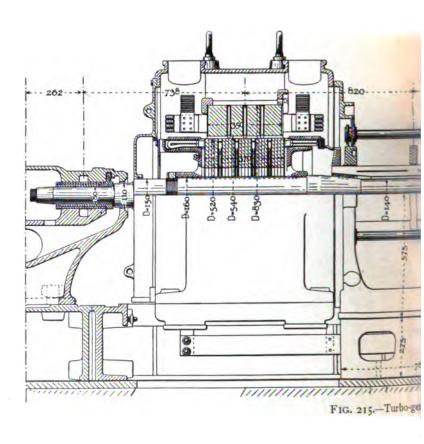
the armature. For holding this winding the pole shoes are provided with slots: the teeth are generally made separate, and bolted to the polar extensions. After the winding has been put in place, the tops of the teeth are fitted with small shoes, which overlap the slots as shown. This increases the area of iron by which the flux enters or leaves the air-gap, and also retains the coils in position. The end connections of the compensating winding are supported by brass bridge-pieces, which in turn are bolted between adjacent pole shoes. The bearings are supported on an extension of the yoke, and the armature and field magnets are partially enclosed by thin brass end covers.

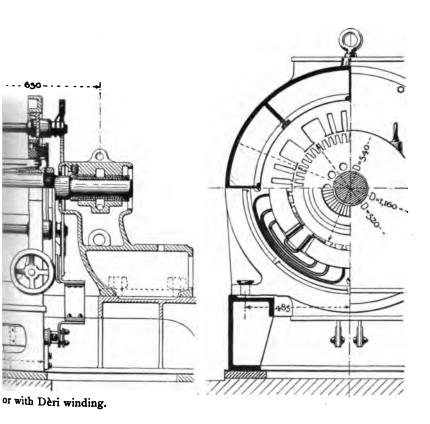
Type 2. — Figure 215 shows sectional drawings of a 250-k.w. 500/600-volt 4-pole turbo-dynamo, the armature of which is driven at a speed of 2500 R.P.M. The drawings are dimensioned in millimetres.

The armature laminations are mounted direct on the shaft and held between end flanges in the manner shown. The inductor portions of the winding are placed in slots on the armature periphery and held in place against the action of centrifugal force by wooden wedges driven into key-ways formed near to the tops of the teeth. The end connections are retained against centrifugal force by metal covers which are bolted to the supporting flanges. The commutator is of the same construction as that shown in Figure 170.

The field magnet is constructed on a different principle to that generally adopted for direct-current machines. The yoke is built up of sheet-iron laminations fitted to radial arms projecting inwardly from a cast-iron frame, and, after being assembled, are clamped between end flanges or rings. The laminations forming the yoke are stamped with inward projections of short radial length, so that, when assembled, the latter form the main poles, as shown in Figure 216. In order to assist ventilation, the field-magnet system has a number of radial air-ducts through which air can be driven by the fanning action of the armature.

At the centre of each interpolar space a tooth, formed with overhanging ends, projects from the yoke,





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and this, along with the sides of adjacent poles, forms wide slots into which are placed the coils exciting the main poles. The latter are formed with a series of

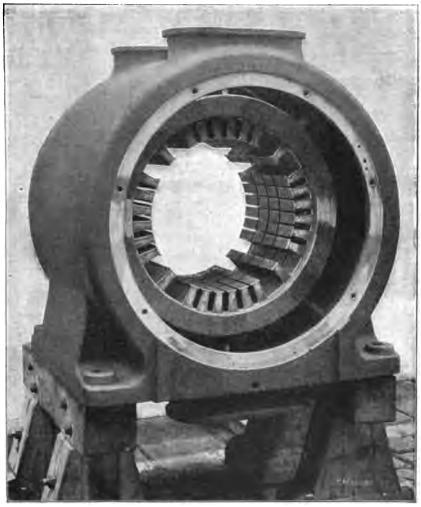


FIG. 216.—Field-magnet frame of turbo-dynamo fitted with a Dèri winding.

almost totally enclosed slots, in which is wound a compensating winding. Slots of this type are used so as to increase the section of iron by which the main flux enters or leaves the pole face.

The compensating winding, often referred to as a Deri winding, after the name of its inventor, is connected

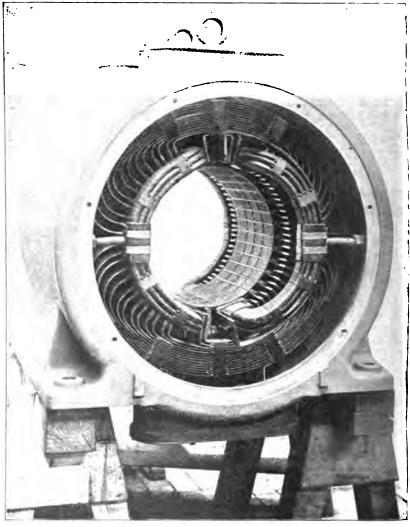


FIG. 217.—Field-magnet frame of turbo-dynamo, showing exciting coils and Deri winding.

in series with the armature, and is an application of the principle illustrated in Figure 212. Figure 217 is a photograph of the field-magnet frame of a 2-pole

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dynamo, showing the main field coils and Deri winding

in position.

In machines of this type the number of compensating ampère-turns is relatively large, and should a dynamo, operating in parallel with others, be driven as a motor, owing to a reverse current flowing, a reversal of the main field might also take place, and if the reversed field be weak there is a possibility of the machine attaining a dangerous speed. In order to prevent the latter contingency, separate direct-coupled exciters are supplied for providing the excitation current, thus ensuring a constant direction of field. In addition to preventing a reversal of the main field, the strength of the latter increases with increase of speed; hence the additional loss thrown on the machine has a strong tendency to prevent excessive speed being attained should any accident occur.

The armature is fitted with a number of vanes so that the revolving armature acts as a fan. Air, drawn from the inlet opening at each end of the machine, is propelled through the ducts in the armature core and field-magnet system into the annular space which surrounds the field-magnet core, and is finally ejected into the atmosphere through the ventilating openings shown in the top of the field frame. By this arrangement every part of the machine which is the seat of the generation of heat is reached by the cooling air, thus resulting in a moderate and uniform temperature rise.

#### CHAPTER X

# THE DYNAMO—CHARACTERISTIC CURVES, PARALLEL WORKING, AND BOOSTERS

#### CHARACTERISTIC CURVES

Magnetisation Curve.—It has been shown in the example, page 317, that for the magnetic circuit of the 33-k.w. dynamo (Figure 194) 4590 and 5210 field ampère-turns are necessary to maintain a magnetic flux of 3.45 and 3.6 megalines respectively through the armature. By similar calculations the ampère-turns required to force any magnetic flux across the air-gap and through the iron parts can be determined. The ampère-turns necessary to maintain five values of the magnetic flux ranging from 1.25 to 3.6 megalines are given in the accompanying table. In the third column is the total E.M.F. induced in the armature at a constant speed of 660 R.P.M., corresponding to each value of the magnetic flux.

Magnetic Flux in Megalines.	Ampère-turns.	Induced E.M.F.		
1.25	1000	200		
1.90	1650	300		
2.80	3100	450		
3.45	4590	550		
3.45 3.60	5210	57 <sup>2</sup> ·		

In Figure 218 the values of the calculated ampèreturns are plotted against the corresponding values of the magnetic flux, and the curve obtained is known as the magnetisation or saturation curve of the dynamo under consideration. If the speed remain constant the

total E.M.F. induced in the armature will be directly proportional to the magnetic flux, and is given by E=4 TNM  $10^{-8}=KM$ , where K is a constant. The curve showing the variation of the induced E.M.F. with the field ampère-turns is known as the *internal characteristic* of the machine, and may be obtained from the magnetisation curve by marking off along the ordinate reference axis the corresponding values of induced E.M.F., as is shown in Figure 218.

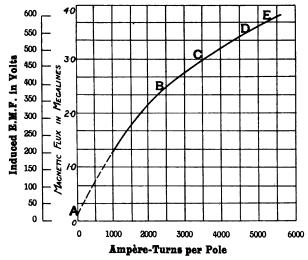


FIG. 218.—Magnetisation curve for a shunt dynamo.

The magnetisation curve of a dynamo is obtained experimentally by running the machine on open circuit at normal speed and separately exciting the field coils. In series with the latter a regulating resistance should be connected, so that the exciting current can be adjusted to a number of suitable values, and the corresponding values of induced E.M.F. read off on a voltmeter connected across the armature terminals.

It will invariably be found that the magnetisation curve does not pass through the origin, but when the exciting current is zero there will be a small E.M.F. induced in the armature, due to residual magnetism in

the field magnets. This effect is shown in the figure, the ordinate oA representing the E.M.F. due to residual

magnetism.

That part of the magnetisation curve between A and B is practically a straight line, as the ampère-turns required to send the flux across the air-gap form almost the whole of the excitation; the magneto-motive force required for the iron parts of the magnetic circuit being only a very small percentage of the total. If the proportions and magnetic densities in the component parts of the magnetic circuit have the values recommended in the previous chapter, it will be found that machines are worked on a portion of the magnetisation curve well over the knee. For instance in the machine under consideration the flux through the armature ranges from 3.45 to 3.6 megalines between no load and full load, so that the working portion of the curve is that between the points Should a dynamo be worked on a portion of the curve below the knee the machine will be very unstable, and a slight variation in speed will cause a large variation in the terminal E.M.F., a result which is always undesirable.

For example, if in the case of a shunt dynamo the speed slightly increases, the resulting increase in the E.M.F. will of course increase the current through the shunt coils: now, below the knee of the curve a small increase in exciting current produces a large increase in E.M.F., so that the E.M.F. will be still further increased. It is therefore of great importance to design dynamos which are excited by shunt coils, so that they work fairly high up on the magnetisation curves, and the best portions to work on are within the limits marked by CE in the figure. Another advantage of working high up on the curve is that the difference of the ampère-turns of the shunt winding when hot and when cold then produces but a small effect on the E.M.F. induced in the armature owing to the iron parts of the magnetic circuit being nearly saturated.

Critical Resistance of a Shunt Dynamo.—The general form of the internal characteristic of any shunt dynamo is shown in Figure 219, where values of shunt

current are plotted as abscissæ and the corresponding values of induced E.M.F. as ordinates. Take any point P on the curve and join P to the origin O. At P the exciting current is given by the abscissæ OC, and the corresponding value of induced E.M.F. by the ordinate OE. Now the resistance of the shunt circuit equals

E.M.F. across shunt winding (including rheostat),

so that the resistance of the latter corresponding to the point P, is given by

$$R = \frac{OE}{OC} = \frac{PM}{PE} = tan POC = tan \theta$$

i.e. the resistance is given by the slope of the line OP.

Expressed in words:
The resistance of the shunt circuit corresponding to any point on the characteristic is given by the tangent of the angle made by the line joining that point to the origin.

If the resistance of the shunt circuit be gradually increased from that represented by tan POC, the point P will move along the

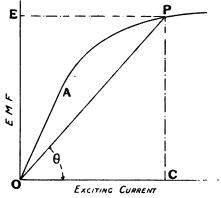


FIG. 219.—Critical resistance of a shunt dynamo.

curve towards the origin, the induced E.M.F. and exciting current decreasing while the slope of the line OP increases. The resistance may be increased until OP practically forms a tangent to the part OA which is approximately a straight line. Any further increase in the shunt resistance beyond that represented by the slope OA will have so reduced the exciting current that it is not sufficient to adequately magnetise the field magnets, with the result that the dynamo loses its magnetism. The slope of the line OA

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is known as the *critical resistance* of a shunt dynamo, *i.e.* the maximum resistance of the shunt circuit which will permit of the dynamo being adequately magnetised.

External Characteristic of a Series Dynamo.—The external characteristic of a dynamo is a curve showing the relation between the electromotive force at the armature terminals and the current output of the machine when the latter is varied; the values of E.M.F. being plotted as ordinates, and those of current as abscissæ. Such a curve can be experimentally deter-

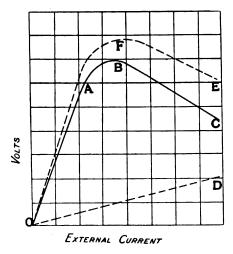


FIG. 220.—Characteristic curves of a series dynamo.

mined by running the machine at constant speed, varying the current by means of an adjustable resistance in the external circuit, and observing the corresponding values of current output and terminal voltage.

In Figure 220 the curve OC shows the form of the external characteristic of a series dynamo, and since the external current is also the magnetising current it

resembles to some extent the curve shown in the previous figure. As the external current is increased from zero the E.M.F. on the armature terminals rapidly increases, as shown by the portion OA. If the current be further increased the curve takes a decided bend and reaches a maximum at B; but beyond this any further increase in the current is accompanied by a decrease in terminal E.M.F. as shown.

This fall of E.M.F. when the current is increased beyond a certain value, is due to (1) the pressure drop over the resistance of the armature and series coils, and (2) the demagnetising effect of the armature ampère-

The former is proportional to the current and is expressed by  $V = C (R_a + R_s)$ , where C is the armature current and R<sub>a</sub> and R<sub>s</sub> the resistance of the armature and series coils respectively. If C  $(R_a + R_s)$  be known, the voltage drop in the armature and series coils can be calculated for various values of current, and when the values of C  $(R_a + R_s)$  are plotted the straight line OD will be obtained, which shows the variation of pressure drop with the load.

By adding to the ordinates of the curve OC the corresponding ordinates of the curve OD, a third curve OE is obtained, which shows the variation of the total E.M.F. induced in the armature with the external current. If it were not for the demagnetising action of the armature ampère-turns the curve OE (i.e. the total characteristic) of a series dynamo would be identical

with its magnetisation curve.

When the field magnets are approaching saturation any increase in the external current is not accompanied by a corresponding increase in the magnetic flux, the result being that the rate of increase of the induced E.M.F. diminishes as the current increases. the armature demagnetising effect be zero, the total characteristic curve would tend to rise continuously with an increase of current: but the demagnetising action of the armature current also increases in proportion to the external current, and tends to reduce the terminal E.M.F. in the following manner:

As already stated, the armature core is worked at a much lower induction than the field magnets, so that when the latter are nearly saturated the armature core will still be considerably below saturation. When the current is increased beyond that corresponding to the point B, the magnetic flux due to the field coils remains approximately constant, whereas the demagnetising flux of the armature will at this stage increase in proportion to the current, with the result that the total flux linked with the armature inductors decreases, and therefore, also, the induced E.M.F., as is shown by the part FE in the curve OE. When the field magnets are saturated any increase in the magneto-motive force increases the

coefficient of magnetic leakage so that a smaller percentage of the flux generated in the magnets enters the armature; this further helps to decrease the induced E.M.F.

External Characteristic of a Shunt Dynamo.—The external characteristic curve of a shunt dynamo takes the form shown in Figure 221. The E.M.F. across the armature terminals is a maximum on open circuit. When the external circuit is closed and the armature current increased from the no load value, the E.M.F. on the armature terminals gradually decreases in the

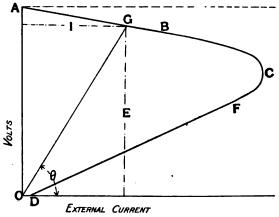


FIG. 221.—External characteristic of a shunt dynamo.

manner shown, the resistance of the shunt circuit being maintained constant. This fall of E.M.F. at the armature terminals is attributable to—(1) The drop in pressure—due to armature resistance—expressed by CR<sub>a</sub>, where C is the armature current and R<sub>a</sub> the resistance. (2) The demagnetising action of the armature current, which increases with the load and can be calculated in the manner shown on page 327. (3) The shunt coils being connected across the armature terminals, any decrease in the terminal E.M.F. due to (1) and (2) also decreases the strength of the exciting current, and thereby further reduces the terminal E.M.F.

Owing, then, to the combined effects of the increase in the demagnetising ampère-turns of the armature and the pressure drop due to armature resistance, the voltage of a shunt dynamo continuously decreases, as the output is increased, up to a point indicated by C, where the current attains its maximum. At this point the flux set up by the demagnetising ampère-turns of the armature is equal to the flux set up by the field magnets, and consequently the voltage decreases to zero. The curve bends back upon itself as shown by the part CD, which cuts the axis of abscissæ a little to the right of the origin as a result of the pressure generated in the armature due to the residual magnetism of the field magnets. shunt dynamo there will thus be a maximum value of the external current beyond which it is impossible to go: but owing to thermal considerations it will generally be impossible to allow the armature to carry this maximum current for any appreciable time. In a well-designed dynamo the full-load current is about 50 per cent. of the maximum. The part AB of the characteristic which shows the change in E.M.F. between no load and full load is known as the regulation or load curve. If the armature be of low resistance the drop in volts for any current within the working limits will be small.

From the external characteristic it will be seen that for every value of the current, except the maximum, there are two values of the terminal E.M.F., and which one of these two E.M.Fs. is obtained will depend upon the resistance of the external circuit.

 $= \frac{\text{terminal E.M.F.}}{\text{avternal current}} = \frac{E}{I} = \tan \theta, \text{ so that the resistance of}$ the external circuit is given by the slope of the line OG. where G is any point on the characteristic at which the current and terminal E.M.F. are expressed by E and I respectively. There is a critical portion of the curve just before the maximum current is reached, and if the resistance of the external circuit be diminished there will be a comparatively large drop in pressure at the armature terminals. After rounding the point maximum current the curve is almost a straight line to the point D, so that very small changes in the external resistance will cause great changes in pressure and current, because the voltage across the shunt is insufficient to adequately magnetise the iron. The slope of the curve between F and D defines the critical resistance of the external circuit, within which the magnetic flux of the field magnets is unstable, and the machine fails to excite.

This is of great practical importance, for if a shunt dynamo be accidentally short-circuited when supplying current the armature is not liable to destruction by the passage of an excessive current, for when the maximum current is attained the field magnets are demagnetised and the armature current immediately falls to zero. some cases when a shunt dynamo is suddenly shortcircuited the field magnets, through certain secondary reactions, become slightly magnetised in the reverse direction, so that when again self-excited the polarity of the terminals is reversed.

Voltage Control.—(1) Shunt Regulation.—In order to regulate the voltage of a shunt dynamo a variable resistance or rheostat R (Figure 182) is connected in series with the field-magnet winding. The rheostat is so designed that at no load the machine gives its full terminal voltage when the whole of the resistance is in series with the field coils. As the load increases the shunt current must be increased, in order to compensate for the pressure drop due to armature resistance and reaction. This is accomplished by manipulating the field rheostat, so that the resistance in series with the field coils is diminished, until at full load nearly the whole of the resistance is cut out.

The function of the shunt-regulating resistance for a dynamo will be best illustrated by an example. In the calculation of the shunt coils for the 33-k.w. dynamo the following was determined (vide page 318):

Ampère-turns at no load =4590.Ampère turns at full load = 6000.Number of turns per shunt coil = 6000. Exciting current at full load = 1 ampère. Constant voltage across shunt + rheostat = 550. Resistance of each shunt coil (60° C.) = 130 ohms. Total resistance of shunt winding  $(60^{\circ} \text{ C.}) = 130 \times 4$ = 520 ohms.

It is usual to design the shunt rheostat so that when full load is attained the entire regulating resistance does not require to be cut out of circuit, thus reserving a possible increment of exciting current sufficient to maintain a constant terminal E.M.F. for a reasonable percentage of overload. The value of the shunt-regulating resistance is such that at full load from 5 to 10 per cent. of the terminal pressure is absorbed, and in the example under consideration 30 volts were so absorbed.

Since the full-load shunt current = 1 ampère, the value of the regulating resistance in circuit at full load = 30 ohms. In order that the field ampère-turns at no load may be 4590, the exciting current must be reduced to  $\frac{4590}{6000}$  = 0.76 of an ampère. The total resistance of the

shunt circuit will then =  $\frac{550}{0.76}$  = 725 ohms.

Since the field coils have a permanent resistance of 520 ohms the total value of the shunt-regulating resistance = 725 - 520 = 205 ohms, of which 30 ohms are in circuit at full load. (At no load the watts absorbed by the shunt rheostat =  $C^2R = 0.76^2 \times 205 = 120$  watts.)

The number of steps into which a shunt-regulating resistance should be divided will depend upon the permissible percentage variation in the total induced E.M.F. when one section of the resistance is cut out of or put into circuit. In practice the variation allowed per step is usually about 4 per cent. of the total range of induced E.M.F. between no load and full load. In the case under consideration there is a range of 22 (i.e. 572 - 550) volts. Allowing for a 4 per cent. variation, the change in the induced E.M.F. at any one step =  $4 \times \frac{22}{100} = 0.88$ 

volt, so that the number of steps =  $\frac{22}{0.88}$  = 25. From Figure 218 it will be seen that between no load and full load the magnetisation curve is practically a straight line, so that each section of the resistance will be of the same value, namely,  $\frac{205}{25}$  = 8.2 ohms. In the majority of

dynamos the working part of the characteristic is practically a straight line, so that in practice, except in special cases, dynamo shunt rheostats are divided into sections, each of which has the same resistance.

Design of Shunt Rheostat.—The resistance coils of shunt rheostats are usually made from one of the alloys given in Table XV., these alloys having a high specific resistance and low temperature coefficient. Iron is also given, but owing to its high temperature coefficient it is never employed for shunt rheostats. It is, however, often used in the construction of motor starting resistances, which are described in the next chapter.

TABLE XV
ALLOYS USED FOR RHEOSTATS

Material			Specific resistance in microhms per centimetre cube at 0 ° C.	Temperature coefficient per ° C.	Specific gravity.	Specific heat.
Beacon .			74	0.00070	8.1	1.0
Constantan			43	zero.	8.8	0.1
Eureka .			47	0.000005	8.8	O. I
German silver			30	0.000273	8.5	0.098
Iron (pure).			9	0.00625	7.9	0.104
Kruppin .			84	0.00077	8.7	0.13
Nickelin .			33	0.00030	9.0	0.08
Platinoid .			40	0.00031	8.6	0.098
Rheostan .			52	0.00041	8.6	0.097
Resista .	•	.!	75		•••	0.1

The size of wire forming the coils of a regulating rheostat should be such that the steady temperature which the wire attains when carrying continuously the maximum current, should not exceed a safe limit. For shunt resistances the permissible temperature rise is generally about 100° C. A steady temperature is reached when the rate of loss of heat by radiation from

the surface of the wire is equal to the rate of generation of heat by the current. The heat generated per second

= 
$$C^2R \times 0.24$$
 calories =  $C^2 \times \frac{\rho \times l \times 4}{\pi d^2} \times 0.24$  calories  
=  $C^2 \times \frac{\rho \times l}{\pi d^2} \times 0.96$ 

where—

 $\rho$  = specific resistance of wire. l = length of wire in centimetres. d = diameter of wire in centimetres.

Let  $\sigma$  denote the emissivity of the wire, *i.e.* the rate of loss of heat in calories by radiation per unit area of the wire per °C. difference in temperature between the wire and the surrounding air. The emissivity is not actually a constant, being higher for black surfaces that for bright, but on an average may be taken at 0.0005. The rate of loss of heat by radiation will therefore = surface area of wire  $\times \sigma \times$  temperature rise above surrounding air

=  $\pi d \times l \times 0.0005 \times (T_2 - T_1)$  calories per second,

where—

 $T_2$  = temperature of wire.

 $T_1$  = temperature of surrounding air.

In practice the coils are usually proportioned so that the temperature rise will not exceed 100° C., in which case the loss of heat by radiation

=  $\pi d \times l \times 0.0005 \times 100 = 0.05 \times \pi d \times l$  calories per second. When a steady temperature has been attained

$$C^{2} \times \frac{\rho \times l}{\pi d^{2}} \times 0.96 = 0.05 \times \pi d \times l$$

i.e. 
$$d^3 = C^2 \times \rho \times \frac{0.96}{\pi^2 \times 0.05} = 2 C^2 \rho$$

and diameter of wire is expressed by  $d = \sqrt[3]{2 \ C^2 \rho}$ .

Having determined the diameter of wire, the length required to give any particular value of resistance is obtained from the formula  $R = \frac{\rho \times l \times 4}{\pi d^2}$ 

i.e. 
$$l = \frac{\pi d^2 \times R}{\rho \times 4}$$
.

Example.—In the shunt rheostat for the 33-k.w. dynamo, the resistance per section has to be 8.2 ohms and the maximum field current 1 ampère. If the resistance coils be of platinoid, determine the diameter of wire required and the length of wire for each section.

$$d = \sqrt[8]{2 \times 1^2 \times 0.00004}$$
  
= 0.043 centimetre.

The nearest standard size to this is No. 26 S.W.G., which has a diameter of 0.0457 centimetres.

Length of wire per section

$$= \frac{\pi \times 0.0457^2 \times 8.2}{0.00004 \times 4} = 340 \text{ centimetres.}$$

Resistance Box.—Resistance wires are usually wound either on porcelain tubes or in the form of open spirals,

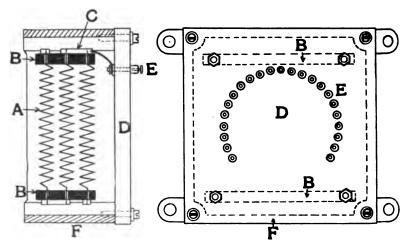


FIG. 222.—Resistance box.

and enclosed in ventilated cast-iron boxes arranged so that the heated air rises and cool air is drawn in from below into the box. Figure 222 shows a design of resistance box suitable for arranging the wires in open spirals. The resistance coils A are stretched between two slate supports BB, which are braced

together. The coils A are arranged in tiers with two or more in each tier, and are held in position by fixing each end of a coil into the terminal blocks C; these also serve to connect the coils in series. The supports BB are bolted to a slate slab D on which are mounted the terminals E. The latter are, at the back, connected to the various points of the resistance, and from the front connection is made to a multiple contact switch (described on page 478), which is usually mounted on a switchboard. The resistance coils are enclosed inside the ventilated cast-iron box F, the cover of which is provided by the slate slab D on which the terminals are fixed.

(2) Compounding.—The best method of maintaining a constant terminal E.M.F. is by winding the field magnets with both shunt and series coils. The shunt winding should be sufficient to give the full terminal pressure at no load, and as the load is increased the current flowing in the series coils should augment the field ampère-turns in such a proportion that the terminal E.M.F. is maintained constant.

In a compound dynamo the shunt simply provides a certain initial flux and voltage, and since the excitation of the series turns varies directly with the external current, the series ampère-turns increase the field flux in such a proportion that they compensate for the drop in pressure due to armature resistance and reaction.

The external characteristic of a correctly compounded dynamo is therefore approximately a straight line throughout the entire working range. Thus in the case of the 33-k.w. dynamo, for which the ampère-turns per pole at no load and full load are 4590 and 6000 respectively, the shunt winding would be designed to give the 4590 ampère-turns at no load, and the additional ampère-turns necessary as the load increased would be provided by the series coils, which at full load would provide a magneto-motive force of 6000 - 4590 = 1410 ampère-turns.

The full-load current of this machine is 60 ampères, so that the number of series turns per pole =  $\frac{1410}{60}$  = 24.

When the load happens to be situated at the end of a long transmission line, it is often required that the voltage at the point of distribution shall remain constant at all loads. In such a case the generator must be over-compounded, i.e. the voltage at the dynamo terminals must increase with the load, thus compensating for the additional CR drop in the transmission line. For instance, generators used for traction work are usually over-compounded, to give a terminal E.M.F. of 500 and 550 volts at no load and full load respectively, the 50 volts increase in terminal E.M.F. at full load compensating for the fall of potential along the transmission line.

# PARALLELING OF DYNAMOS

The prime mover and dynamo of a generating set are invariably designed to give their maximum efficiency at or near full load. The output of a generating station usually varies within wide limits at different times of the day, so that it is best to employ two or three smaller units rather than one unit large enough to supply the maximum demand. With this arrangement the number of dynamos coupled in parallel can be increased with the load, and disconnected one after the other as the load diminishes. The individual generators can thereby be maintained at nearly full load, and consequently work near to their maximum efficiency, whereas if one large unit be used, its output during the greater part of the day might be considerably less than half its full-load capacity, with the result that it would have a very low efficiency. The method of connecting shunt or compound dynamos in parallel will now be considered.

Shunt Dynamos in parallel.—Figure 223 shows the connections between two shunt-wound dynamos, D<sub>1</sub> and D<sub>2</sub>, which are to run in parallel. The positive and negative terminals of each dynamo are connected through double pole switches S<sub>1</sub> and S<sub>2</sub> to the common conductors B + and B - respectively. The latter are known as bus-bars, and from them feeders are run to the network of mains. In series with the positive main of each dynamo are connected the ammeters A<sub>1</sub>

and  $A_2$ , while the voltmeters  $V_1$  and  $V_2$  indicate the pressure generated by the respective dynamos. The shunt coils C, C, are joined in series with the regulating resistances R<sub>1</sub> and R<sub>2</sub> respectively.

Suppose the machine D<sub>1</sub> is supplying the total current output, and that the latter has attained such

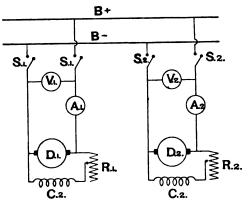


FIG. 223.—Shunt dynamos in parallel.

a value as to necessitate the second machine D<sub>2</sub> being connected to the bus-bars. The method of paralleling the two dynamos is as follows:

The incoming dynamo D<sub>2</sub> is run up to its normal speed, and by adjusting the field rheostat it is allowed to excite itself to approximately the same voltage as that of D<sub>1</sub>. When the voltmeters V<sub>1</sub> and V<sub>2</sub> indicate the same, the switch S<sub>2</sub> is closed, thus connecting D<sub>1</sub> and D, in parallel. If at the instant of paralleling the two machines have the same terminal pressure, then the switch S<sub>2</sub> may be closed without any current flowing either into or out of D<sub>2</sub>. After paralleling, if the field current of D, be increased, the voltage generated is also increased, so that D<sub>2</sub> will begin to take some of the load while the load on D, will diminish. The exact proportion in which the total current divides between the two machines will depend on their respective internal E.M.Fs. and armature resistances. The condition which determines this division of current is, that after deducting the volts drop due to the armature

resistance of either machine from its total internal E.M.F., the remainder or terminal voltage must be alike in both cases. Thus if two similar machines, similarly excited and run at the same speed, be connected in parallel, each will take half the total current, and the proportion of the current which each machine supplies can be regulated by the shunt rheostat.

Assuming the two machines D<sub>1</sub> and D<sub>2</sub> to be equally loaded, then if there be a slight momentary decrease in the speed of D<sub>1</sub>, the E.M.F. generated by it will decrease, thus shifting a larger portion of the current on to D<sub>2</sub>. The decreased loss over the armature resistance of D<sub>1</sub> and the decreased armature reaction along with the resulting slight increase in the speed of the prime mover, combine to increase both the internal and terminal E.M.F. of D<sub>1</sub>. At the same time the increased current through D<sub>1</sub> tends to reduce the terminal E.M.F., with the result that the electrical inter-reactions of the two machines exert an inherent tendency to equalise their speeds and loads.

In order to disconnect one of a number of dynamos in parallel, its load is shifted over to the other dynamos by gradually reducing its field current and increasing the field current of the other generators. When the current output of the machine to be disconnected is reduced to almost zero the main switch is opened.

Compound Dynamos in parallel.—If two compound-wound dynamos are paralleled by connecting their main terminals to common bus-bars, as shown in Figure 223, they will be unstable. Suppose that two machines D<sub>1</sub> and D<sub>2</sub> are connected in parallel and have their excitation adjusted so that each supplies one-half of the total current delivered to the mains. If D<sub>1</sub> runs momentarily at a slightly decreased speed a momentary decrease in the induced E.M.F. is effected, which in turn diminishes the current supplied by D<sub>1</sub> and increases the current of D<sub>2</sub>. The decreased current supplied by D<sub>1</sub> decreases the strength of the series excitation, so that the induced E.M.F. and current output will be still further reduced. When once started, this unequal

distribution of current supplied by the two machines increases more and more until the load on D, becomes excessive, while the current supplied by D<sub>1</sub> is reduced to The latter is finally driven as a motor taking current from D<sub>0</sub>.

To eliminate this instability and to ensure the proper distribution of load among two or more compound dynamos connected in parallel, the terminal of each dynamo at which the armature and field coils are connected in series is joined through switches S<sub>8</sub> and S<sub>4</sub> to a common conductor, known as an equalising busbar, and shown in Figure 224. The series coils of the

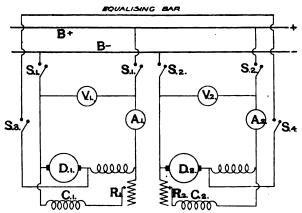


FIG. 224.—Compound dynamos in parallel.

dynamos D<sub>1</sub> and D<sub>2</sub> are thus connected in parallel with The equalising bus-bar must be of each other. negligible resistance as compared with the series coils.

 $\tilde{\text{To}}$  connect machine  $D_2$  in parallel with machine  $D_1$ , when the latter is supplying current, D2 is run up to speed and excited so as to give the same voltage as D<sub>1</sub>, the excitation being provided by the shunt winding only. Switch S<sub>4</sub> is then closed. This excites the series field to its proper amount, and the shunt current is adjusted until the voltage at the terminals of D2 is the same as D<sub>1</sub>. The switch S<sub>2</sub> is closed, and the machine may be made to supply current by adjusting the field rheostat.

If it be required to unparallel machine D<sub>2</sub>, its shunt excitation should be slightly reduced until it supplies a very small current, after which S<sub>2</sub> and S<sub>4</sub> are opened. The opening and closing of the equalising and main switches in the required order may be conveniently effected by a 3-pole switch S<sub>1</sub> (Figure 287), in which the equalising connection is made first on closing the switch, and broken last on opening it.

Should the speed of one of a number of dynamos connected in parallel slow down to such an extent that the voltage generated is less than that of the bus-bars, then current would flow into it from the other machines, i.e. the faulty dynamo would be driven as a motor. To prevent this an automatic circuit-breaker (described on page 493) is usually connected between each dynamo and the bus-bars, so that a dynamo may be disconnected from the latter, when either its current falls to zero or a predetermined reverse current flows.

# BOOSTERS

A booster is a dynamo which is used to alter the voltage of a circuit in which an E.M.F. already exists. The operation is known as boosting, and was first suggested by Professor Perry. A booster may be driven by an electric motor, a steam engine, or any other suitable prime mover. The usual practice, however, is to drive it at constant speed by a shunt motor. The booster armature is connected in series with the circuit in which it is desired to alter the voltage, while the field magnets may be excited in various ways, depending upon the manner in which the pressure has to be altered.

Boosters are principally employed for—(1) Raising the voltage of feeders, which are of much greater length than others connected to the same bus-bars: in such cases the increased voltage due to the booster compensates for the fall of potential in the feeders resulting from ohmic resistance. (2) Altering the voltage of a battery circuit, so that current may flow from the generators to the battery and so charge it, or vice versa.

Feeder Booster.—Figure 225 shows two feeders  $F_1$  and  $F_2$  connected to central station bus-bars B + and B -, the pressure of the latter being maintained constant at say 460 volts. Now suppose that the pressure at the distributing end A of the feeders is also required to be maintained constant at 460 volts, and that the fall of potential along the feeder at full load is 20 volts. To ensure this, the pressure at the generator end of the feeder is regulated by means of a booster B driven by a motor M. The armature and field windings of B are connected in series with the feeder  $F_1$ . Since the field of the booster is excited by the line current the excita-

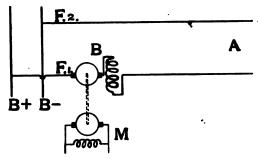


FIG. 225.—Diagram of connections for feeder booster.

tion and consequently the value of the boosting E.M.F. will vary with the feeder current. The fall of potential in the feeder will be directly proportional to the current transmitted, and in order that the booster may truly compensate for any fall of potential it should be designed so that the E.M.F. generated is directly proportional to the exciting current, *i.e.* the load current. To effect this boosters are worked on the straight line portion of their magnetisation curve, *i.e.* the part AB, Figure 218. Should they be designed to work on or above the knee of the curve, the saturation of the field magnets would prevent the induced E.M.F. varying in direct proportion to the exciting current.

Battery boosters may be divided into two classes-

- 1. Irreversible.
- 2. Reversible.

Irreversible Booster.—Figure 226 shows the method of connecting a booster to charge a battery B, which when discharging is connected in parallel with the generator G. The booster armature A is driven by the motor M, and the field coils F are connected across the bus-bars. The pressure generated by the armature can be varied by a rheostat R in series with the field. The armature is connected to the contacts a a of a double-pole throw-over switch S. When the latter is at b b the battery is connected in parallel with the generator. To charge the battery the switch S is thrown over to a a,

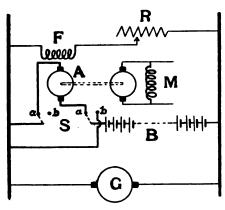


FIG. 226.—Shunt booster for battery charging.

thus connecting armature of the booster series with the battery. The rheostat in the field is then adjusted so that the requisite charging current flows from the bus-bars through the the charging voltage being equal to that of the bus-bars plus that of the booster. As the charge proceeds the latter can be increased by adjusting

the rheostat R until, when the cells are nearly charged, the voltage will be about 2.5 per cell. After the cells have been charged the switch S is thrown over to b, thus cutting the booster armature out of circuit.

Automatic Reversible Boosters for Traction generating Plants.—In all traction generating stations the load undergoes violent fluctuations, and in order to equalise the load on the generators a secondary battery is, as a rule, connected in parallel with the bus-bars. The connections are such that when the load is equal to the normal output of the generators, the bus-bar and battery E.M.Fs. are equal. If the load be less than normal, the battery E.M.F. is lowered and a current flows from the generators through the battery, thereby charging

it; on the other hand, should the load be greater than normal the battery discharges, owing to an increase in its E.M.F. Under such conditions the share of the load which falls upon the generators remains approximately constant, the battery taking in all the surplus current from the generators when the load falls below normal, and supplying the excess current when the load is above normal.

If the generators were compounded for a constant E.M.F. at all loads, then a battery alone is of little use; for when current is taken out of it, its voltage will fall and the discharge cease; and when a current is put into it, the voltage will rise and the charge cease. In most traction systems in Britain and America the generators are over-compounded, in which case a battery connected direct across the bus-bars would simply increase the fluctuation of load; at heaviest loads the increased pressure of the generators would send the maximum charging current through the cells.

It will now be evident that a battery used to maintain a constant load on the generators must have some auxiliary machine connected in series with it in order to overcome the above-mentioned difficulties. batteries are therefore worked in conjunction with Automatic Reversible Boosters, and the combined battery and booster is often referred to as a floating battery.

The advantages of this are—

(1) Saving in initial capital outlay on boilers, engines, and generators. The actual advantage under this heading is, however, considerably reduced owing to the large capital outlay on battery and booster.

(2) High working efficiency owing to the constant

operation of the plant at full load.

Differential Boosters.—A diagram of connections for a reversible differential booster is given in Figure 227. The armature A of the booster is driven by the motor M and the field magnets are excited by shunt and series coils S<sub>H</sub> and S<sub>E</sub> respectively. S<sub>H</sub> is connected in parallel with the mains  $F_1$  and  $F_2$ , and  $S_E$  in series with  $F_1$ , the two windings acting in opposition. At normal load the field windings neutralise each other, so that the booster pressure

is zero, and the battery B will be neither charged nor discharged. When the line current is less than the normal output the shunt winding predominates, and the booster generates an E.M.F. in such a direction that it adds to the pressure of the generator G and so charges the battery. With a current greater than normal the series winding predominates, and therefore changes the polarity of the booster terminals, thus adding to the pressure of the battery circuit and helping to discharge the battery.

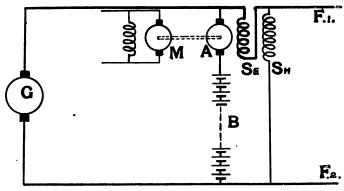


FIG. 227.—Reversible differential booster.

In the case of this simple differential booster, the current supplied to, or taken from, the battery is dependent upon the E.M.F. of the latter as well as upon the line current. Suppose, for instance, that when the battery is fully charged its E.M.F. is equal to that of the bus-bars, then at normal load the booster will be neutral and the battery current zero. But if the battery be not fully charged and the load is again normal, the booster will still be neutral, and since the battery voltage will be less than that of the bus-bars a current will flow from the generators to charge the battery. The current supplied to, or taken from, the battery is thus dependent upon the E.M.F. of the latter.

In order that the battery output will be dependent only upon the load, the simple differential booster requires to be fitted with an additional exciting coil C, which is connected across the booster terminals, as

shown in Figure 228. The current in the coil C will thus be proportional to the difference between the battery and bus-bar E.M.Fs. With this arrangement the shunt coil S<sub>H</sub> is connected in parallel with the battery.

When the battery volts are equal to the bus-bar volts no current flows in C. If the battery pressure be lower than that of the bus-bars a current flows through C in one direction, and in the reverse direction when the battery pressure is the greater. The winding of the

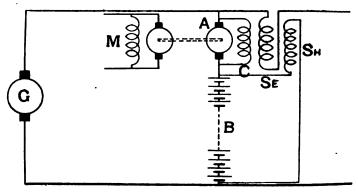


FIG. 228.—Differential reversible booster.

coil C is such that for every volt fall of the battery the booster gives one volt positive and vice versâ.

The action of the booster will be best illustrated by a concrete example. Suppose the bus-bar voltage and average output of the plant be 500 volts and 500 ampères respectively. When the feeder current is at the normal value of 500 ampères the coils SH and SE will neutralise each other so that the booster E.M.F. is zero. Now suppose the feeder current rises to 900 ampères, 400 of which would be supplied by the battery; this will cause the E.M.F. of the latter to fall to say 460 volts. Under these conditions a current of such a value will flow in the coil C that it will give exactly 40 volts positive to the booster, so that the battery and booster volts will be 460 + 40 = 500 = bus-bar volts. As the discharge continues the battery pressure will fall

still lower, but for every volt it falls coil C will add one volt to the booster.

Suppose, next, that the load falls to 100 ampères. Since the generator field will be adjusted so that its output current remains approximately constant at 500 ampères, 400 ampères must go to charge the battery. This will cause the battery E.M.F. to rise to about 540 volts, and the current in the coil C to reverse, so that the booster voltage equals -40. The battery and booster volts will therefore be 540 - 40 = 500, the bus-bar voltage.

This example shows how the generator may be maintained constantly at full load, and all variations in output taken up entirely by the battery.

When the average output of the plant is greater than 300 ampères, the series winding of the booster may be shunted with a low-resistance, adjustable diverter, so that the current in the coil  $S_{\rm E}$  is a definite percentage of the total output current.

Exciter Control or Highfield Booster.—Figure 229

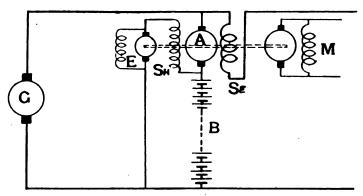


FIG. 229.—Highfield's exciter control booster.

illustrates the principle of a second form of reversible booster designed by J. S. Highfield. The booster armature A is driven by a motor M as before. The field magnets of the booster are wound with two coils  $S_{\rm H}$  and  $S_{\rm E}$ . The series coil  $S_{\rm E}$  carries either the main current or a definite percentage of it. The shunt or fine wire coil  $S_{\rm H}$  is connected, through a small shunt-excited

generator E, across the battery terminals as shown. The machine E, generally referred to as an exciter, is mechanically coupled to the motor and booster shaft. The exciter is designed to give any pressure between 500 and 550 volts, a regulating rheostat being connected in series with its field coils, and is so connected that it opposes the E.M.F. of the battery, tending to send a current through the coil S<sub>E</sub>.

The windings of the coils  $S_H$  and  $S_E$  are such that when the line current is normal, the sum of the booster and battery E.M.Fs. is equal to that of the bus-bars. Any increase of load above normal augments the excitation of the coil  $S_E$ , thereby increasing the booster E.M.F. and causing the battery to discharge. When the load is less than normal the reverse takes place.

The function of the exciter is to render the battery current independent of the battery E.M.F. Suppose, for example, that the battery is fully charged, then when the load is normal the excitation of E is adjusted so that its E.M.F. is equal to that of the battery, with the result that no current flows in the coil  $S_H$ . On the other hand, if the battery be *not* fully charged when the load is normal, its E.M.F. will be less than that of the exciter, and a current will flow through the coil  $S_H$  in such a direction that it assists the coil  $S_H$  in such a direction that it assists the coil  $S_H$  and so increases the booster E.M.F. by an amount which balances the drop in E.M.F. of the battery; hence the battery will still receive no current, even although its pressure be less than that of the bus-bars.

When the battery is being either charged or discharged a similar regulation occurs, the shunt coil of the booster being so designed that any difference between the exciter and battery E.M.Fs. causes an exciting current to flow, which alters the booster E.M.F. by an amount equal to the difference. For example, if the field rheostat of E be set to give 550 volts, then should the battery pressure fall to 530 volts, the resulting current in the coil S<sub>H</sub> would raise the booster E.M.F. by 20 volts in a discharge direction. When the pressure of the battery rises above that of the exciter, a current flows through E in the reverse direction, thus driving

it as a motor. At the same time, the booster generates a reverse E.M.F. equal in value to the rise of battery pressure. The exciter thus runs as a motor when charging and as a generator when discharging.

Carbon Rheostat Controlled Booster.—Another principle of booster control, due to Entz, is illustrated in Figure 230. The field winding S<sub>H</sub> of the booster is of fine wire and connected in series with an exciter E. The

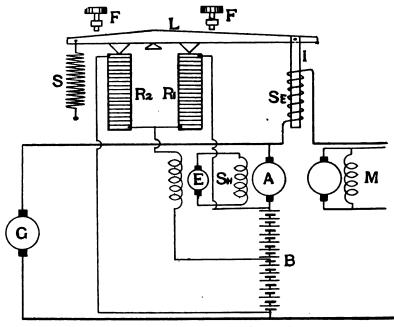


FIG. 230.—Reversible booster controlled by carbon rheostat.

armature A of the booster, along with that of the exciter, is mechanically coupled to a constant speed motor M. The field coils of E are connected across the middle point of the battery B and the middle point of a carbon-regulating resistance R<sub>1</sub> R<sub>2</sub>, consisting of a number of carbon discs connected across the battery. The former are subjected to a varying pressure by a rocking lever L. From one end of the latter is freely suspended a softiron core I, which lies inside a solenoid S<sub>E</sub> excited by the output current. To the other end of L is attached a

helical spring S, the tension of which may be adjusted by hand, to counterbalance the pull of the solenoid at any desired output. Slight variations of load above or below this amount will alter the mechanical pressure on the carbons R<sub>1</sub> R<sub>2</sub>. The result is a wide variation in the contact resistance, the resistance of one set of carbons increasing while that of the other set diminishes, or vice versa, according as the lever L moves one way or another. The controller is so adjusted that when L is horizontal the two sets of carbons R<sub>1</sub> R<sub>2</sub> have the same resistance. The potential of the middle point of R, R, will then be the same as the middle point of the battery, with the result that no current flows in the field of the exciter.

Should the load increase above normal, the increased current through S<sub>E</sub> pulls down I against the spring S, thus reducing the resistance of the carbons R<sub>1</sub> and increasing that of R<sub>2</sub>. A difference of potential will then exist between the terminals of the exciter's field coils, and the resulting current will induce an E.M.F. and so excite the booster field in such a direction that the booster E.M.F. adds to that of the battery, and so allows it to discharge. With loads less than normal the reverse takes place.

The action of the lever L on the carbons is limited in either direction by adjustable mechanical stops F F, which may be set to limit the battery charge and dis-

charge current to any predetermined maximum.

When automatic reversible boosters are used in conjunction with over-compounded generators, the series windings of the latter must be connected so that they are traversed by a current proportional to the total output current, and not by the generator current alone. With the latter arrangement no compounding would be effected, since the generator current is maintained approximately constant at all loads.

Boosters have to be designed for heavy currents, and their armatures are therefore lap-wound. As they rarely work at their full-rated output, the current density in the inductors may be much higher than that recommended for ordinary dynamos. In reversible boosters

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the magnet cores are generally laminated, to ensure a quicker reversal of the polarity of the field than would be the case with solid cores. Since boosters are worked low down on their magnetisation curves the fields are necessarily weak, even at times when the armature current is great, so that sparking troubles are liable to occur, unless great care is taken in designing the armature to have low reactance and sparking voltages. Boosters in which the current varies within wide limits can with advantage be fitted with commutation poles.

### CHAPTER XI

#### MOTORS—STARTERS AND CONTROLLERS

Principle of the Motor.—The construction of the electric motor is based upon the principle that when a current is sent through a conductor which lies across a magnetic field the conductor is acted upon by a force tending to move it in a direction at right angles to the lines of force. In Figure 231 is shown an inductor C

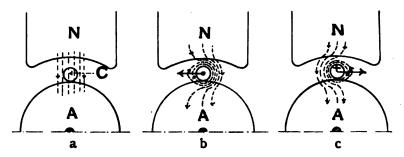


FIG. 231.—Principle of the motor.

placed on the periphery of a soft-iron core A, centred on bearings between poles N and S (the latter not shown) of an electro-magnet. When no current flows through C, the magnetic flux due to the poles leaves the N pole, crosses the air-gap, and passes through the core A to the S pole in the manner shown at a. When current is sent through the inductor C in a direction towards the observer (as indicated by the dot at the centre of the section of the conductor), it is encircled by lines of force, which move in a clockwise direction. The direction of the lines of force surrounding the inductor is, on the right-hand side, the

same as that of the lines due to the main field, while on the other side their direction is opposite. As a result the main flux is distorted, so that the field on the left-hand side is weakened, and strengthened on the right-hand side as shown at b.

To grasp the resultant effect produced upon the inductor by this distortion, the student is commended to the following mechanical analogy: Regard the lines of force in the air-gap between N and A as being straight strips of spring steel deflected towards the right by the pressure against them of a bar C. The reaction of the springs endeavouring to re-straighten themselves tends to push the bar back again, i.e. to return to the electrical reality, to push the inductor C across the magnetic field in the direction indicated by the arrow in the figure. Now if the inductor be fixed to the iron core A it will be clearly seen that the latter must rotate when the push acting on the inductor is sufficient to overcome the mechanical friction between the spindle of the core and its bearings. When the direction of the current in C is reversed, as shown by the crossed circle at c, the direction of the lines of force surrounding C is also reversed, and thereby also the direction of rotation of the core.

If H denote the strength of the magnetic field in the air-gap due to the poles N and S, and l the length in centimetres of inductor which is under the influence of the magnetic field, then, when a current of i C.G.S. units flows in the inductor, it is acted upon by a force  $f = H \times l \times i$  dynes.

If a direct-current dynamo be supplied with current from an external source it will run as a motor giving out mechanical energy; and, irrespective of the number of field-poles or the type of armature winding, the electro-dynamic action between the main field and all the armature inductors carrying current will tend to produce rotation in one direction. The function of the electric motor is to convert electrical energy into mechanical energy. It is therefore the converse of the dynamo.

Design of Motors.—The general principles involved in the electric and magnetic design of the two machines

are identical, but the constructional details vary to suit the purposes for which each is intended. Motors are often required to run in either direction, and in such cases the brushes are set radially in the geometrical neutral axis. The design of brush-holder shown in Figure 175 is suitable for motors required to run in either direction.

A dynamo is invariably erected in a specially arranged engine-room, whereas a motor is usually placed, irrespective of environment, as near to its load as can be conveniently arranged, and in this way may be exposed to dust or to weather, be near inflammable material, or liable to mechanical injury. Except for very small sizes, motors are as a rule now multipolar, and the bearings contained in either extensions of the field yoke or accurately fitted end covers, which enclose more or less completely the armature, commutator, and brushes, as is shown in Figure 232. When motors can be erected in clean and well-ventilated buildings, where they are not likely to be injured, there is no necessity for enclosing these parts; but when placed in exposed positions they should be totally enclosed. Motors of this latter type are invariably used for tramway and mining work, but for less arduous applications a semi-enclosed or even opentype motor can with advantage be installed.

The Direction of Rotation of a Motor.—If the posi-

tive and negative terminals of a shunt dynamo be connected with the corresponding mains of a source of supply S, as shown in Figure 233, then the direction of the current through the armature A will be the reverse of that generated by itself,

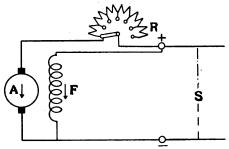


FIG. 233.—Diagram of motor connections.

while the direction of the current in the field coils F will still be the same as when generating. In the case of a dynamo it was shown (page 248) that the current flowing in the armature opposes the direction of rotation, so that the armature current being reversed the motor represented in the figure will rotate in the same direction as when generating. To reverse the direction of rotation of any motor it is therefore necessary only to reverse either the direction of the field current or the current through the armature, but not both.

Counter E.M.F. of a Motor.—When the armature of a motor rotates an electromotive force is generated in the inductors as they cut the lines of force of the field magnets; but by Lenz's law the E.M.F. thus induced opposes the direction of the current and is therefore known as a counter e.m.f. The value of this e.m.f. is expressed by  $e = 4TNM10^{-8} = 4T\frac{RP}{60}M10^{-8}$ , where T

is the turns per circuit through the armature, R the armature speed in R.P.M., p the number of pairs of poles, and M the magnetic flux entering the armature. The existence of this counter e.m.f. may be observed by connecting a voltmeter across the armature terminals, and when the main current is switched off the voltmeter takes several seconds to fall to zero, reaching zero when the armature comes to rest.

Torque and Power of a Motor.—When current flows through the armature of a motor each inductor is acted upon by a force  $f = H \times l \times i$  dynes, and if the armature consist of C inductors, then the total force acting on the armature is expressed by  $F = H \times l \times C \times i$  dynes. The torque on the armature due to the field is equal to the product  $F \times \frac{d}{2}$ , where d is the diameter of the armature.

The power given out by a motor =

 $P = torque \times angular \ velocity$ 

= 
$$F \times \frac{d}{2} \times 2\pi \times \frac{R}{60}$$
 dyne-centimetres per second

= H × 
$$l$$
 × C ×  $i$  × 2  $\pi \frac{d}{2}$  ×  $\frac{R}{60}$  dyne - centimetres per second.

Multiplying both numerator and denominator by 2 p

$$P = H \times l \times \frac{2\pi d}{2} \times \frac{2p}{2p} \times \frac{R}{60} \times i \times C \text{ dyne-centimetres per second.}$$

But  $\frac{H \times l \times 2\pi d}{2} \times \frac{1}{2p}$  = approximately the flux M entering the armature per pole; C = 2Tq, where T is the turns per circuit through the armature, and q the number of circuits; and  $i = \frac{i_t}{q}$ , where  $i_t$  is the total current in C.G.S. units entering the armature. Substituting these values in the last equation

P = M × 2 
$$\frac{Rp}{60}$$
 ×  $\frac{i_t}{q}$  × 2  $Tq$  dyne-centimetres per second  
= 4 T ×  $\frac{Rp}{60}$  × M ×  $i_t$  dyne-centimetres per second.

Now 4 T  $\times \frac{Rp}{60} \times M$  is the value of the counter e.m.f. in C.G.S. units, and may be denoted by E, so that  $P = E \times i$ , C.G.S. units.

The counter e.m.f. expressed in volts =  $e = E \times 10^{-8}$ , and the current input in ampères =  $I = i_t \times 10$ . Now since I watt =  $10^7$  C.G.S. units, the output of the motor is expressed by

$$P = E \times i_t \times 10^{-7}$$
 watts  
=  $E \times 10^{-8} \times i_t \times 10 = e \times I$  watts.

That is, the rate at which work is done is given by the product of the counter e.m.f. in volts, and the current in ampères flowing through the armature.

If S be the torque in dyne-centimetres with which the field magnets act upon the armature, then the mechanical work done by the motor per second

= S x angular velocity in radians per second

$$= S \times 2\pi \frac{R}{60}$$
 dyne-centimetres

=  $S \times 2\pi \frac{R}{60} \times 10^7$  watts: but the power developed by the motor is also equal to  $e \times I$  watts, so that

$$S \times 2\pi \frac{R}{60} \times 10^7 = e \times I.$$

Therefore 
$$S = \frac{e \times I}{R} \times \frac{10^{-7} \times 60}{2\pi}$$
 dyne-centimetres.

Torque = 
$$\frac{e \times I}{R} \times \frac{10^{-7} \times 60}{2\pi} \times \frac{I}{981} \times \frac{I}{1000} \times \frac{I}{100}$$
 kilogramme-metres

$$= e \times \frac{I}{R} \times 0.96$$
 kilogramme-metres.

But  $e = 4 \text{ T} \times \frac{Rp}{60} \times M \times 10^{-8}$ , so that substituting this value in the above equation

Torque = 
$$4 \times T \times \frac{Rp}{60} \times M \times 10^{-8} \times \frac{I}{R} \times 0.96$$
 kilogramme-  
metres =  $0.65 \times p \times T \times M \times I \times 10^{-9}$  kilogramme-metres.

That is, the torque or turning effort of a given motor is proportional to the armature current and the magnetic flux per pole. Of course the effective torque at the pulley of the motor will be less than that given by the above equation by the amount required to overcome the mechanical and iron losses.

Example.—From the following data regarding a 4-pole motor calculate the total horse-power developed by the motor when the armature current is 50 ampères.

Flux entering the armature per pole  $(\hat{M}) = 4.0$  megalines.

Turns per circuit through the armature = 160.

Number of circuits = 2.

Speed of armature = 500 R.P.M.

Torque acting on the armature

=  $0.65 \times 2 \times 160 \times 4.0 \times 10^{6} \times 50 \times 10^{-9} = 41.5$  kilogramme-metres.

Power developed by motor

= torque x angular velocity in radians per second

= 
$$41.5 \times 2\pi \times \frac{500}{60}$$
 = 2170 kilogramme - metres per second.

I British H.P. = 76 kilogramme-metres per second, so that the total power developed by motor

$$=\frac{2170}{76}=28.5$$
 H.P.,

of which about 5 per cent. would be absorbed in overcoming the mechanical friction and iron losses, so that the B.H.P. at motor pulley

$$=28.5 \times \frac{95}{100} = 27.$$

Fundamental Equation of a Motor.—The E.M.F. which is applied at the terminals of a motor is known as the impressed E.M.F., and will be denoted by E. This E.M.F. may be divided into two components—(1) the component e, which balances the counter e.m.f., and (2) the component  $R_aI$ , which overcomes the armature resistance. The impressed E.M.F. will therefore be expressed by

$$E = e + R_a I = 4 T \frac{Rp}{60} M 10^{-8} + R_a I.$$

This is the fundamental equation for a direct-current motor, and a useful form is that which expresses the current I in terms of the other quantities, thus:

$$I = \frac{E - e}{R_a}.$$

E must always be greater than e, but if the motor be designed so that the no-load losses are small, then when the motor is running unloaded e will be very nearly equal to E. The product (E-e) I represents the power required to overcome the mechanical and iron losses of the machine, and if e were equal to E it would mean that no power was required to drive it.

Example.—A 30-B.H.P. 220-volt motor has to be designed to run at a speed of 600 R.P.M., and have an efficiency at full load of 90 per cent. The motor has 4 poles, and the flux entering the armature per pole equals 3.9 megalines. Calculate the number of inductors if the armature be wave-wound, and the watts absorbed due to armature resistance be limited to 235 watts.

Full-load current of motor (I) =  $\frac{30 \times 746}{220} \times \frac{100}{90} = 113$  ampères.

Armature resistance ( $R_a$ ) not to exceed  $\frac{235}{113^2} = 0.0184$  ohms.

Flux per pole  $(M) = 3.9 \times 10^6$  megalines. Impressed E.M.F. (E) = 220 volts.

$$\frac{R \cdot p}{60} = \frac{600}{60} \times 2 = 20.$$

From the fundamental equation, turns per circuit through the armature

$$= T = \frac{E - R_a I}{4 \times R/ \times M \times 10^{-8}} = \frac{220 - (0.0184 \times 113)}{4 \times 20 \times 3.9 \times 10^{6} \times 10^{-8}} = 70.$$

Therefore total number of armature inductors  $= 70 \times 2 \times 2 = 280$ .

Starting of a Motor.—When a motor is at rest the speed R and consequently the counter e.m.f. is zero, so that if the impressed E.M.F. be applied direct to the motor terminals the current  $I = \frac{E}{R_a}$ . Now  $R_a$  is always

a small fraction of an ohm, so that the current I would be excessively large. To avoid this excessive rush of current when a motor is being started, a variable resistance R (Figure 233) must be connected in series with the armature, and as the speed increases this resistance is, step by step, cut out of circuit until at full speed the only resistance in the armature circuit is that of the armature itself.

From the fundamental equation of a motor the speed may be expressed in terms of the other quantities, thus:

$$R = \frac{E - IR_{\alpha}}{4 T \times \cancel{p} \times M \times 10^{-8}} = \frac{E - IR_{\alpha}}{T \times \cancel{p} \times M \times 0.66 \times 10^{-9}}$$

That is, the speed of a motor is directly proportional to the counter *e.m.f.*, and inversely proportional to the number of turns per armature circuit, the number of poles, and the flux per pole. In well-designed motors the value of IR<sub>a</sub> is very small compared with E, and as T

and p are constants for a given machine the speed of a motor is expressed approximately by  $R = K \frac{E}{M}$ , where K

is a constant. Thus the speed of a direct-current motor can be controlled either by varying the E.M.F. impressed on the armature terminals or the strength of the magnetic field.

Speed Characteristic of a Motor.—The speed characteristic of a motor is the curve which shows the variation of speed with exciting current when the

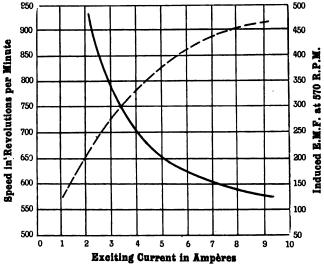


FIG. 234.—Speed characteristic of a shunt motor.

counter e.m.f. is maintained constant. The latter condition may be observed by separately exciting the field coils and allowing the motor to run unloaded with a constant pressure across the armature terminals. A typical speed curve is shown in Figure 234, where values of speed are plotted as ordinates, and values of exciting current as abscissæ. The magnetisation curve for the same machine when run as a dynamo is shown dotted, so that comparison may be made between the two curves.

When the exciting current is zero the speed is very great, since R = K  $= \infty$ ; this is shown by the curve

approaching the ordinate reference line asymptotically when the exciting current is very small. As the excitation increases the magnetic flux increases rapidly (as will be seen from the magnetisation curve), and since the speed varies inversely as the latter, the speed will decrease rapidly until the field magnets are nearly saturated, at which stage a large increase in the exciting current produces a very small increase in the magnetic flux, and consequently a very small decrease in speed. The value of exciting current, at which the field magnets are saturated, is shown by the speed curve approaching the abscissæ reference line asymptotically.

Armature Reaction.—As has been explained, for a

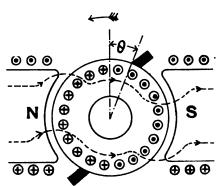


FIG. 235.—Distortion of the magnetic field in a motor.

given direction of rotation the current in the armature motor flows in the reverse direction that which it would do if run as a dynamo. effect armature ampère-turns will be to distort the magnetic flux in the opposite direction to the rotation of the armature, with

the result that the flux density in the air-gap under the trailing pole tips is diminished, while that under the leading pole tips is increased, as shown in Figure 235. Thus in the case of a motor the brushes must be moved backwards through an angle  $\theta$ , if it be desired to obtain perfect commutation. This, as in the case of a dynamo, produces a number of back ampère-turns, which tend to demagnetise the field magnets. The extent of the demagnetising action can be calculated (as shown on page 327) when the angle through which the brushes have been moved from the geometrical neutral axis is known. In order that the current may be commutated without undue sparking, the field magnets of motors, required to run in either direction, should be

nearly saturated, thereby reducing distortion at full load to a minimum.

## SHUNT-WOUND MOTORS

Regulation.—Shunt motors are as a rule supplied with current at constant potential, and within the thermal limits of output they can be made to run at approximately constant speed. When a shunt motor is loaded it is essential that the counter e.m.f. decrease sufficiently to allow enough current to flow through the armature for developing the requisite torque. The counter e.m.f. being given by  $e = 4T \frac{Rp}{60} M$  10<sup>-8</sup>, a decrease can be effected by a diminution either in speed or magnetic flux. If the brushes be set at the geometrical neutral axis there will be a natural tendency for the speed to decrease as the load increases. The speed of a motor is expressed  $E - IR_a$ by  $R = \frac{E - 1 N_a}{T \times p \times M \times 0.66 \times 10^{-9}}$ , so that if the flux remain constant the speed will be proportional to E-IR<sub>a</sub>. If R<sub>a</sub> be large, then the speed of the motor will fall off more rapidly as the load increases than would be the case if R<sub>a</sub> were small. Thus the best speed regulation is obtained by designing the armature to have a low resistance. The falling off in speed of a shunt motor, having its brushes set in the geometrical neutral axis, as the load is increased from no load to full load, ranges from 3 per cent. of the no-load speed in largesized motors to 7 per cent. or more in small sizes. If the brushes be set with a slight backward lead the reaction of the armature will decrease the magnetic flux as the load increases, so that the armature reaction tends to increase the speed. Under the latter conditions the necessary decrease in the counter e.m.f. as the load increases is brought about partly by a diminution in the magnetic flux M and partly by a diminution in the speed. The net decrease in speed is less than would be the case if the brushes were set in the neutral axis, when M of course would remain constant in value.

If absolutely constant speed is desired it may be

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attained by setting the brushes with such an angle of backward lead that as the load increases the necessary reduction in the counter e.m.f. is obtained by a decrease in the magnetic flux, thus allowing the armature speed to remain constant at all practical loads. The conditions of operation of a shunt motor, however, are rarely such that a few per cent. variation in speed between no load and full load is of any consequence, and the brushes are set with a view to obtaining the best commutation results. Since the magnetic flux is approximately constant, the torque increases in direct proportion to the current input.

Starting Rheostat.—Figure 236 is a diagram show-

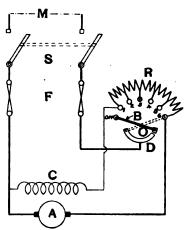


FIG. 236.—Diagram of connections for a shunt motor.

ing the simplest arrangement of connections for a shunt motor, the latter being connected to the supply mains M through a double pole switch S, double pole fuse F, and starting rheo-The latter consists of a switch arm B which can be moved about O through an angle of 90 degrees or thereabouts, so that one end of it passes over a number of contact studs marked 1 to 6, while the other end passes over but remains in contact with

the quadrant-shaped bar D. The resistance R is divided into five sections, each of which is connected between two successive contact studs in such a manner that they are all in series, as shown in the figure. When the switch S is closed and the switch arm B of the starter moved on to stud No. 1, the field coils C are connected directly across the mains and the armature, through the whole of the starting resistance, which is of a value that permits the armature current to produce sufficient torque to start the motor. As the speed increases the switch B is moved slowly over the studs 1 to 6, cutting out

resistance until, when it reaches the last stud (as shown by the dotted lines), the motor is running independent of the starting resistance, with its armature directly across the mains.

Suppose that after the motor has thus been run up the supply is interrupted, and the motor consequently stopped, with the arrangement shown the connections would remain as adjusted, and on the supply being reestablished an excessive current would flow through the armature and probably destroy it. An excessively large current might also pass through the armature should the motor be heavily overloaded. To meet such contingencies starting rheostats for shunt motors may be provided with devices for automatically returning the switch lever B to the off position. These contrivances are respectively styled no-voltage and overload releases.

Figure 237 shows the construction of a starting rheostat provided with no-voltage and overload releases. The connections between the mains and the motor are indicated by the red lines. The rheostat consists of two principal parts—(1) a multiple contact switch and safety devices mounted on a slate base Q; (2) a series of resistances fixed in a ventilated cast-iron box. The construction and arrangement of the resistance, and the method of fixing it to the containing box, is similar to that of the regulating resistance shown in Figure 222.

The switch-arm A, shown in detail at (a), is of brass, and cast with a hollow boss B, which is fitted to a centre pin C so that the switch arm can be moved over the contact studs E<sub>1</sub>. Contact is made with the studs by means of a laminated copper brush D<sub>1</sub>, which is secured into a recess at the end of the switch arm. In a similar way contact is made with the quadrant E2, by means of the brush D<sub>2</sub>. These laminated brushes ensure a better electrical contact between the switch arm and the studs than is the case with solid brushes. The studs and quadrant are of cast copper, and the wire F makes permanent connection between resistance and stud. The contact area between the brush and the stud should be sufficient to permit of a current density of about 50 ampères per square centimetre.

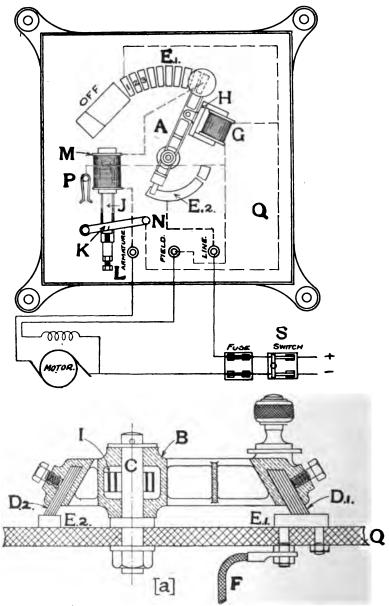


FIG. 237.—Shunt motor starting switch.

The no-voltage release consists of an electro-magnet G having an iron core and wound with an exciting coil,

which is connected in series with the shunt coils of the motor. When the switch A has been moved to the last contact, the iron armature H loosely attached to the switch arm comes into contact with the poles of the electro-magnet and is held against the recoil of a strong steel spring I enclosed inside the boss of the switch arm. Should the motor be disconnected from the supply mains or the supply interrupted, the electro-magnet G is denergised and the recoil of the spring I causes the switch arm to fly back into the off position, so that the motor cannot be restarted without inserting the starting resistance.

The overload release consists of a solenoid, of which the adjustable iron plunger J is fixed to an aluminium lever K and held by the adjusting screw L so that its upper end lies at the mouth of the coil M, which is connected in series with the armature circuit. The lever K is pivoted at N, and when the plunger is pulled up its full length the other end of K makes connection with the stud P through two copper spring contacts. N and P are each connected to a terminal of the exciting coil of G. When current flows in the armature circuit the coil M tends to pull up the plunger J, and when the armature current exceeds a predetermined limit it is pulled up sufficiently to come into contact with P, thereby short-circuiting the coil of the electro-magnet G, which consequently releases the switch arm.

At the lower end of the slate base are three terminals marked armature, field, and line, from which connections are made to these respective parts. When the motor is connected to the supply mains by closing the main switch S and bringing the switch arm on to the first stud, current flows from the positive main to the line terminal, and thence to the armature and negative main by way of quadrant E, switch arm A, stud No. 1, starting resistance, overload coil M, and armature terminal. As the switch is moved over the studs the resistance is gradually cut out, and when contact is made with stud No. 6 the switch is held in that position by G.

From the diagram it will be seen that one end of the shunt winding is connected to the negative terminal of

the armature, and the other to the terminal field, from whence connection is made through the no-voltage coil G to stud No. 1. By this arrangement the field circuit is closed simultaneously with that of the armature, and when the switch lever is held up by the electro-magnet G the exciting current flows continuously through the starting resistance. Thus, when the motor is being stopped by withdrawing the main switch the field is left connected across the armature and starting resistance, so that it is subjected to the gradually decreasing voltage of the former. Consequently there is no sudden rise of potential due to the self-induction of the field coils which would otherwise result.

Design of Starting Resistance. — The current i required to start a motor with its load from rest is greater than the normal full-load current I. When the switch arm is moved on to the first contact of the starting switch there will be no counter e.m.f., and at the moment of starting the current taken by a motor is expressed by

$$i = \frac{E}{r + R_a} \tag{1}$$

where E denotes the pressure of the supply mains, R<sub>a</sub> the armature resistance, and r the starting resistance in series with the armature when the current first attains a value capable of starting the motor. If n denote the number of steps into which the resistance is divided, then  $r = r_1 + r_2 + \dots + r_n$ . After the motor attains the speed which is normal for the first contact the current falls to its normal value I. Let  $e_1$  denote the counter e.m.f. generated when the switch arm is on the first stud, then the normal current is such that

$$I = \frac{E - e_1}{r + R_a} \tag{2}$$

When the switch arm is moved on to the second stud the counter e.m.f. will still have a value  $e_1$ , but since the resistance r has been diminished by  $r_1$  the current increases to a value i expressed by

$$i = \frac{E - e_1}{(r - r_1) + R_a} \tag{3}$$

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Each time the switch arm is moved from one contact to another the current will suddenly increase and then fall in the same ratio as the counter *e.m.f.* increases. The current I is that required to provide the necessary torque for accelerating the rotation of the armature, and the value of the resistance cut out as the switch arm is moved from one stud to another should be such that the ratio  $\frac{i}{I}$  is constant during the whole time the motor is accelerating.

After the motor has been running for some time with the switch arm on the second stud the counter e.m.f. will have attained a value  $\epsilon_2$ , and the current will fall to the normal value I, so that

$$I = \frac{E - e_2}{(r - r_1) + R_a}.$$
 (4)

Similarly when the switch arm passes on to the third stud the current increases to the value

$$i = \frac{E - e_2}{(r - r_1 - r_2) + R_a}$$
 (5)

but will immediately fall to normal, that is

$$I = \frac{E - e_3}{(r - r_1 - r_2) + R_a}.$$
 (6)

As the switch arm is moved from the first stud to the second, the ratio of  $\frac{i}{I}$ , as obtained by dividing equation (3) by (2), equals

$$\frac{i}{I} = \frac{r + R_a}{(r - r_1) + R_a}.$$
 (7)

Similarly when the switch arm is moved from the second stud to the third

$$\frac{i}{I} = \frac{(r - r_1) + R_a}{(r - r_1 - r_2) + R_a}$$
 (8)  
[the quotient of equations (5) and (4)].

The ratio of  $\frac{i}{I}$  for a starting resistance having n steps is given by the general equation

$$\frac{i}{I} = \frac{r - (r_1 + r_2 + \dots + r_{n-1}) + R_a}{r - (r_1 + r_2 + \dots + r_{n-1} + r_n) + R_a}.$$
 (9)

There will be n equations, and if they be multiplied together

$$\frac{\binom{i}{I}^{n}}{r-r_{1}+R_{a}} \left( \frac{r-r_{1}+R_{a}}{r-r_{1}-r_{2}+R_{a}} \right)$$

$$\frac{\binom{r-(r_{1}+r_{2}+\ldots+r_{n-1})+R_{a}}{r-(r_{1}+r_{2}+\ldots+r_{n-1}+r_{n})+R_{a}}$$

$$= \frac{r+R_{a}}{r-(r_{1}+r_{2}+\ldots+r_{n-1}+r_{n})+R_{a}}$$

Now  $r = r_1 + r_2 + \dots + r_n$ , and from equation (1)  $r = \frac{E}{r} - R_n$ , so that

$$(\frac{i}{I})^n = \frac{\frac{E}{i} - R_a + R_a}{R_a} = \frac{E}{iR_a}.$$

But  $n \log \frac{i}{1} = \log \frac{E}{iR_a}$ , so that the number of steps required in order that the current shall not exceed i ampères when the switch arm is moved from one stud to another is given by the equation

$$n = \frac{\log \binom{E}{iR_a}}{\log \binom{i}{I}}.$$
 (10)

Note.—In order that there be no alteration in the current in moving the switch arm from one stud to another, *i.e.* when i = 1, the number of steps into which the starting resistance must be divided

$$= \frac{\log \binom{E}{iR_a}}{\log \binom{I}{I}} = \frac{\log \binom{E}{iR_a}}{o} = \infty.$$

From equation (10) it will be obvious that the greater the number of steps the smaller will be the momentary increase in current in passing from one stud to another. Having determined the number of steps required for a given starting resistance, the resistance required for the first step can be obtained from equation (7), and is expressed by

$$r_1 = \{r + R_a\} - \left\{ (r + R_a) \cdot \frac{I}{i} \right\}$$
  
=  $\{r + R_a\} \left\{ I - \frac{I}{i} \right\}$ 

Similarly the resistance required for the second step is obtained from equation (8) and =

$$r_2 = \{(r-r_1) + R_a\} \left\{ I - \frac{I}{i} \right\}$$

From the above it will be seen that the resistance required for any step n of a starting rheostat is given by the general equation

$$r_n = \{ (r - r_1 - \dots - r_{n-1}) + R_a \} \left\{ I - \frac{I}{i} \right\} (II)$$

In the above equations it has been assumed that the necessary starting current passes through the armature when the switch arm comes on to the first contact, but in order that the current may be increased gradually to that required for starting, rheostats for large motors are provided with more steps than that given by equation (10). In motors taking less than 25 ampères the starting resistance should allow sufficient current for starting to pass through the motor when the switch arm is on the first stud. Starters for motors taking from 30 to 100 ampères should allow the starting current to be reached on the second stud, while motors taking still larger currents should start up when the switch lever comes on to the third stud.

The rheostat for starting a motor without load does not require to have as many steps as that required for a motor starting with the load on. The no-load starting current seldom exceeds 20 per cent. of that required for

normal full load. Let the former and the latter be respectively denoted by  $i_0$  and  $i_1$ , then since the maximum current at starting can be allowed to attain the full-load value the number of steps is given by

$$n = \frac{\log\left(\frac{E}{i_1 R_a}\right)}{\log\left(\frac{i_1}{i_0}\right)}.$$

Example.—A 12-B.H.P. 220-volt shunt motor requires a current of 46 ampères when running normally at full load. If the maximum starting current has not to exceed 60 ampères, determine the number of steps required for the starting resistance and the resistance of each step. The armature has a resistance of 0.35 of an ohm.

From equation (10) the number of steps into which the resistance must be divided would be =

$$\frac{\log\left(\frac{220}{60\times0.35}\right)}{\log\left(\frac{60}{46}\right)} = \frac{\log 10.5}{\log 1.3} = \frac{1.0212}{0.1139} = 9.$$

Since the starting current is 60 ampères it should attain this value in two steps, so that the actual number of steps = 9+1=10, *i.e.* there will be 11 contact studs. On the first contact 30 ampères should be allowed to pass through the motor, so that the total resistance in the armature circuit when the switch arm is moved on to the first contact =  $\frac{220}{30}$  = 7.3 ohms.

Since the motor should start on the second contact stud and the starting current should not exceed 60 ampères, the total resistance in the armature circuit when the switch is moved on to the second contact is equal to  $\frac{220}{60} = 3.65$  ohms: but the armature itself has a resistance of 0.35 of an ohm, so that the resistance between contacts 2 and 11 = 3.65 - 0.35 = 3.3 ohms, while the resistance between contacts 1 and  $2 = R_1 = 7.3 - 3.65 = 3.65$  ohms.

From equation (11) the second step of the starting resistance (i.e. the first step for which the current is equal to the starting current)

= 
$$r_1 = (r + R_a) \left( 1 - \frac{I}{i} \right)$$
  
=  $(3.3 + 0.35) \left( 1 - \frac{46}{60} \right) = 3.65 \times 0.235 = 0.86 \text{ ohm.}$ 

Again, the resistance of the third step

$$= r_2 = (3.3 - 0.86 + 0.35) \left(1 - \frac{46}{60}\right)$$
  
= 2.79 × 0.235 = 0.66 ohm.

Similarly

$$r_3 = 0.50$$
  $r_7 = 0.17$   
 $r_4 = 0.38$   $r_8 = 0.13$   
 $r_5 = 0.29$   $r_9 = 0.10$   
 $r_6 = 0.22$ 

Another method of determining the value of the resistance of a shunt motor starter is derived as follows: From equations (7), (8), and (9) it will be seen that

$$\frac{i}{I} = \frac{r + R_a}{(r - r_1) + R_a} = \frac{(r - r_1) + R_a}{(r - r_1 - r_2) + R_a} \cdot \dots 
= \frac{(r - r_1 - r_2) \cdot \dots \cdot r_{n-1} + R_a}{(r - r_1 - r_2) \cdot \dots \cdot r_n + R_a}.$$

If  $R_1$  denote the resistance in the armature circuit when the switch arm is on the first stud,  $R_2$  that when on the second, and  $R_n$  that when on the  $n^{th}$  stud, then  $R_1 = r + R_n$ ,  $R_2 = (r - r_1) + R_n$ , and  $R_n = (r - r_1 - r_2) + R_n$ .

Substituting these values in the above equation,

$$\frac{i}{I} = \frac{R_1}{R_2} = \frac{R_2}{R_3} = \dots = \frac{R_n}{R_{n+1}}.$$
 (12)

That is, the steps of the resistance  $R_1$ ,  $R_2$ ...  $R_n$  form a geometrical series whose constant ratio is  $\frac{i}{\bar{1}}$  and whose first and last terms are  $\frac{E}{i}$  and  $R_n$  respectively.

The method of applying equation (12) to determine the number of steps and the resistance per step is set forth in the following example:

Example.—A 10-B.H.P. 460-volt motor takes 20 ampères at full load. If the maximum starting current has not to exceed 30 ampères, determine the number of steps required in the starting resistance and the resistance of each step. Armature resistance equals 0.6 of an ohm.

Resistance in armature circuit when the switch arm comes on to the first stud

$$= R_1 = \frac{E}{i} = \frac{460}{30} = 15.4 \text{ ohms.}$$
Since  $i = 30$  and  $I = 20$ ,  $\frac{i}{I} = \frac{30}{20} = 1.5$ .

From equation (12) the resistance in armature circuit when the switch arm comes on to the second stud

= 
$$R_2$$
 =  $R_1 \times \frac{I}{i}$  = 15.4 ×  $\frac{I}{1.5}$  = 10.3 ohms.

Similarly with the other steps of the resistance. The values of  $R_1$ ,  $R_2$ , . . .  $R_{n+1}$  are respectively given by

The last term  $R_{n+1} = 0.6$  is the value of the armature resistance, so that the starting resistance will be divided into 8 steps. The resistance of the first step = 15.4 - 10.3 = 5.1; similarly the resistance of the second step = 10.3 - 6.8 = 3.5. The values of the resistance of the steps 1 to 8 are respectively given by

When starting rheostats were first introduced, the invariable practice was to distribute the resistance equally between all the steps. This method was soon, however, discarded, as it gave very unequal increments of current, the result being excessive sparking and uneven acceleration. Figures 238 and 239 illustrate the case of a 10-H.P. 400-volt starting rheostat having a total resistance of 18 ohms and 10 contact studs.

The resistance of the armature, brushes, and brush

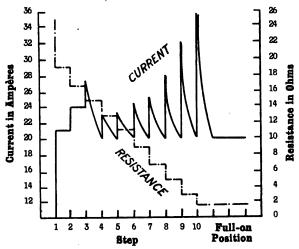


FIG. 238.—Curve illustrating the fluctuations in current when starting resistance is equally distributed.

leads was I ohm. The former figure indicates the fluctuations in starting current when the resistance is

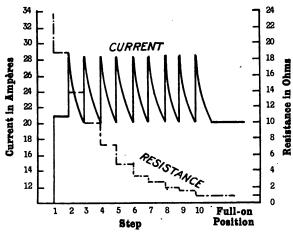


FIG. 239.—Curve illustrating the distribution of a starting resistance designed to secure equal increments of current per step.

equally divided between the contacts. If instead of equal divisions the resistance be divided up so that

the resistance in circuit on successive steps forms a geometrical ratio, then the current increments will be equalised, as shown in Figure 239.

The resistance coils of motor-starting rheostats are made from such alloys (see Table XV. p. 372) as are used for shunt-regulating resistances, and the formula for determining the size of wire is obtained as follows:

Let R be the resistance of the wire in ohms, a the area of cross-section in square centimetres, l the length in centimetres, and  $\rho$  the specific resistance, then the rate of generation of heat due to the passage of a current of C ampères

= 0.24 
$$C^2R = 0.24$$
  $C^2 \frac{\rho \times l}{a}$  calories per second.

Further, let s denote the specific heat of the wire, g its specific weight, and T° the temperature rise per second above the surrounding air. To produce this rise of temperature in one second the heat generated =  $l \times a \times g \times s \times T^{\circ}$ calories. The time required for starting a motor does not usually exceed 30 seconds, so that the amount of heat radiated during starting may be neglected, in which case

 $l \times a \times g \times s \times T^{\circ} = 0.24 \, C_{a}^{2\rho} \times l$ , i.e. the rise of tempera-

ture per second

$$= T^{\circ} = 0.24 \times \frac{C^2}{a^2} \times \frac{\rho}{sg}.$$

Suppose the wire carries the current C for t seconds, and let T<sub>1</sub>° denote the permissible temperature rise of the wire above the surrounding air, then the rise of temperature per second

$$= \frac{T_1^{\circ}}{t} = 0.24 \times \frac{C^2}{a^2} \times \frac{\rho}{sg}, \text{ and the area of cross-section}$$

of the wire

= 
$$a = \sqrt{\frac{0.24 \, \text{C}^2 \, \rho \, t}{s \, g \, \text{T}_1^{\circ}}} = 0.155 \, \text{C} \sqrt{\frac{\rho}{s \, g} \times \frac{t}{\text{T}_1^{\circ}}}$$

For starters, a temperature rise of about 150° C. is usually permitted, so that

$$a = 0.0126 \text{ C}\sqrt{\frac{\rho}{s_{\mathcal{L}}} \times t}$$
.

Example.—In the starting resistance calculated in the previous example determine the size and length of wire required for the resistance between the last contacts. The resistance coils are to be made from platinoid wire, and it may be assumed that the motor is started in 20 seconds, and that the switch arm is moved uniformly over the contacts.

Resistance of the step = 0.3 of an ohm.

The maximum current = 30 ampères.

The minimum current = 20 ampères.

Therefore average current (C) = 25 ampères.

From Table XV. (p. 372)  $\rho = 0.00004$  ohm per centimetre cube, g = 8.6, and s = 0.098.

The area of cross-section of wire

$$= a = 0.0126 \times 25\sqrt{\frac{0.00004 \times 20}{0.098 \times 8.6}}$$

= 0.0097 square centimetres.

Diameter of wire

= 
$$d = \sqrt{\frac{4^a}{\pi}} = \sqrt{\frac{4 \times 0.0097}{\pi}} = 0.112$$
 centimetres.

Nearest size of standard wire = No. 18 S.W.G. Length of wire to give the requisite resistance

$$= l = \frac{\pi \times d^2 \times R}{\rho \times 4} = \frac{\pi \times 0.22^2 \times 0.3}{0.00004 \times 4}$$
$$= 88 \text{ centimetres.}$$

Liquid Starting Resistance.—Figure 240 illustrates the principle of the liquid starting switch. A cast-iron trough A contains a solution usually of sal-ammoniac or caustic soda. Dipping into the trough is an iron plate B which swings about the pivot C. The latter is supported on an insulated bracket bolted to the trough at E. Projecting from the plate B is an arm F to which a suitable insulated handle is attached. One terminal T<sub>1</sub> is connected to the trough and the other T<sub>2</sub> is mounted on a porcelain block G and connected by means of a flexible cable to the movable plate. In operating the switch the plate B is lowered into the

liquid, and current flows from it through the liquid to the sides of the trough, thus introducing a certain resistance into the circuit of which the starter is a part. As the plate B is lowered, the resistance offered by the liquid is gradually decreased until it is finally short-circuited by the copper blade H engaging with the contact I mounted on the trough.

An inherent drawback to the use of liquid starters is that the electrolyte is subject to evaporation, and is

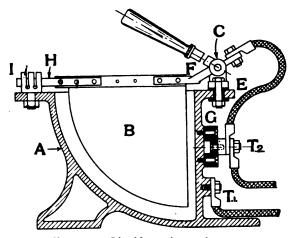


FIG. 240.—Liquid starting resistance.

also liable to become frozen. Liquid starters are invariably used for mining work, where an accumulation of gas would be fired by the flashes occurring with a metallic starting rheostat.

## SPEED CONTROL OF SHUNT MOTORS

Shunt motors find their widest scope in stationary applications such as the driving of machine tools, looms, lines of shafting, etc. It is often desirable to be able to vary the speed of a motor over a wide range, and this can be accomplished in a shunt machine by varying either the current through the field coils or the E.M.F. impressed upon the armature.

Speed Variation by Field Adjustment.—This method

of varying the speed is the one more often used, and is accomplished by connecting a variable resistance in series with the field coils, the former being of similar construction to the dynamo shunt rheostat described on page 374. The field coils of a variable speed shunt motor are so designed that it runs at minimum speed when the field magnets are nearly saturated. When the magnetic flux is diminished in order to increase the speed, the operation of shunt motors, unless fitted with some compensating device, becomes unsatisfactory, as the reactions of the armature begin to preponderate over the weakened magnetic field. The result is that the distortion is increased until a speed is attained, where further increase is practically impossible owing to the serious sparking which occurs.

Experience has shown that the maximum practical range of speed control of ordinary shunt motors by means of field resistance is about 50 per cent., though 400 per cent. is practicable if commutation poles be fitted. The coils exciting the latter are connected in series with the armature, and are so connected that they provide the reversing field necessary for sparkless commutation. Shunt motors working over a large range of speed are as a rule now of this design.

The value of the shunt-regulating resistance required to give a certain range of speed is determined from the speed characteristic of the motor in question, as is shown

in the following example:

Example.—A 15-B.H.P. 460-volt motor, whose speed characteristic is given in Figure 234, is required to give a range of speed of from 600 to 900 revolutions per minute by means of field adjustment. If the field coils have a resistance of 655 ohms at the normal working temperature, determine the value of the resistance of the rheostat.

For speeds of 600 and 900 R.P.M. it will be seen from the speed curve that the values of the exciting current are 0.7 and 0.23 respectively. Since the field coils and regulating resistance will be connected in series across 460 volts, the shunt resistance at a speed

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of 600 R.P.M. =  $\frac{460}{0.7}$  = 655 ohms; but this is the value of the resistance of the shunt coils when warm, so that the lower speed limit will be obtained when all the regulating resistance is cut out.

To obtain a speed of 900 R.P.M. the field current must be reduced to 0.23 ampère by having a total shunt

resistance of  $\frac{460}{0.23}$  = 2000 ohms. Thus the shunt rheostat must have a resistance of 2000 - 655 = 1345 ohms. The number of steps into which this resistance will be divided will of course depend upon the degree of speed regulation required.

Speed Variation by varying Armature impressed E.M.F.—The E.M.F. impressed on the armature terminals may be varied in three ways: (1) Rheostat in armature circuit, (2) Multiple voltage control, and (3) Potential regulator.

Rheostat in Armature Circuit.—If the E.M.F. across the shunt coils be maintained constant the speed of a shunt motor may be varied from full speed to zero by means of a variable resistance in the armature circuit. This method of manipulation is very wasteful, due to the C<sup>2</sup>R loss in the rheostat, the loss in which, at certain speeds, is often considerably more than the power required to drive the motor. Again, for a given position of the rheostat the speed will vary with the load on the motor, i.e. as the current taken by the armature. Owing to these two disadvantages this method of speed control is only infrequently used in special circumstances.

Multiple Voltage Control.—By this method of speed control, current is supplied from three or more bus-bars, between which constant E.M.Fs. are maintained. The shunt coils are connected permanently to one pair of the supply mains, and by means of a suitable controller the armature can be connected to any pair of mains depending upon the voltage required at its terminals. For instance, if three pressures, E, 2E, and 3E, are available, then by means of the controller the armature can be supplied with current at any of these pressures,

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and the corresponding speeds would be approximately R, 2 R, and 3 R. To obtain intermediate values of speed a field rheostat is connected in series with the shunt This system of speed control is very expensive in initial cost, as it is of course necessary to provide several generators and an elaborate system of wiring.

Figure 241 shows how the two pressures of a 3-wire system may be utilised for giving a large range of speed. In the 3-wire system the pressure between the two outer wires + and - is twice that between either outer

and the middle wire M, and by means of a double-pole throwover switch the armature may be supplied with current either pressure. The switch contacts C and D are respectively connected to the 2V and V volt mains, while the armature A is connected through the starting resistance R<sub>1</sub> to the common contacts E. The field coils F are connected through a shunt rheostat R, to the 2V volt mains. With all the shuntregulating resistance out of circuit a minimum speed R will be obtained, when the arma-

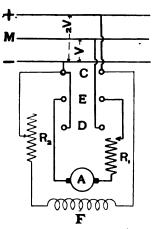


FIG. 241.—Two-voltage method of speed control.

ture is connected across the V volt mains. When the switch is thrown over to the 2V volt side the speed will be approximately doubled. Intermediate values of speed are obtained by field adjustment. If when the armature is connected across 2V volts a speed of 2R is obtained with the maximum field, the speed can be further increased to about 3R by introducing resistance into the field circuit. Thus with a V and 2V volt supply the speed of a shunt motor, having a field rheostat, may be varied through a range of 200 per cent.

Potential Regulator.—The potential regulator method of speed control is shown diagrammatically in Figure 242. A is the armature of the main motor which is to be driven at a variable speed, and its field winding F is excited from a source of constant pressure E. The armature of the motor is supplied with current from a generator G which is driven at constant speed by the auxiliary motor M, the latter being supplied with current from the mains E. The field coils of the generator are also excited from the mains E, and con-

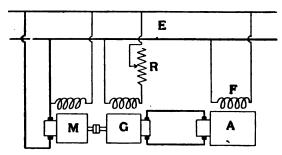


Fig. 242.—Speed control by potential regulator.

nected in series with them is a field rheostat R, which is of sufficient range to change the exciting current from its full value to nearly zero. The voltage across the armature terminals of the main motor can thereby be varied from zero to the greatest voltage obtainable from the generator, when the field of the latter is fully excited.

When it is desired to start the motor the shunt rheostat of the generator G is adjusted so that the magnets are weakly excited, thus sending a current of low potential through the armature, thereby causing the latter to revolve at a slow speed. To accelerate the motor, resistance is cut out of the generator field, thus increasing the E.M.F. on the armature terminals. The speed of the motor can then be varied by increasing or decreasing the current through the generator field by means of the shunt rheostat.

The potential regulator system of speed control is the most expensive to instal, since every main motor must be provided with two auxiliary machines. It is, however, the most perfect method of speed control, a finely graded regulation being obtained from zero to full speed. This principle of speed control has been adopted for operating high-speed hoists, battleship-turrets and other equipments where accuracy of control is of great importance.

## COMPOUND-WOUND MOTORS

There are two classes of compound-wound motors: first, *Differential*, *i.e.* those in which the series winding opposes the shunt winding; and second, *Cumulative*, or those in which the series winding reinforces the shunt.

Differential.—In the former the series winding causes the magnetic field to decrease with the load, thus compensating for the fall in speed which would result if the motor were simply shunt-wound. Differential compound motors are, however, rarely used, as a shunt motor can be made to run at approximately constant speed at all loads by setting the brushes with a slight backward lead. Furthermore, there is the objection that special means have to be adopted for short-circuiting the series winding while the motor is being started up, otherwise the series field, with its lower inductance, would rise to its full strength much more quickly than the shunt field, with the result that, due to the preponderance of the former, the motor would start in the wrong direction.

Cumulative.—Since the two windings of a cumulative compound motor act together the speed will decrease with increasing load, and the extent of the decrease in speed will depend upon the relative strengths of the shunt and series windings. If, for example, the shunt winding of a motor of this type supply 4000 ampèreturns per pole and the series winding, at full load, 1500 ampère-turns, then, neglecting magnetic saturation and drop in volts in the armature and series coils, the

speed at full load will be  $\frac{4000}{5500} \times 100 = 73$  per cent. of the no-load speed; but in designing a compound motor the dimensions of the field magnets would be such that they are nearly saturated by the field ampère-turns at full load, and the effect of the saturation of the magnetic

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circuit prevents the speed at full load from falling below

say 80 per cent. of the no-load speed.

In the case of motors required to operate intermittent and heavy loads, when there is no objection to the heaviest work being performed at much lower speeds, this large decrease in speed as the load increases is a great advantage to the supply system, as the generating plant is more evenly loaded, and so maintains a better potential equilibrium in the system. Moreover, much better commutation will result if a motor carry its heaviest loads at reduced speeds, since the periodicity

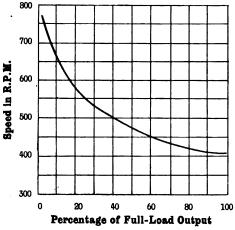


FIG. 243.—Speed curve of cumulative compound motor.

of commutation, and therefore the reactance voltage for given current, proportional to the speed.

Figure 243 shows the manner in which the speed of a cumulative - connected compound motor varies with the load. As the load is increased from zero speed rapidly

falls, but at full load.

or a few per cent. overload, the field magnets become saturated, and when the load is increased beyond this, the speed is not further reduced.

The torque of a compound motor at first increases much more rapidly than the output, owing to the large increase in the strength of the magnetic field; but when the magnetic circuit is nearly saturated the strength of the field increases only slightly with the load, and the torque only at a slightly higher rate than the output. Compound-wound motors are becoming more widely used for such special purposes as hoists in mining work, rolling mills, etc., where heavy intermittent loads are often encountered. The great advantage of the compound motor over the series motor for such classes of work is that the speed of the former does not increase indefinitely when the load is removed and the motor left connected to the supply mains.

The method of connecting a compound motor to the supply mains is the same as in the case of a shunt motor, so that the design and construction of the motor-starting gear, shown in Figure 237, serves equally well for a compound machine, the speed of which can be controlled, at any particular load, by means of a shunt rheostat.

## SERIES-WOUND MOTORS

In a series motor the field coils are excited by the armature current, so that if it were not for the saturation of the magnetic circuit the flux would be proportional to the current input to the motor. As previously stated, the torque developed by a motor is proportional to the armature current and the strength of the magnetic field. When a series motor is at rest the counter e.m.f. is zero, so that at starting the current taken by the motor will be very large, and since this current also flows through the field winding, a large starting torque is obtained. Neglecting saturation of the magnetic circuit the torque developed by a series motor is approximately proportional to the square of the current input, so that it will develop its maximum torque at starting. For this reason, together with the fact that they permit of their heaviest loads being taken at reduced speeds, series motors are chiefly used for electric traction, electric cranes, and other work where a high-starting torque is required.

The current taken by a series motor, used for driving, say, an electric locomotive, is a maximum when the train is being started, and as it accelerates the back e.m.f. induced in the armature gradually reduces the motor current so that the torque tends to decrease. To counteract this, resistance can then be cut out, so that the motor continues to take the maximum current and consequently exert its maximun torque until normal speed is attained. At that stage all the resistance would

be out and the motor connected direct to the supply mains. In this way a motor can be arranged to start from rest, under full load, with a large torque, and to maintain this torque until up to speed. Under such conditions the acceleration is rapid, a condition of great importance in traction and crane work where stopping and starting is frequent.

If it were not for the saturation of the magnetic circuit and the internal pressure drop, the speed at constant terminal pressure would be inversely proportional to the current input; but series motors are generally

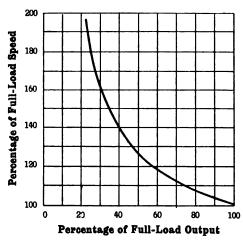


FIG. 244.—Speed curve of series motor.

designed to have their magnetic circuit nearly saturated full-load current, that the speed curve is of the form shown in Figure 244. From the latter it will be noticed that the speed approaches a constant value when the current input has attained its full-load 100 value, thus showing magnetic that the circuit has become saturated. As the

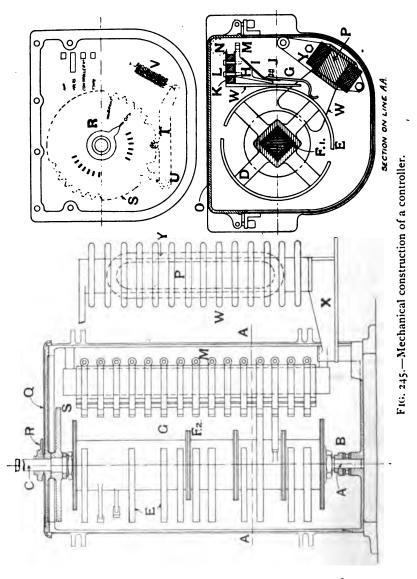
load on a series motor is diminished the speed rapidly increases, and when the current input approaches zero the speed rises indefinitely. This is due to the fact that the no-load current (which is just sufficient to give the necessary torque to overcome the no-load losses) produces a very weak magnetic field, the speed approaching infinity as the current approaches zero. Thus if the load on a series motor were suddenly thrown off, the resulting excessive speed would set up enormous centrifugal force, which would probably destroy the armature. Because of this possibility a series motor is only employed under such condition as that the load is always and inseparably connected to it, as is the case with

locomotives, street cars, cranes, etc. So far as torque is concerned, a series motor would be admirably suited for driving rolling mills, but the load on the latter often falls to zero. Compound motors are therefore used instead, the shunt excitation keeping the no-load speed within safe limits.

Controllers for Series Motors.—As previously mentioned, series motors are started with a variable resistance in series. As the motor accelerates the resistance is cut out in a suitable number of steps, and when normal speed is attained the motor is connected directly to the supply mains. Again, series motors are generally required to operate in either direction, so that arrangements must be made for reversing, when necessary, the direction of the current through the armature. The foregoing operations are generally performed by a drum controller. Rotation of the controller in one direction causes the motor to start forward gradually, also, cutting out the resistance. If the controller be rotated from the off position in the opposite direction, the previous connections to the armature are reversed, thus changing the direction of the current through the armature, and thereby reversing its direction of rotation. In both the forward and reverse running positions all the resistance is removed from the motor circuit.

Mechanical Construction.—Figure 245 illustrates the mechanical construction of a controller suitable for operating crane motors. It consists of a cast-steel spindle A carried on a ball-thrust bearing B, designed to take the weight of the rotating parts, and is manipulated by a handle fixed at C. On the spindle are mounted a series of cast-iron sleeves carrying arms D, to which are attached copper contact plates or segments E of varying lengths. The sleeves are insulated from the spindle as shown at F<sub>1</sub>, and from each other by the insulating rings F<sub>2</sub>.

A row of spring contact fingers G is fixed parallel to the drum, so that the segments on the latter make contact with the fingers as the drum is rotated. The contact fingers G (shown in detail in section on line AA) are of hard-drawn copper, and are linked to the brass carriers H by strips of phosphor-bronze I. The latter material is used to ensure a good spring contact, and the



tension is adjustable by means of a set-screw shown at J. The carriers H are clamped to an iron bar K, and insulated from it by micanite bushes and washers L

which fit over the bar throughout its entire length. The carriers are provided with terminals M and are connected by insulated wires to the armature, field coils, and various sections of the resistance. The connecting wires are brought through a hole N in the bottom of the controller shell. The contact plates on the drum are electrically connected to one another in such a manner that on rotating the drum the necessary connections between the armature, field coils, resistances, and supply mains are made.

A sheet-iron cover O completely encloses the working parts, and the top of the controller is provided with a cover Q, the plan of which is shown. An index R attached to the spindle passes over a marked dial and indicates the position of the controller. Immediately below the cover there is fixed to the spindle a ratchet disc S, which is engaged by a pawl T. One end of the latter is slipped over a steel pin U, and the other is attached to a strong spring V. This arrangement produces a snap action which renders it impossible for the controller arm to be accidentally left in an intermediate position between contacts. When in the off position the pawl engages in a slot, thus preventing over-riding and sudden unintentional reversal.

On breaking any of the motor or resistance circuits, serious arcs are liable to be set up between neighbouring segments and contact fingers. To prevent this, adjacent segments and contact fingers are separated by strips W of compressed asbestos insulating compound, which constitute fire-proof partitions. These asbestos strips are fixed to an iron arm X, which is hinged to the case and can be swung back to afford access to the fingers and other wearing parts. The elevation shows the arm X swung out, and the section at AA shows the position of the separating strips under working conditions.

Controllers are also fitted with magnetic blow-outs to extinguish the arcs set up when the contact fingers are disconnected from the contact plates on the drum. The magnetic blow-out, consisting of an electro-magnet, the coil Y of which is connected in series with the circuit controlled, is mounted on an iron core P attached to the arm X.

The drum of the controller becomes one pole of the blow-out magnet, and the arm X the other. When the latter is in position the magnetic flux set up by the electro-magnet passes from X, across the points of contact of the fingers, to the drum spindle A. If an arc be formed at the contact fingers it is drawn out by the magnetic field and thereby extinguished.

Reversing Series Motor Controller.—Figure 246 shows the development of a controller suitable for starting

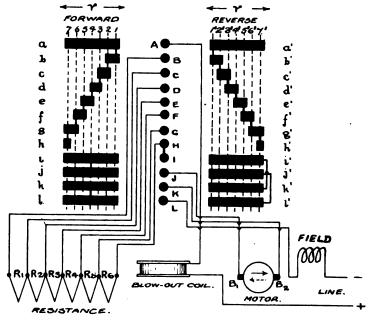


FIG. 246.—Diagram of connections for a reversing series motor controller.

and reversing a series motor. The spindle and contacts are shown cut through the off position and laid out flat. The distance r represents half the circumference of the drum, so that the length of each contact can be compared. There are two sets of contact plates on the drum. One set, marked a to l, is used when the motor is required to run in a forward direction, and the set marked  $a^1$  to  $l^1$  when the motor is required to run in the reverse direction. The contacts a, i, j, k, and l, along with the corresponding contacts on the other half of the drum, are in length a

little less than the distance r, so that after leaving the off position these contacts are always in connection with the corresponding set of fingers, whereas the shorter contacts, b to h and  $b^1$  to  $h^1$ , are only connected to their respective fingers one at a time. The contacts a to h are all electrically connected by fixing them to the same sleeve (see Figure 245), and similarly contacts i and j, k and l,  $a^1$  to  $k^1$ ,  $i^1$  and  $k^1$ , and  $j^1$  and  $l^1$ .

The circles lettered A to L represent the contact fingers: finger A is connected through the blow-out coil to the +ve main; fingers B to H are each connected to a section of the starting resistance, H and I being common. The armature is connected across I and K, while finger L is connected through the series field coil to the -ve main. When the controller is on the off position none of the fingers make contact with the plates. When the drum is turned so that line I is under the contact fingers, the motor starts up in the forward direction, and the path of the current is as follows: +ve main, blow-out coil, finger A, contacts  $\alpha$  and b, finger B, resistances  $R_1$  to  $R_6$ , fingers H and I, contacts i and j, finger I, through the armature from B<sub>1</sub> to B<sub>2</sub> (as indicated by arrow), finger K, contacts k and l, finger L, field and When line 2 comes under the contact - ve main. fingers the section R<sub>1</sub> of the starting resistance has been cut out, and in five successive steps, as indicated by the lines 3 to 7, the resistance is gradually cut out until on the seventh step the motor is connected direct to the supply mains. That this is so can be verified by tracing out the path taken by the current for the seven forward positions.

To reverse the direction of rotation of the motor, the controller is first moved back to the off position, and then moved from 11 to 71. When the drum is turned so that the line 11 is under the contact fingers, the path of the current is as follows: +ve main, blow-out coil, finger A, contacts  $a^1$  and  $b^1$ , finger B, resistances R<sub>1</sub> to  $R_6$ , fingers H and I, contacts  $i^1$  and  $k^1$ , finger K, through armature from B<sub>2</sub> to B<sub>1</sub> (as indicated by dotted arrow), finger J, contacts  $j^1$  and  $l^1$ , finger L, field and – ve main. In this position the previous connections of the armature

terminals are reversed, and consequently also the direction of rotation of the motor.

Crane Motor Controller.—Figure 247 shows the development of a controller for the lifting motor of an electric travelling crane. The contact segments are interconnected as shown. There are 13 operating positions. In the off position the contact segments and fingers are entirely disconnected. For lifting, the controller is moved from the off position through positions 1

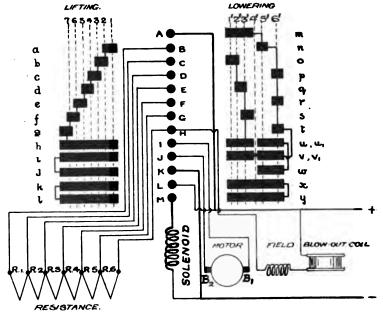


FIG. 247.—Diagram of connections for a crane controller.

to 7, thus reducing the resistance between the motor and the supply mains.

In position 1, the path of the current is as follows: +ve main, blow-out coil, field coils, finger H, starting resistances R<sub>6</sub> to R<sub>1</sub>, finger B, contacts a to h, finger I, through the armature from  $B_1$  to  $B_2$ , finger J, contacts i and j, finger K to the - ve main. From the +ve main current also flows by way of finger L, contacts k and L, and finger M, through a solenoid, and thence to the -ve main. This solenoid operates an electric brake

which comes into action when no current flows through the former, and from the diagram it will be seen that this only takes place when the controller is moved into

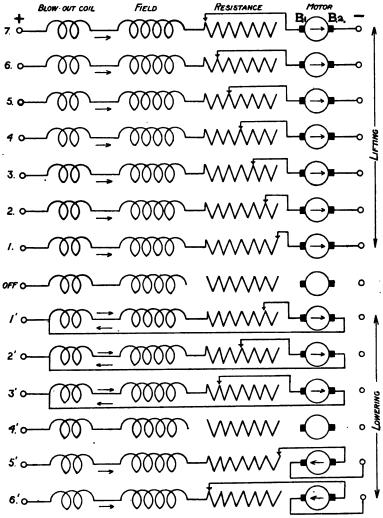


FIG. 248.—Key to crane controller (Fig. 245).

the off position. The construction and working of an electric brake suitable for crane motors is explained on page 433. As the controller is moved from position 1

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to 7, the starting resistance is step by step cut out of circuit, until at 7 the motor is connected direct to the supply mains. On positions 1<sup>1</sup> to 6<sup>1</sup> the lowering of the load takes place, and at the same time current flows through the brake solenoid, thus keeping the brake released. If the load being lowered is very small the controller is turned to positions 5<sup>1</sup> or 6<sup>1</sup>. With the controller in position 5<sup>1</sup>, the motor is in series with the starting resistance, but the current flows through the armature from B<sub>2</sub> to B<sub>1</sub>, i.e. in the opposite direction to that which it does in positions 1 to 7, so that the direction of rotation is reversed. In position 6<sup>1</sup> the motor is connected direct to the supply mains, and revolves in the same direction as when the controller is in position 5<sup>1</sup>.

If the load be sufficient to go down by its own weight then the controller is turned to position 41, where the motor is allowed to run free, the fingers connected to the motor being entirely disconnected from the segments, but current still flows through the brake solenoid. If the load be so heavy that it will go down too fast by its own weight, the controller is moved on to either positions 11, 21, or 31. The motor is then disconnected from the supply mains and runs as a generator, sending current through a portion of the resistance R<sub>1</sub> to R<sub>6</sub>. The energy of the descending load is thus converted into heat, and the motor and resistance are then said to act as a rheostatic brake. The lower the value of the resistance in series with the armature the greater will be the current generated, and consequently also the braking action tending to stop the motor. In position 11 the current thus generated flows from the brush B<sub>2</sub> of the armature to brush B<sub>1</sub> by way of finger J, contacts v and m, finger A, blow-out coils, field coils, finger H, resistances R<sub>6</sub> to R<sub>2</sub>, finger C, contacts o and u, and finger I. As the controller is moved from position 1<sup>1</sup> to 31 the resistance in series with the motor is diminished, and consequently the braking action increased. position 31 the resistance in series with the armature should be low enough to permit of such a current to flow as will stop the motor.

Figure 248 is a diagram of connections for the

13 positions of the controller, the direction in which the current flows in any position being indicated by the arrows. The brake solenoid has been omitted for the sake of clearness.

In the case of crane motors the starting resistance is frequently in use, and the intervals during which it does not carry current are so short that there is not sufficient time for the resistance to cool down materially. If the resistances for crane controllers were designed as for ordinary starters they would be insufficient, so that the usual practice is to design them for permanent loads, as is the case with regulating resistances described on page 373.

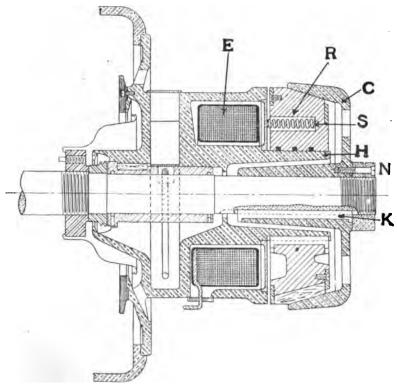


FIG. 249.—Electric brake for crane motor.

Electric Brake for Motors.—Figure 249 shows a type of electric brake suitable for crane and other

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motors where quick-braking action is necessary. The brake is formed on an extension of the commutator bearing, an annular space being provided in which is supported a well-insulated exciting coil E. On the extended hub H is carried a conical steel ring R, which is free to move laterally. In this ring several steel springs S are carried, which normally tend to push the ring away from the face of the magnet. At the extreme end of the motor shaft, a malleable iron crown C is keyed by the key K, and prevented from moving laterally by the nut N, which is fastened to the hub of the crown C by a set-pin.

When the motor is disconnected from the supply mains, the spiral springs S thrust the conical steel ring R into the crown, thus preventing the shaft from rotating. When the controller (see Figure 247) is moved so as to start the motor, current flows through the exciting coil E (marked solenoid in the latter figure), so that the electro-magnet is energised and overcomes the thrust of the springs. The ring R is attracted to the face of the magnet, thus leaving the

### CHAPTER XII

## DIRECT-CURRENT MACHINES—HEATING, LOSSES, EFFICIENCY, AND TESTING

#### HEATING AND LOSSES

So long as a machine is at work there is a continuous generation of heat in the armature, commutator, and field magnets, due primarily to the passage of a current. This appearance of heat implies that a corresponding amount of energy is lost, in so far as no useful work is derived from it. A machine should be designed so that the losses are reduced to the minimum consistent with initial cost. Having reduced the losses to the lowest practical limit, it remains to make the mechanical design of such a nature that the heat generated through this waste of energy does not cause the temperature of any part to become excessive.

Wherever heat is generated the temperature gradually and continuously rises above that of the surrounding air until it attains a value at which the rate of generation of heat is equal to the rate of loss of heat by radiation, convection, and conduction. The steady temperature to which any part of a machine will rise depends upon the extent and nature of the cooling surface provided, and from a knowledge of the energy lost in a particular part, that part should be designed to have sufficient radiating surface to prevent the temperature from exceeding a safe limit.

Maximum Permissible Temperature.—The maximum temperature to which any part of a machine may attain must be such that the insulation does not deteriorate, and such that no appreciable increase occurs in the

hysteresis loss in the armature core due to ageing of the iron. If the armature or field coils be maintained at a temperature of 80° C. or upwards, the insulation of these parts rapidly deteriorates, both as regards their electrical and mechanical properties. Cotton, and other fibrous materials used for insulating electrical conductors, become charred, and crumble away when subjected to the least mechanical strain, so that although the insulation may still remain comparatively high, the possibility of a breakdown is considerably increased.

Some engineers have suggested the exclusive use of such insulating material as mica and asbestos, which may be subjected to as high a temperature as 120° C. without the slightest deterioration: but supposing the armature conductors were allowed to attain to such a high temperature, the armature core would soon become heated to the same degree, and when iron has been subjected to prolonged heating at a temperature of 85° C. or more, its hysteresis constant is considerably increased. This so-called ageing is discussed on page 439, but it has been mentioned here to direct attention to the fact that if the iron core of a machine be maintained at a greater temperature than 85° C. the hysteresis loss increases.

To reduce to a minimum the deterioration of insulation and iron, the maximum temperature to which any part of a machine may rise, when working continuously, should not exceed 70° C. at the most, and the usual practice among British engineers is to fix 60° C. as the maximum permissible temperature. The permissible temperature rise will depend upon the temperature of the surrounding air during the working of the dynamo or motor, as the case may be. In well-ventilated central stations in Britain the temperature of the atmosphere seldom exceeds 20° C.: thus the permissible temperature rise would be greater than that for a dynamo which was to work in a tropical climate where the temperature of the dynamo-room would probably be about 40° C.

The usual practice is not to state the actual limit of temperature, but to specify the permissible temperature rise of any part of a machine, this being so chosen that under normal working conditions the heating does not exceed the safe limits mentioned above. The standard practice is to specify a temperature rise not greater than 40° C.

The output of a dynamo is therefore limited to the current which can be continuously carried by the armature without the permissible temperature rise being exceeded. Of course, in some machines commutation difficulties will limit the current output to a value much below that determined by thermal considerations. slow-speed machines the thermal limit is generally reached long before commutation difficulties are encountered, whereas the reverse is generally the case in high-speed machines; though, when the latter are fitted with commutation poles, thermal considerations, rather than sparking, limit the output.

Losses. — The losses occurring in direct-current machines may be classified as follows:

### Armature—

(1) C<sup>2</sup>R loss due to armature resistance.

(2) Iron loss due to (a) hysteresis, and (b) eddy currents.

## Commutator—

(3) C2R loss due to brush contact resistance.

(4) Brush friction loss.

## Field Coils—

(5) Excitation loss.

## Mechanical—

(6) Friction and windage.

The method of predetermining these losses and the resulting increase in temperature will now be considered, together with a brief discussion of their influence on the design of a machine.

## Armature

C<sup>2</sup>R Loss.—This loss is due to current flowing in the armature winding, and the resistance of the latter may be determined as follows:

Let L denote the length of one turn, T the turns per

circuit,  $\alpha$  the area of cross-section of conductor, and  $\rho$  the specific resistance of copper, then the resistance per circuit =  $\frac{\rho \times L \times T}{\alpha}$ , and if q denote the number of armature circuits, the total resistance of the armature

$$= \frac{\rho \times L \times T}{a \times q} \text{ ohms.}$$

In making calculations relating to resistance it is desirable to adopt some uniform temperature rise as a basis. This may conveniently be taken as 40° C., since it is the general specified value for ordinary machines: hence assuming the average temperature of the surrounding air to be 20° C., the resistance would be calculated on the assumption that the normal working temperature of the armature conductors is 60° C. The specific resistance of copper at 60° C. equals  $2 \times 10^{-6}$  ohms per centimetre cube.

Example.—Calculate the resistance, volts drop, and watts absorbed in an armature having the following constants:

Full-load current (C) = 60 ampères. Mean length of one turn (L) = 150 centimetres. Number of slots = 121.Inductors per slot = 6.Cross-sectional area of inductor = 0.072 square centimetre. Armature circuits (q)Number of face inductors  $= 6 \times 121 = 726.$ Total armature turns = 363.= 363/2 = 181.Turns per circuit (T)

Resistance of winding from positive to negative brush

$$= \frac{2 \times 10^{-6} \times 150 \times 181}{0.072 \times 2} = 0.37 \text{ ohm.}$$

Volts drop in armature =  $C \times R = 60 \times 0.37 = 22$ .  $C^2R$  loss at  $60^{\circ}$  C. =  $60^2 \times 0.37 = 1340$  watts. *Iron Loss: Hysteresis.*—The hysteresis loss in iron has already been discussed in Chapter III., where it was shown that the loss in watts per kilogramme might be calculated from the formula:

 $W_h = 0.000127 \eta B^{1.6} n.$ 

where—

 $\eta$  = hysteresis constant.

B = maximum induction.

n = magnetic cycles per second.

For armature laminations  $\eta$  has a value ranging from 0.0015 to 0.003. In Figure 24 is a curve of hysteresis loss for a sample of iron in which  $\eta = 0.003$ . The ordinates of the curve are calculated from the above formula, and give the watts lost per kilogramme for one cycle per second. Since the induction in the teeth of armatures is considerably greater than that in the rest of the core, the hysteresis loss in the teeth should be calculated separately.

The hysteresis loss in iron increases with continued heating, and this deterioration is known as ageing; but as to the change in the state of the iron producing this phenomenon there is at present no reliable information. The extent of this deterioration depends upon the composition of the iron and the temperature from which it has been annealed. The increase of hysteresis by ageing is greater with annealed iron than with unannealed This is clearly shown by the curves in Figure 250.\* Two samples of sheet iron were subjected to a temperature of 100° C. for over 600 hours, and the hysteresis constant measured at intervals. Curves A and B are respectively for good annealed and unannealed sheet iron. At the beginning of the test the hysteresis constant of sample A was practically the same as for sample B, but after a time it increased rapidly, while the hysteresis constant of B remained approximately constant.

Recent investigations show that as a general rule the brands of iron used in the construction of electrical machinery begin to age at a temperature of about

<sup>\*</sup> Journal of the Institution of Electrical Engineers, vol. xxxviii. p. 37, February 1907.

85° C., so that to avoid the possibility of increased loss through ageing the best practice is not to allow the iron to attain a temperature higher than 60° C.

Again, the hysteresis loss is found to increase when the iron is subjected to mechanical pressure, and W. M. Mordey has shown, in one test he performed, that

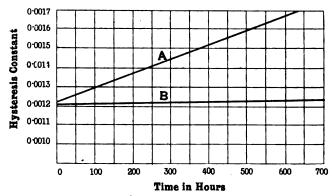


FIG. 250.—Ageing of sheet iron.

A. Annealed iron.

B. Unannealed iron.

the hysteresis loss increased 21 per cent. when an iron core was subjected to a pressure of 100 kilogrammes per square centimetre. Re-annealing after injury by pressure generally restores the iron to its original condition. Owing to this injury under pressure it is advisable in assembling the laminations of an armature core to apply as little pressure as is possible, consistent with good mechanical construction.

Eddy Currents.—Besides the hysteresis loss in the core there is also a loss accompanying the eddy currents which circulate in the core plates. For the brands of iron from which armature laminations are made this loss in watts per kilogramme at o° C. is expressed by the theoretical formula:

$$W_e = 1.65 t^2 B^2 n^2 10^{-11}$$

where-

t =thickness of laminations in centimetres.

B = induction density in lines per square centimetre.

n = number of magnetic cycles per second.

Owing to the increase in the resistance of the core plates, the eddy current loss decreases by about 0.2 per cent. per degree centigrade increase in temperature. Experience shows that the eddy current loss given by the above formula is generally less than that obtained by test by an amount ranging from 50 to 200 per cent. This discrepancy occurs owing to the fact that the formula does not take into account the increased eddy currents set up by (1) neighbouring plates making contact with each other, and (2) solid metal parts being subjected to inductive influences.

During the process of milling and filing the slots, the edges of the laminations are liable to become burred, thus destroying the insulation between them and forming more or less continuous conductors lying parallel to the armature inductors. The strength of the eddy currents will therefore be increased, and consequently the energy required for their maintenance. Armature laminations should therefore be assembled with the minimum of milling and filing.

The solid metal parts liable to have eddy currents induced in them are the armature end flanges and the pole shoes. The end plates and their flanges for supporting the end connections have eddy currents induced in them owing to their cutting the leakage lines of force which enter by the ends of the armature core. The cause of the eddy currents set up in the pole face has already been discussed, and it was pointed out that this loss could be considerably reduced by making the pole shoe laminated.

Owing to the uncertain factors that require to be introduced it will now be evident that any attempts to estimate the armature hysteresis and eddy current loss from the above formulæ must necessarily be very unreliable, so that empirical estimations of these losses are invariably resorted to. It has been found convenient to treat them collectively and refer to them as the Core losses or Iron losses of a machine.

In practice the iron losses are predetermined from the results of tests on previous machines of similar construction, and the results obtained in this manner are much more reliable than those derived from the theoretical formulæ. The curve in Figure 251 shows the relation between the flux density in the core and the corresponding iron loss, the latter being given in watts per kilogramme per cycle. This curve was obtained from a machine tested under normal conditions by the method described on page 462. In estimating the iron losses from the above curve it will be found sufficiently accurate to calculate the total weight of armature laminations, and to assume that the flux density in the teeth is the same as that in the body of the core. The

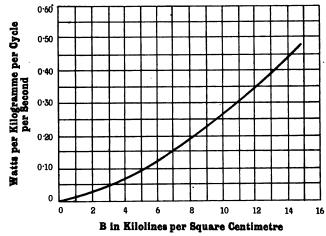


FIG. 251.—Curve of armature iron loss

above curve will be used for estimating the core losses in the following example, but it must be remembered that in practice the curve of iron losses should be experimentally determined for each type of machine.

Example.—The core of the armature referred to in the previous example has the following constants from which the iron losses have to be predetermined:

External diameter of laminations  $(d_1) = 52$  centimetres. Internal diameter of laminations  $(d_2) = 24$  ,, Depth of slot = 2 ,, Width of slot = 0.8 centimetre. Number of slots = 121. Gross length of core = 18.4 centimetres. Number of ventilating ducts = 2.
Width of ventilating ducts = 1 centimetre.
Flux density in core at full load = 10.0 kilolines per square cen-

Magnetic cycles per second = 22.

Area of laminations (including slots) =  $\frac{\pi}{4} (d_1^2 - d_2^2)$ 

$$=\frac{\pi}{4}(52^2-24^2)=1670$$
 square centimetres.

Area occupied by slots =  $2 \times 0.8 \times 121 = 193$  square centimetres.

Area of laminations (excluding slots) = 1670 - 193 = 1480 square centimetres.

Net length of armature core =  $\{18.4 - (2 \times 1)\} \times 0.9$ = 14.8 centimetres.

Volume of iron = 1480 × 14.8 = 22,000 cubic centimetres.

Since I cubic centimetre of sheet iron = 7.8 grammes, the weight of laminations =  $\frac{22,000}{1000} \times 7.8 = 173$  kilogrammes.

From Figure 251, a flux density of 10.0 kilolines per square centimetre entails a loss of 0.265 watt per kilogramme per cycle, so that the iron loss =  $0.265 \times 173 \times 22$  = 1020 watts.

Heating.—The total watts expended in heating the armature will be given by the sum of the C<sup>2</sup>R loss and iron losses, and the rise in temperature of the armature resulting from the generation of heat will be directly proportional to the watts expended in the armature, and inversely proportional to the armature radiating surface. The temperature rise will also be affected by the manner in which the armature is ventilated, and the velocity of the cooling air traversing the internal ventilating channels. The total armature loss can be fairly accurately estimated by the methods discussed above, but the true radiating surface of the armature is an indefinite quantity, as the surfaces of the ventilating channels, and the end connections of the armature coils, all assist in radiating the

heat. It would be rather impracticable to attempt to estimate the total exposed surface of the winding and iron from which radiation can take place, so that the usual practice is to make use of the external cylindrical surface of the armature.

If L denote the overall length of the armature winding, and D the external diameter of the core, the external cylindrical surface =  $\pi DL$ . Having determined the external surface area of the armature the temperature rise may be obtained from the equation,  $T^{\circ}$  = watts lost per unit of armature surface × K, where K is a coefficient the value of which depends upon the internal construction

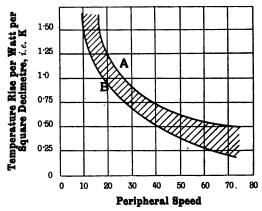


FIG. 252.—Heating coefficient for armatures.

of the armature and its peripheral speed. For well-ventilated armatures of modern design the temperature rise ranges from 1° C. to 1.5° C. per watt per square decimetre for a peripheral speed of about 17 metres per second, and from 0.65° C. to 0.8° C. for a peripheral speed of 35 metres per second. The peripheral speed of turbine-driven dynamos may be as high as 55 to 70 metres per second, so that the temperature rise will be much lower, and ranges from 0.2° C. to 0.5° C. per watt per square decimetre of radiating surface. In the above equation for temperature rise the values of K fall within the shaded area between the two curves A and B in Figure 252, where values of K are plotted as ordinates

and values of peripheral speed as abscissæ. For semienclosed and totally-enclosed motors, the values of K given by the above curve have to be multiplied by 1.5 and 2 respectively.

The value of this heating coefficient K for any particular construction of machine must necessarily depend upon the manner in which the machine is ventilated, therefore the accuracy of the above values of K should be verified by actual tests.

Figure 253 shows the arrangement for ventilating an

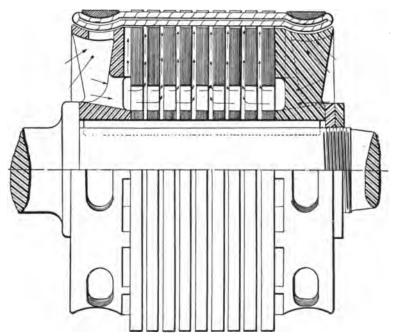


FIG. 253.—High-speed armature showing ventilating arrangements.

armature in which the laminations are mounted direct on the shaft. The core is designed so that cool air may be driven in at each end of the rotating armature and drawn out through the ventilating ducts, the passages along which the air travels being indicated by the arrows. In slow- and medium-speed machines the width of a duct ranges from 1 to 1.5 centimetres, and the distance between them from 5 to 7 centimetres; in such

cases the ratio of the net to gross length of core ranges from 0.7 to 0.8.

Turbine-driven dynamos require to have very liberal ventilation—say I centimetre duct for every 4 centimetres

of iron—for the following reason:

Owing to the small overall dimensions of high-speed dynamos the radiating surface is relatively small, but the total losses are about the same as for a slow-speed machine of the same output, with the result that the watts per unit area are higher. Instead of increasing the dimensions or reducing the losses, which may not be necessary so far as the efficiency is concerned, the heating of the armature is kept within safe limits by providing ample ventilation, as shown in the previous figure.

Example.—If the armature whose losses have been estimated in the two previous examples (namely, pp. 438 and 442) has an overall length of 47 centimetres, and revolves at 660 revolutions per minute, determine the

approximate temperature rise.

Diameter of armature = 52 centimetres.

Area of armature surface =  $\pi \times 52 \times 47 = 7700$  square centimetres = 77 square decimetres.

 $C^2R$  loss = 1340 watts.

Iron loss = 1020 watts.

Total estimated armature loss = 2360 watts.

Watts per square decimetre of armature surface

$$=\frac{2360}{77}=30.$$

Peripheral speed of armature =  $\pi \times 52 \times \frac{660}{60} \times \frac{1}{100}$ 

= 18 metres per second.

From Figure 253, at this peripheral speed and with normal armature ventilation there will be a rise in temperature of 1° per watt per square decimetre of armature surface. The estimated temperature rise  $= 30 \times K = 30 \times I = 30^{\circ} C$ .

Output Coefficient.—From the preceding it will be obvious that the extent of the heating in an armature of given output will depend greatly upon its dimensions. In designing a machine the overall dimensions may be

estimated from previous experience with the same type of machine, but unless this is available an empirical rule must be resorted to for connecting the output of the machine with the length and diameter of the armature core. The empirical rule more frequently used is that first suggested by Professor G. Kapp, and is given by the following equation:

$$\sigma = \frac{W}{D^2 L R'}$$
, where—

W = rated output of machine in watts.

D = diameter of armature in centimetres.

L = gross length of armature core in centimetres.

R = speed in R.P.M.

 $\sigma = a$  coefficient called the output coefficient.

The diameter D is expressed by the formula  $D = \frac{V}{2\pi R}$  where V is the peripheral speed of the armature. A high peripheral speed is somewhat desirable in order to reduce the weight and size of machine for a given output, but it is limited by considerations of mechanical strength depending upon the way in which the armature is constructed. With ordinary slotted armatures the peripheral speed ranges from 16 to 24 metres per second, and 20 metres may be considered an average. Of course it must be remembered that turbine-driven dynamos have as high speeds as 70 metres per second. The value of R being known, and assigning a suitable value to V, the diameter D of the armature core is given by  $D = \frac{V}{2\pi R}$ .

Knowing D, the length of the core is expressed by  $L = \frac{W}{\sigma D^2 R}$ . The value of the output coefficient  $\sigma$  as a function of the armature diameter can be obtained from the curve in Figure 254. These values may be taken as typical of present-day designs, but they are only to be regarded as rough approximations to determine the preliminary dimensions of a machine, the actual dimensions being settled from temperature and commutation considerations.

The tendency in present-day designs is to make the length of the armature small in comparison with the diameter, thus reducing the reactance voltage for a

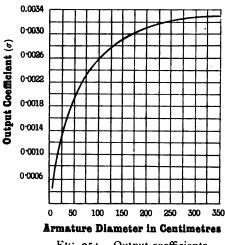


FIG. 254.—Output coefficients.

machine of specified output as explained on page 341. Armatures in which the diameter is great in comparison with the length are known as armatures of the flywheel type.

The heating of an armature is also affected by the current density at which the conductors are worked, and with ordinary ventilated armatures the general

practice is to allow a current density of from 200 to 300 ampères per square centimetre.

## COMMUTATOR

C<sup>2</sup>R Loss.—Recent investigations by Professor Arnold and others have shown that for a given quality of brush, the value of the contact resistance depends upon (1) the brush pressure, (2) the current density at brush surface, and (3) the peripheral speed of the commutator. As stated in a previous chapter, owing to better commutation results and greater durability, carbon brushes are generally employed in machines of recent design, although, for turbine-driven dynamos, metal brushes are frequently employed.

In order to reduce the commutator friction loss to a minimum, the brush pressure should be as light as possible, and a pressure of 100 grammes per square centimetre of bearing surface gives the best results. If the pressure be increased beyond this, the contact resistance is not materially improved, and further, the smoothness of the sliding contact may be distinctly impaired and thereby bad commutation produced. However, in the case of tramway and crane motors the brush pressure may be considerably greater than the value given above, this being necessary on account of the possibility of the brushes vibrating.

With normal brush pressure, the contact resistance of carbon brushes decreases rapidly as the current density increases from zero, but at current densities greater than 6 or 7 ampères per square centimetre the resistance approaches a more or less constant value, so that in machines of large and medium outputs the usual practice is to run carbon brushes at a current density of about 4 ampères per square centimetre. In small machines having good commutation constants the brushes may have a somewhat higher value of current density, the limit being 6 ampères per square centimetre.

The contact resistance varies greatly with different grades of carbon, and may be taken as ranging from 0.2 ohm in brushes of a soft quality to 0.3 ohm in a hard quality. For machines having good commutation properties, brushes of low-contact resistance should be used, so as to reduce the C2R loss and consequently the heating; but for machines having a large sparking voltage, higher contact-resistance brushes should be employed, in order to reduce the tendency to spark. Since the contact resistance varies approximately inversely as the current density, it follows that the resulting drop of potential between the positive and negative brushes of a given quality will be nearly constant at all loads. With the usual current densities and brush pressure, the voltage drop ranges from 1.6 to 2.8 volts, depending upon the grade of carbon from which the brushes are made.

Professor Baily\* has recently made investigations relating to the fall of E.M.F. due to brush-contact resistance, and the results of his tests show that for current densities between 1.5 and 9 ampères per square centimetre and brush pressure of 35 to 207 grammes per square

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<sup>\*</sup> Journal of the Institution of Electrical Engineers, vol. xxxviii. p. 153, February 1907.

centimetre, the drop in E.M.F. between positive and negative brushes is given by

$$E = \frac{(6.5i)^k}{1.0 + 0.7\sqrt{P}},$$

where—

i = current density in ampères per square centimetre.P = brush pressure in grammes per square centimetre.

k = constant ranging in value from 0.28 to 0.5,according to the quality of brush.

The peripheral speed of the commutator also influences the volts drop at the brushes. For machines having carbon brushes the best practice is to limit the peripheral speed to a maximum of 20 metres per second, as with speeds higher than this the brushes have a tendency to vibrate and thereby lower the efficiency of contact.

Brush Friction Loss.—The power wasted due to friction between the brushes and the rotating commutator is expressed by

 $W = 100 \text{ V}\mu\text{PA}$  gramme-centimetres per second, where—

V = peripheral speed in metres per second.  $\mu = coefficient$  of friction.

P = pressure in grammes per square centimetre.

A = total brush contact area.

For carbon brushes in good condition the coefficient of friction may be taken as 0.3, and since I grammecentimetre per second = 981 ergs per second =  $\frac{981}{10^7}$  watts, the brush friction loss is expressed by

$$W = 100 \times V \times 0.3 \times P \times A \times 981 \times 10^{-7}$$
  
= 0.003 \times V \times P \times A watts.

The method of estimating the commutator losses is set forth in the following example; but it should be remembered that if the commutator and brushes are in bad condition, both the electrical and mechanical losses will be considerably increased. There will also

be additional losses due to the waste currents set up by the short-circuiting of adjacent segments and to the loss of energy resulting from sparking at the brushes. At present there is no reliable information regarding the magnitude of these losses, but in practice it is best to allow for them by adding from 15 to 20 per cent. to the sum of the C2R loss and friction loss.

Example.—Estimate the total commutator loss of a dynamo having the following constants:

Full-load current = 60 ampères. Speed of armature = 660 R.P.M.Diameter of commutator = 45 centimetres.

Number of sets of brushes = 4. Number of brushes per set = 3.

Width of each brush = 0.386 centimetre. Length of brush arc = 0.65 centimetre.

Brush pressure = 100 grammes per square centimetre.

# Brushes of Carbon

Contact area per brush =  $0.386 \times 0.65 = 2.5$  square centimetres.

Number of positive or negative brushes =  $3 \times 2 = 6$ . Contact area of positive or negative brushes =  $2.5 \times 6 = 15$  square centimetres.

Current density of brush =  $\frac{60}{15}$  = 4 ampères per square centimetre.

With a current density of this value, and brush pressure of 100 grammes per square centimetre, the resistance of brush contact may be taken as 0.2 ohm per square centimetre of contact area. The contact resistance of positive brush

$$= \frac{0.2}{\text{contact surface}} = \frac{0.2}{15} = 0.0135 \text{ ohm.}$$

This will also be the resistance of the negative brushes,

so that the total brush-contact resistance between positive and negative brushes =  $2 \times 0.0135 = 0.027$  ohm.

 $C^2R$  loss due to brush-contact resistance =  $60^2 \times 0.027$ = 100 watts.

Total area of brush contact at positive and negative brushes  $(A) = 15 \times 2 = 30$  square centimetres.

Brush pressure (P) = 100 grammes per centimetre.

Peripheral speed of commutator (V) =  $\pi \times \frac{45}{100} \times \frac{660}{60} =$ 

15.5 metres per second.

Brush friction  $loss = 0.003 \times 15.5 \times 100 \times 30 = 140$ watts.

Total commutator loss =

(100+140)+20 per cent. to allow for sparking losses, etc. =  $240 \times 1.2 = 290$  watts.

Heating.—The rise in temperature of commutators having peripheral speeds of about 15 metres per second is about 1.2°C. per watt per square decimetre of peripheral radiating surface. In large commutators the inside can be designed so as to permit of it being exposed to air currents, in which case the above temperature rise may be reduced to 1° C. Professor Arnold has investigated this subject, and the results of his experiments show that the temperature rise in ° C. of well-constructed commutators is expressed by

$$T^{\circ} = \frac{300 \times W}{A \times (1 + 0.09 \text{ V})},$$

where-

W = total commutator loss in watts.

A = peripheral radiating surface in square centimetres.

V = peripheral speed in metres per second.

Until recently, the usual practice was to permit the temperature rise of the commutator to exceed by 10° C. or thereabouts that of any other part of the machine. This is undesirable, for owing to the mechanical construction of a commutator successive segments of copper and mica are secured by means of end flanges and bolts

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to the spider, not directly but with an intervening ring of mica. Thus when the commutator is subject to varying temperatures the component parts of the structure do not expand and contract at the same rate, with the result that the commutator deteriorates owing to a rigidly true and concentric cylindrical surface not being maintained. The greater the range of temperature to which the commutator is exposed the more rapidly does deterioration take place, and to obtain a durable commutator the design should be such that the temperature rise does not exceed about 35° C. The usual plan in designing commutators is to make the diameter about 0.75 the armature diameter, and from a knowledge of the estimated losses to assign a length so that there is sufficient radiating surface to keep the temperature rise within the above-mentioned limit.

Example.—If the commutator in the previous example has a length of 10 centimetres, determine the temperature

rise at full load.

Total commutator loss (W) = 290 watts.

Diameter of commutator = 45 centimetres.

Peripheral radiating surface  $(A) = \pi \times 45 \times 10 = 1400$  centimetres.

Peripheral speed (V) = 15.5 metres per second.

Temperature rise in '° C.

$$= \frac{300 \times 290}{1400 \{1 + 0.09 \times 15.5\}} = 26^{\circ} \text{ C}.$$

Reduced Losses with Metal Brushes.—With metal brushes the contact resistance is about one-eighth that of carbon brushes, and the permissible current density can be as high as 30 ampères per square centimetre without excessive heating at the contacts; again, the coefficient of friction is 0.2 as compared with 0.3 for carbon brushes. This means that with metal brushes the area of brush contact need only be 0.12 of that necessary with carbon brushes. There will therefore be a considerable decrease in the commutator loss and a proportional reduction in the size of commutator. In turbine-driven dynamos the commutator assumes very considerable proportions compared with the armature, and the problem of the centri-

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fugal force of the segments is also involved, so that if commutation poles are employed to eliminate commutation difficulties, the substitution of metal brushes for carbon would be a distinct advantage. Again, carbon brushes when used on such high-speed machines are liable to vibrate, and thereby diminish the efficiency of contact and cause undue heating and wear. It would therefore appear that at turbine speeds the limits of carbon brushes have been exceeded, and metal brushes are now often employed. The voltage drop will also be considerably reduced, and the efficiency of the machine increased by an amount ranging from 1 to 2 per cent.

#### FIELD COILS

Excitation Loss.—The excitation loss in a shunt machine is given by  $W_{sh} = C_{sh} \times E$ , where  $C_{sh}$  is the shunt current and E the E.M.F. across the armature terminals. The watts expended in excitation range from 1 per cent. in machines of 1000 k.w. or more to 6 per cent. in machines of less than 10 k.w. If the field magnets be series-wound the watts expended are given by  $W_{se} = C_{se}^2 \times R_{se}$ , where  $C_{se}$  is the current flowing through the series winding and  $R_{se}$  is its resistance. The latter can

be calculated from the formula  $R = \frac{\rho \times l}{a}$ , where l would be the total length of wire forming the series winding and  $\rho$  the specific resistance of copper at the average working temperature, namely, 60° C. In a compound machine the total watts would be given by

$$W = (C_{sh} \times E) + (C_{se}^2 \times R_{se}).$$

Heating.—The rise in temperature of the field coils may be estimated from the formula

$$T^{\circ} = \frac{W}{A} \times K,$$

where-

W = watts absorbed per coil.

A = total radiating surface in square decimetres.

K = the temperature rise per watt per square decimetre.

The value of K will depend upon the depth of the winding, the extent to which the coils are cooled by air currents set up by the revolving armature, the shape of the coils, and the material from which the bobbins (if any) are made. From investigations made by Professor Epstein and E. H. Rayner it has been found that the hottest part of a field-magnet coil is somewhere near the innermost layers of the winding, and that if a coil is fixed upon an iron core and the armature is at rest the former is more effective in conveying away the heat than

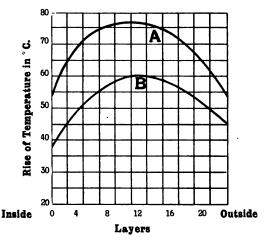


FIG. 255.—Heating curves of a magnet coil.

A. Without iron core.

B. With iron core.

the air which surrounds the outside layers of the winding. But when the armature revolves the fanning action of the latter maintains the outside surface of the coil much cooler than the inner surface next to the core; this is particularly the case with multipolar machines of the fly-wheel type, i.e. machines in which the length is narrow compared with the diameter.

The curves in Figure 255 are the results of tests on a magnet coil, of a 700-k.w. generator of the fly-wheel type, consisting of 22 layers. They show (1) the variation in temperature with the depth of winding, and (2) the effectiveness of an iron core in assisting con-

duction of the heat generated. The temperatures at the different layers of the winding were obtained by means of thermo-electric junctions. In these curves the highest temperature occurs at the middle layer of the coil, and when dismounted from its pole the inside and outside layers are approximately at the same temperature; but when in situ the temperature at the middle layers fell by 15° C., while the temperature at the inside of the coil next the core is considerably lower than that at the outer layers. This demonstrates that the iron is more effective than the air in conducting away heat. When the coil was tested without its pole the average temperature was 70° C., whereas when mounted on the pole it fell to 54° C. The coil was further tested when the machine was running, and the temperature of the outside layer fell to 9° C., while the average temperature was 35° C.

The results of these tests show (1) that the temperature rise is affected by the fanning action of the revolving armature, and (2) that the temperature of the external layers of the coil may be considerably lower than that at the centre layers. Owing to the great difference between the temperature of the surface layers and that at the centre of the coil, the usual practice is to measure the ohmic resistance when hot and when cold, and to compute the average temperature rise from the formula  $R_2 = R_1 \{ 1 + a(t_2 - t_1) \}$ , where  $R_1$  and  $R_2$  are the resistances of the coil at the temperatures  $t_1$  and  $t_2$ respectively. For copper a has a value 0.0043, and the method of calculating the temperature rise is shown in an example on page 20. In ordinary machines the average temperature of the coils, as computed from the increase in resistance, varies between 50 to 100 in excess of the temperature of the outside layers, the temperature being measured by a thermometer. The greater the radial depth of the coil the greater will be the difference between the temperature of the external layers and the temperature at the middle layers. In order to prevent the latter exceeding a safe limit the radial depth of winding should range from 5 to 8 centimetres.

Returning to the value of K in the previous equation, in multipolar machines of modern design an average

temperature rise (i.e. as measured from the increase of resistance) of about 10° C. is obtained per watt per square decimetre of total radiating surface, so that the temperature rise of a field coil is expressed by  $T^{\circ} = \frac{W}{\bar{\Lambda}} \times 10$ .

H. M. Hobart, in his book on dynamo design, states that for an ordinary field coil in which the cooling air passing it is blown from an armature revolving at 17 metres per second, the rise in temperature as measured by a thermometer at the surface layer of the winding ranges from 3° to 4° C. per watt per square decimetre of exposed surface of the coil, i.e. the surface which is exposed to air. The above values of K hold good only for opentype machines, and in the case of semi-enclosed and totally-enclosed motors the temperature rise per square decimetre may reach a value 1.5 and 2 times as great as that given above.

Friction and Windage Loss.—The bearing and windage losses of a machine cannot be pre-determined with any degree of accuracy, so that it is usual to estimate this loss from previous experience with machines of the same type, and to express the loss as a percentage of the output. If the armature and commutator spider be provided with ventilating tunnels the advantage of cooling thereby gained necessarily involves an increased windage loss, thus slightly lowering the efficiency. Experience shows that the bearing friction and windage loss ranges from 0.5 per cent. in machines of about 1000 k.w. to 2 per cent. in machines of 40 or 50 k.w.

## Efficiency

The efficiency of any machine is given by the ratio of power output to power input. In a dynamo the power output is that delivered at the terminals of the machine, and is given by the product of ampères output and the pressure at the dynamo terminals: the power input is that supplied mechanically at the shaft to turn the armature, and as this can also be expressed in watts, the efficiency =  $\frac{\text{watts}}{\text{watts}}$  output input. If W denote the total

output of the dynamo in watts, and w the total loss (also in watts) as estimated in the manner described above, then the efficiency expressed as a percentage is given by

efficiency = 
$$\frac{W}{W+w} \times 100$$
.

The same formula holds good for determining the efficiency of a motor, the output at its pulley being expressed in watts by multiplying the B.H.P. by 746.

The efficiency of a direct-current machine will vary at different loads, and the form of the curve showing the variation of efficiency with output will depend upon the relative values of the various losses. The losses may be divided into two groups—the constant and variable. In a shunt machine the excitation and mechanical losses are constant at all loads, and the core losses may also be considered constant although they increase by a few per cent. at full load, due to distortion of the magnetic field. On the other hand, the C<sup>2</sup>R losses in armature, series winding, and brush-contact resistance are proportional to the square of the current output.

The efficiency of an electric generator or motor is zero at no load, and remains small at low outputs, as the constant losses are then large in comparison with the power output. The efficiency increases with the output in the manner shown in Figure 256, and attains a maximum at that output for which the constant and variable losses are equal, but if the output be further increased the efficiency diminishes.

Let A denote the sum of the constant losses, E the terminal voltage, and C the current output of a dynamo or current input of a motor, as the case may be. It will be assumed that this current is equal to the current flowing in the armature: this assumption is allowable since the shunt current is negligible, compared with the armature current, except in very small machines. Taking the case of a dynamo, the power output =  $C \times E$ , and the variable losses =  $C^2R$ , where R denotes the combined resistance of arma-

ture, series field winding, and brush contact. The efficiency can therefore be denoted by

$$efficiency = \frac{C \times E}{CE + C^2R + A} = X.$$

Assume A to be constant, then differentiating this equation with respect to C and placing the differential coefficient equal to o

$$\frac{dx}{dC} = \frac{EC}{EC + C^2R + A} = \frac{E}{E + CR + \frac{A}{C}}$$

$$= \frac{E\left(R - \frac{A}{C^2}\right)}{\left(E + CR + \frac{A}{C}\right)^2} = \frac{AE - C^2ER}{\left(CE + C^2R + A\right)^2} = 0.$$

$$AE - C^2ER = 0$$

$$AE = C^2ER,$$

$$AE = C^2R$$

The efficiency is a maximum when the sum of the variable losses equals the sum of the constant losses.

when

The efficiency curve of a 250-k.w. 550-volt generator is shown in Figure 256, and may be taken as typical of either shunt- or compound-wound machines. In the same figure is shown the variation of the various losses with the output, and attention is directed to the slight increase in the iron loss caused by distortion of the field, and the increase in the magnetic flux necessary to compensate for the internal CR drop. In designing a dynamo the losses are so proportioned that the maximum efficiency occurs at full load, but it should also be high at three-quarter and even half load. In Figure 257 is given a curve showing the values of efficiency at full load, which may be obtained under ordinary commercial conditions with machines of outputs up to 1000 k.w.

The relation of the variable to the constant losses in a shunt or compound motor will depend upon the conditions under which the motor has to work. If, as is usually the case, the motor is partially loaded during

the greater part of each day, then the constant losses

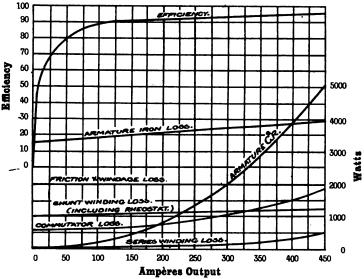


FIG. 256.—Efficiency and losses of a 250-k.w. 550-volt generator.

should be low in comparison with the variable losses. This can be obtained by increasing the number of

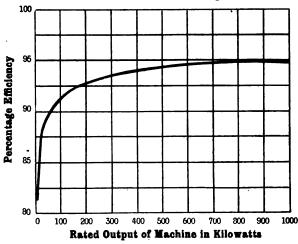


Fig. 257.—Full-load efficiency of machines up to 1000-k.w. output.

armature turns and making a corresponding reduction in the magnetic flux entering the armature, thus increas-

ing the armature C2R loss and decreasing the excitation and iron losses. A motor having a relatively small constant loss will therefore be characterised by having

a high efficiency at all loads, though the fullload efficiency is slightly less than the maximum, as is shown by curve A, Figure 258. When a motor has constantly to carry its full load, then, as with a dynamo, the variable and constant losses should be made equal, so that the maximum efficiency occurs at full load. Figure 258 shows the efficiency curves of two 100-H.P. 500-volt motors.

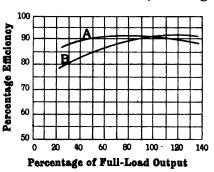


FIG. 258.—Efficiency curves of motors. A. Constant losses, 45 per cent. of full-load variable losses. B. Constant losses, 60 per cent. greater than full-load variable losses.

One motor was designed so that the constant losses were equal to

45 per cent. of the full-load variable losses, and its 90 80 Percentage Mifficiency 70 60 50 40 30 20 10 Percentage of Full-Load Output

FIG. 259.—Efficiency curves of a 30-H.P. series motor.

efficiency was therefore high at all loads, as shown by curve A. In the second motor the constant losses were nearly 60 per cent. greater than the variable losses. that the maximum efficiency occurs at 27 per cent, above the rated output, shown by curve It should be further noted that at light loads the efficiency

of the latter motor is much lower than that of the motor having a low constant loss.

In series motors there are no constant losses, the mechanical losses diminish as the load increases, owing to decrease in the speed, while the C<sup>2</sup>R, excitation, and iron losses increase with the load. A series motor will therefore be characterised by attaining its maximum efficiency at a load considerably less than the rated full-load output. The variation of efficiency with load for a 30-H.P. 500-volt series motor is shown in Figure 259, from which it will be seen that the maximum efficiency occurs at about 50 per cent. of the rated full-load output. Owing to the nature of the work for which series motors are suitable they are invariably subject to extremely varying loads, and it will generally be found that the average load is about 50 per cent. of the rated full-load output, so that a high efficiency at half load is highly desirable.

#### TESTING OF DIRECT-CURRENT MACHINERY

In the preceding part of this chapter the method of predetermining the losses and efficiency of direct-current machines has been examined. It will now be of advantage to consider a few of the more important commercial tests to which complete machines are subjected for determining their actual losses and efficiency.

Core Loss Test.—The machine D to be tested is direct coupled to a suitable motor, and the watts input to this motor are measured for various flux densities in the armature core of D. To obtain the best results the size of the driving motor should be from 10 to 15 per cent. of the total output of the machine being tested. The input to the motor, when D is unexcited, is consumed in the friction and windage losses of the two machines, and the core losses in the driving motor; while the input when D is excited also includes the iron losses in its armature core which correspond to the particular flux density at which the input is measured. Thus to determine the iron losses of D the other losses for each input reading must be known.

In performing this test various precautions require to be taken. To avoid including the volts drop due to brush-contact resistance at the commutator of the motor, the armature voltage should be read direct from the commutator segments instead of across the terminals. This condition is fulfilled by insulating one brush in each of the positive and negative sets from the brush spindle and connecting the voltmeter across them. By this means the actual voltage on the commutator is measured independently of any CR drop due to brush-contact resistance.

The iron losses would be measured for a particular speed, so that the friction and windage losses of the set remain constant. The iron losses of the motor, being unknown, must also be kept constant, so that they can be eliminated in the final calculation. To meet this requirement both the speed and exciting current of the motor must be kept constant. Thus it is necessary to separately excite the field of the motor and control the speed by the voltage supplied to the armature; this can be performed most conveniently by driving an auxiliary dynamo to supply power, and regulating its field or speed.

In performing this test the brushes of machine D should be raised, as otherwise currents flow in the brush

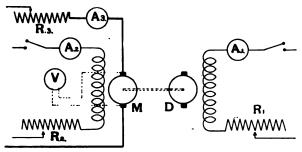


Fig. 260.—Diagram of connections for core loss test.

faces when the machine is excited. It is necessary, therefore, to take a characteristic curve of the machine D on open circuit for the speed at which the core loss is to be taken, so that the armature voltage and flux can be determined from the strength of the field current. The field of D will, of course, be separately excited. The diagram of connections is as shown in Figure 260.

The field coils of the machine to be tested are con-

nected to a source of E.M.F. through a regulating resistance  $R_1$ , ammeter  $A_1$ , and a switch. The field of the driving motor is similarly connected through  $R_2$ ,  $A_2$ , and a switch. The armature of the motor is connected through a starting resistance  $R_3$  to an auxiliary dynamo whose voltage can be controlled. The ammeter  $A_3$  and voltmeter V indicate respectively the current input to, and pressure of, the armature of the motor M.

During the test the current supplied to M and its voltage should be observed for about ten values of exciting current in machine D taken from zero to about 25 per cent. above that corresponding to the normal voltage of D. These results should be tabulated as follows:

← Driving Motor → Machine D →							
Armature Volts.	Armature Current.	Field Ampères.	Armature Volts from characteristic.				

Knowing the resistance R of the motor armature, the core losses may be calculated from the above data and tabulated as below.

← Driving Motor →						← Machine D →		
		Arma- ture C <sup>2</sup> R.	Input Watts C.E.	CE-C <sup>2</sup> R.	Core Loss in Watts	Armature Volts.	Field Current.	
——				·				
						,		
1			 					
		Input.	Input. Arma-	Input. Arma- Input ture Watts	Input. Arma- Input ture Watts CE-C2R.	Input. Arma- Input ture Watts CE-C2R. Core Loss in	Input. Arma- Input ture Watts CE-C2R. Core Loss Armature Volts.	

C and E are the ampères input and voltage respectively of the motor, and  $C^2R$  the corresponding copper loss in the motor armature for each value of C. CE is the total input in watts, and  $CE - C^2R$  gives for each observation the sum of the iron losses in D, the constant losses in the iron of the motor, and the friction and

windage of the set. The reading taken with D unexcited is called the friction reading; thus if the value of  $CE - C^2R$  for the friction reading be subtracted from the value of  $CE - C^2R$  when the field is excited the result in each case gives the iron loss of D for that field excitation. The frequency of reversal of flux, as given by  $\frac{Rp}{60}$ , will remain constant.

A curve should be plotted with armature volts as abscissæ and core loss in watts as ordinates. For design purposes the usual practice is to plot watts lost per kilogramme of iron, at some definite frequency, as ordinates, and the corresponding flux density B in the armature core as abscissæ. Such a curve is shown in Figure 251, page 442. The weight of armature iron can be calculated if its volume be known. The total flux M entering the armature per pole may be computed from the equation  $E = 4T.N.M.10^{-8}$ , T being the number of turns per circuit through the armature. The flux density in the armature core is given by  $B = \frac{M}{A}$ , where A =area of cross-section of armature iron.

Efficiency Tests.—1. By Prony Brake.—The prony brake is an absorption dynamometer, and is used largely

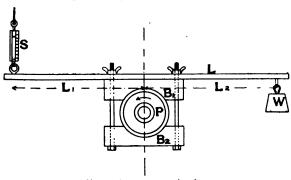


Fig. 261.—Prony brake.

for testing the efficiency of motors up to about 15 H.P. It consists of two wood blocks B<sub>1</sub> and B<sub>2</sub>, which are clamped to a pulley P keyed to the motor shaft as shown in Figure 261, so that the friction between the blocks

and the pulley can be easily adjusted to any required extent. To B<sub>1</sub> is fixed a lever L, the lengths of the arms L<sub>1</sub> and L<sub>2</sub> being made equal. The unknown turning effort exerted by the motor is balanced by weights W attached at the end of one arm to take up the bulk of the pull, and a spring balance S at the end of the other to facilitate fine adjustments, and for the purpose of maintaining the lever horizontal. The friction is adjusted to the required value by tightening the nuts. Ampères input, voltage, and speed are then observed. While the speed is being taken the clamps must be adjusted and due attention paid to lubrication to keep the friction value constant. Readings may be taken for any load up to about 25 per cent. overload by attaching suitable weights.

The power input to the motor =  $W_1 = E \times C$  watts =  $\frac{E \times C}{746}$  H.P.

To determine the B.H.P. of the motor, let-

L = length, in metres, of lever from centre of pulley to point of attachment of W, *i.e.* distance L<sub>1</sub>. l = radius of pulley in metres.

P = Weight + spring balance pull in kilogrammes.

p = turning effort in kilogrammes at surface of pulley.

N = speed in revolutions per second.

The Power output at pulley of motor =

 $W_2 = 2\pi N l \times p$  kilogramme-metres per second.

When the lever is horizontal

$$L \times P = l \times p$$

so that  $W_2 = 2\pi N L \times P$  kilogramme-metres per second  $= \frac{2\pi N L \times P}{76} \text{ H.P.}$ 

The efficiency of the motor at any particular load is therefore

$$\frac{W_2}{W_1} = \frac{2\pi NLP \times 746}{EC \times 76} = \frac{62 \times NLP}{EC}.$$

2. By Hopkinson's Method.—When testing machines by the prony brake the entire output is absorbed

without doing useful work, and if large units were tested in this manner the energy wasted would render the test a very expensive one. The late Dr. John Hopkinson suggested the testing of machines in pairs, one running as a motor, driving the other as a generator, the current from the latter being returned to the source of supply. By this means a considerable saving in power is effected, since only sufficient power is required to supply the losses of the two machines. In the original Hopkinson test the power was supplied mechanically, but its measurement was rather difficult to obtain. A modifica-

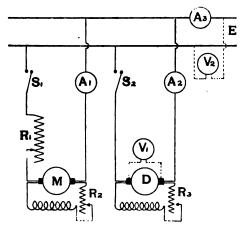


FIG. 262.—Diagram of connections for Hopkinson's test.

tion has since been devised by Professor Kapp whereby the power is supplied electrically.

The machines to be tested should be similar both mechanically and electrically, and coupled either direct

or by means of a belt.

The diagram of connections for testing by this method is as shown in Figure 262. M and D are the machines to be tested, and it will be supposed that M is the motor and D the generator. The power is taken from the supply mains E, between which there is maintained an E.M.F. equal to the normal E.M.F. of M and D. The motor M is connected to the supply through a starting resistance R<sub>1</sub>, ammeter A<sub>1</sub>, and switch S<sub>1</sub>. D is connected to E through a switch S<sub>2</sub> and ammeter A<sub>2</sub>, care being taken to observe that the positive and negative terminals of D are connected to the leads of M of similar polarity. In series with the field coils of M and D are connected the regulating resistances R<sub>2</sub> and R<sub>3</sub> respectively.

The method of performing the test is as follows. Machine M is started up as a motor, and its speed adjusted to normal by R<sub>2</sub>. The second machine D is then excited to the same voltage as the supply by adjusting R<sub>3</sub>. When the readings of voltmeters V<sub>1</sub> and V<sub>2</sub> coincide the switch S<sub>2</sub> is closed, thus connecting D in parallel with the supply. By adjustment of R<sub>3</sub> the excitation of D can be increased, and so permit it to supply current; this will consequently increase the load on the motor. By means of R<sub>2</sub> and R<sub>3</sub> it should be possible to increase the load on the machines up to about 25 per cent. overload. The ammeter A<sub>3</sub> measures the current taken from the supply mains, and the sum of the readings on A<sub>2</sub> and A<sub>3</sub> should equal the current input to the motor, *i.e.* the reading on A<sub>1</sub>.

Let the current taken by the motor from the supply E and generator D be denoted by  $C_3$  and  $C_2$  respectively, and the pressure by E, then the power absorbed by  $M = E(C_2+C_3)$  watts. Since the two machines are nearly equally loaded it may be assumed that their efficiencies for any particular value of  $(C_2+C_3)$  are equal. This is not strictly so, as the motor will be loaded to a greater extent than the generator, and the excitation of D will be greater than that of M. Let e denote the efficiency of each machine, then the output of the motor  $e \times E(C_2+C_3)$ ; but this also represents the mechanical power supplied to the generator, so that the output of the generator  $e \times e E(C_2+C_3) = e^2 E(C_2+C_3)$ . The output of D is also expressed by  $E \times C_2$ , so that

$$e^2 \operatorname{E}(C_2 + C_3) = \operatorname{E} \times C_2$$
, *i.e.* the efficiency  
=  $e = \sqrt{\frac{\operatorname{E} C_2}{\operatorname{E}(C_2 + C_3)}} = \sqrt{\frac{C_2}{C_2 + C_3}}$ .

The current C<sub>2</sub> supplied by the generator is not wasted but flows into the motor, helping to drive the

latter; it is therefore known as the "circulating current." Where two machines of the same size and type have to be tested this is the method invariably adopted both for efficiency tests and those to determine the maximum temperature rise.

- 3. By measuring the Losses separately.—The losses in any electrical machine may be divided into
  - 1. Copper losses (W<sub>1</sub>).
  - 2. Excitation losses (W<sub>2</sub>).
  - 3. Core, friction, and windage losses (W<sub>3</sub>).

By this method the losses are measured separately, and the efficiency computed from the known output of the machine. Let C denote the current output and E the terminal pressure; then the power output =  $C \times E$  watts, and the power input =  $C \times E + losses = C \times E + (W_1+W_2+W_3)$ . The efficiency would therefore

$$=\frac{CE}{CE+(W_1+W_2+W_3)}$$

The individual losses may be determined as follows: Copper Loss.—Let R<sub>a</sub> denote the resistance of the armature winding, brushes, and brush leads, then the copper loss is expressed by

$$W_1 = C^2 R_{\alpha}$$
.

R<sub>a</sub> may be measured by sending a known current through the armature and observing the fall of potential.

Excitation Loss.—If  $C_{sh}$  denote the shunt current to produce normal excitation, and E the total E.M.F. across the shunt winding and its rheostat, then the loss in the shunt coils =  $C_{sh} \times E$  watts. If there be a series winding of resistance  $R_{se}$ , the watts lost in it =  $C^2R_{se}$ .

The total excitation loss would therefore be expressed by

$$W_2 = C_{sh}E + C^2R_{se}$$

Core, Friction, and Windage Loss.—These losses are often referred to as the "stray power" losses, and for a uniform speed they remain approximately constant at all loads; though, as has already been stated, the core losses

increase by a few per cent. with the load due to the effects of armature reaction. To determine these losses, the machine is run as a motor at no load with normal excitation of the field. If  $C_1$  denote the current input and E the E.M.F. impressed on the armature the stray power loss is expressed by

$$W_3 = C_1 E - C_1^2 R_a$$

where  $C_1^2 R_a$  is the copper loss in the armature occurring at the particular current.

This method of determining the efficiency of generators and large motors is invariably adopted when two machines of similar design are not available for determining the efficiency by the Hopkinson method.

## CHAPTER XIII

#### ELECTRICITY CONTROL

In this chapter the general principles governing the grouping of electric machines will be examined, together with the apparatus required for controlling the output and pressure of supply from direct-current generating stations. The output is controlled from a switchboard which contains the necessary switches, protective devices, measuring instruments, rheostats, etc. Before proceeding further it will be as well to look into the construction and design of such of these as have not already been described.

#### SWITCHES.

Knife Switches. — A switch is a device introduced into a circuit by which its continuity may be established or interrupted as required. Switches for direct-current circuits may be divided broadly into two types—(1) slow break, and (2) quick break.

A slow-break switch is simply a hinged link fitted with a handle, and is not intended to be relied upon for opening a circuit in which current is flowing, though it is commonly used to accomplish the final step in completing a circuit. These switches should only be connected in circuits provided with "circuit breakers," which can be operated either automatically or "tripped" by hand. For example, suppose the positive terminal of the dynamo D (Figure 263) be connected to the positive bus-bar through a circuit breaker B, and the negative terminal by way of the switch S to the negative bus-bar. If it be necessary to disconnect the dynamo when supplying current, the circuit is broken by opening the

circuit breaker, after which the switch S is simply used to complete the isolation of the dynamo from the switchboard.

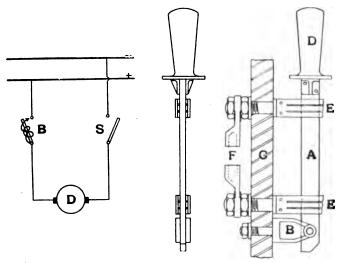


FIG. 263.

FIG. 264.—S.P. Slow-break switch.

Figure 264 illustrates the construction of a slow-break switch. The parts which carry current are made of hard-drawn copper. The link or blade A is of rectangular cross-section, and hinged to the gun-metal block B. The latter is cast with a shank by means of which it can be bolted to an insulating base. The switch is operated by means of an insulated handle D. On closing the switch the circuit is completed by the linking up of the contacts E. The latter consist usually of copper strip bolted to the insulating base, and are saw cut in order to make them as flexible as possible, thus ensuring an efficient contact. The bolt or shank of the contacts is made long enough to support the cable sockets F.

Quick-break switches are used to interrupt a circuit when carrying current. Before such a circuit can actually be broken the switch must be withdrawn from its contact clip to such a distance that the E.M.F. can no longer cause the current to bridge the gap. During the process of withdrawing the switch the intense heat

of the arc formed is, of course, fusing the metal blade and contact clip of the switch. It therefore appears to be a matter of the utmost expediency to reduce the duration of this fusing to the minimum possible period, *i.e.* the interruption must be performed quickly; hence the employment of "quick-break" switches.

The construction of a double-pole quick-break switch is shown in Figure 265. To the main blade A is attached an auxiliary blade B. The two blades are connected at the top by a stiff spring C, and at D the auxiliary is hinged to A. On closing the switch they act as one blade, but on opening the friction of the contacts retains

the part B until the tension of the spring is sufficient to overcome the friction of the contact, when it is pulled off so quickly that any appreciable arc is avoided.

It will be observed that in this type of switch the hinges of the main blades are also

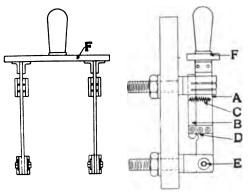


FIG. 265.—D.P. Quick-break switch.

electrical contacts. These contacts are ground in, and, in order to obtain sufficient area of contact with the blade, washers E of comparatively large diameter are placed between the contacts and the bolt heads or nuts. At one time such contacts were very imperfect, but hinge contacts, which are well ground in, now afford a better electrical connection than that formed by clip contacts.

Double- and triple-pole (often denoted by D.P. and T.P. respectively) switches are formed by coupling together by an insulating cross-bar F (Figure 265) the requisite multiples of single-pole switches.

Knife switches should be designed so that the normal current density of the blades is about 150 ampères per square centimetre, and the surface density

at contacts 20 ampères per square centimetre. In switches for pressures up to 500 volts the distance between the centres of contacts ranges from 8 centimetres in 50-ampère switches to 20 centimetres in 1600-ampère switches.

Plug-bar Connector.—Screw plug switches, of the type shown in Figure 266, are used on switchboards for connecting bars on the front to others mounted at the back, the plug passing through the panel. For instance, suppose the feeder F be connected to the bar D on the front of the board, and that there are two bus-bars B<sub>1</sub>

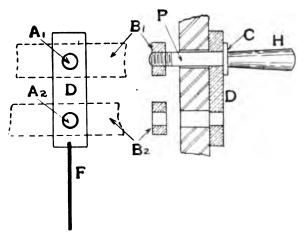


FIG. 266.—Plug-bar connector.

and  $B_2$  mounted on the back; F may be connected to either of these bars by inserting the plug P at  $A_1$  or  $A_2$  respectively. The bar D and plug P are usually made of copper or gun-metal. P is fixed to an insulating handle H, and is provided with a turned collar C, which bears against the face of the bar D, while contact is made with  $B_1$  or  $B_2$  by screwing the plug into either of them as shown.

Field Switches.—The field-magnet coils of a directcurrent generator are highly inductive, so that the sudden breaking of such a circuit when carrying current causes an e.m.f. many times greater than the normal working pressure to be induced across the terminals of the machine due to the collapse of the lines of force. This self-induced e.m.f. produces a persistent arc at the points of interruption, and may attain to such a value as to break down the insulation of the field-magnet coils. In most direct-current generators there is no necessity to break the field circuit at all, and in such cases it is better to eliminate such switches altogether. When, however, field switches must be used they should be so constructed that when the field coils are disconnected from their source of E.M.F. the magnetic flux is made to decrease

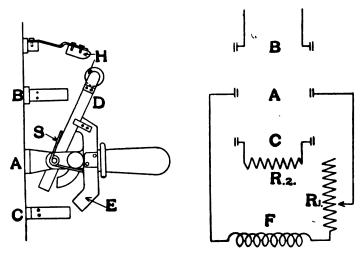


FIG. 267.—Field-break switch.

slowly to zero, and thereby prevent the induction of an abnormal e.m.f.

The principle and construction of one form of field-break switch is shown in Figure 267. The field coils F are connected in series with a rheostat R<sub>1</sub> across the common contacts A of a double-pole throw-over switch. The contacts B of the latter are connected to a source of E.M.F., and between those marked C is connected a non-inductive resistance R<sub>2</sub> having a value approximately equal to that of the shunt coils. To each main blade D of the switch is rigidly fixed an auxiliary blade E. When the switch is thrown over to B the field coils are connected to the source of E.M.F. On breaking the

field circuit a spring S is put into tension, and before the main blades leave the contacts B the auxiliary blades E make contact with C, thus putting the resistance R<sub>2</sub> across the field coils before the exciting circuit is broken.

When the supply circuit is disconnected the field flux begins to decrease, but this sets up a counter e.m.f. which opposes the decrease in the field current, with the result that the field subsides slowly and thereby prevents an abnormal rise in pressure. Even with this arrangement there will be some arcing when the supply circuit is disconnected, and to prevent damage to the switch parts the supply circuit is finally broken at carbon faced contacts H.

Voltmeter Switches and Plugs.—When a number of

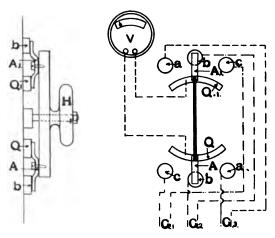


FIG. 268.—Voltmeter switch.

dynamos are operated in parallel one voltmeter is sufficient to serve all the generators, and by means of a multiple-way switch the voltmeter may be connected to any dynamo. The arrangement is shown in Figure 268. There are in this case three pairs of contact studs marked aa, bb, and cc, connected to three generators, as indicated at  $G_1$ ,  $G_2$ , and  $G_3$  respectively. Fixed to an insulated handle H are two contact strips A and  $G_1$ . The latter bear on the metal quadrants Q and  $G_1$  respectively, across which is connected the voltmeter V.

When the switch contacts are moved to bb the voltmeter is connected across generator  $G_2$ ; similarly  $G_3$  and  $G_1$  may be connected by moving the switch to the positions aa or cc respectively. A drawing is also shown of the switch to illustrate its construction.

Another method of using one voltmeter for a number of generators is by means of plugs and receptacles. The arrangement is shown in Figure 269. Each generator panel is fitted with four metal receptacles or sockets A. The lower pair of each set are connected to the generator terminals indicated at  $G_1$  and  $G_2$ , and the top pair are

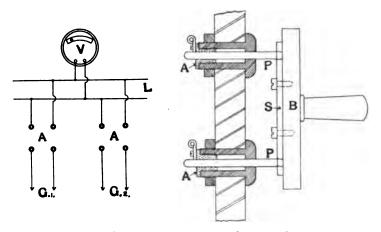


FIG. 269.—Voltmeter plugs and receptacles.

joined to the voltmeter leads L, which run along the entire length of the generator panels. The terminals of the voltmeter V are connected to these leads. For connecting the voltmeter to any one generator a four-pronged metal plug is inserted into the receptacles. The prongs P are connected in pairs by insulated metal strips S, fixed to the underside of an insulating base B, to which a handle is attached, in such a manner that receptacles in the same vertical plane are connected together. The sectional drawing illustrates the construction of the removable plugs and the method of fixing the receptacles to the switch-board.

Multiple-way Regulating Switch.—Figure 270 shows the construction of a multiple-way switch suitable for a field-regulating rheostat. The switch consists of a laminated copper brush A fixed to, but insulated from, a metal arm B pivoted at C. The brush A can be moved through an angle of about 300°. One end passes over the contact studs D arranged in circular formation, and the other end slides over but remains in contact

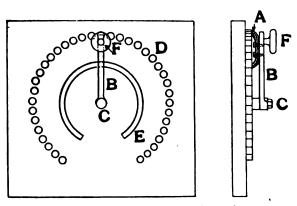


FIG. 270.—Multiple-way regulating switch.

with the circular contact E. The studs and circular contact are fixed to an insulating base in a similar manner to those for a motor starting switch shown in Figure 237. Resistance coils are connected between the several studs. It will be seen that any resistance from zero to the sum of the whole of the several individual sections may be introduced by varying the position of the arm B, which is provided with a suitable insulated handle F for manipulation.

# Cut-outs

It is necessary in an electric circuit to provide means for protecting the apparatus comprising it from possible injury when abnormal conditions arise. The devices used to effect such protection are known as "cut-outs."

The essentials of a cut-out are—

(1) Automatic quick and reliable action.

(2) Inability to maintain the arc incident to the

interruption of the current.

Cut-outs are of two distinct classes: (1) those in which a link of metal is heated to fusion, and (2) those which are actuated by an electro-magnet. The former or "thermal cut-outs" are commonly known as fuses, and the electro-magnetic class as "circuit breakers."

#### Fuses

The metals of which fuses are now made are tin,

lead, copper, or aluminium.

Tin and Lead. — In the early forms of fuses, wires of tin, lead, or tin and lead alloy were invariably used, as they melted at a low temperature and were therefore considered to be less dangerous from a fire risk point of view than other metals having a higher temperature of fusion; but tin and lead have a very low conductivity in comparison with the other metals named, so that a much greater mass is required to carry normal current. The arc formed at fusion, too, is much more persistent with these metals than with copper or aluminium; so much so that fuse fittings which will stand direct short circuits with the latter materials are liable to destruction if used for tin or lead fuses. This is probably due to the greater mass of metal disrupted. At fusion a proportion of the products are deposited on adjoining cold surfaces; these deposits are often difficult to remove, and if allowed to remain facilitate the maintenance of subsequent arcs.

The fusing current of tin and lead wires, particularly when of small diameter, is considerably affected by the action of the atmosphere. When the wire becomes heated a layer or skin of oxide is formed of sufficient thickness and strength to hold up the metallic core of the wire when in a molten condition, so that the fusing current is abnormal. Again, tin and lead become exceedingly brittle at a temperature slightly below that of fusion, so that when subject to vibration the fusing current of a wire in this state is appreciably lowered.

Copper.—Tinned copper appears to be the most

reliable material to use for fuses. It is mechanically strong, and the mass required to carry a given current is comparatively small. A copper fuse does not oxidise appreciably when carrying 50 per cent. of its normal fusing current, but for currents higher than 60 per cent. the deterioration due to oxidation has a marked effect on the ultimate fusing current. Copper attains a red heat with about 75 per cent. of its normal fusing current, and when the current is increased beyond this the deterioration is very rapid. This severe oxidation at high currents will cause the fuse to act prematurely if it be permitted to carry continuously 80 per cent. or more of its normal fusing current. When a copper fuse is disrupted the greater part of the metal is scattered, only a small quantity being volatilised. Unless guarded, the molten particles may on a dead short circuit be scattered as much as from 3 to 6 metres.

Aluminium.—This metal possesses valuable non-arcing properties, but when exposed to the atmosphere a skin of oxide is, as in the cases of tin and lead, formed which is particularly tough and has a marked effect upon the ultimate fusing current. Aluminium attains to a dull red heat just before fusion, and when ruptured particles are scattered for a distance of from 2 to 3 metres. This metal is highly electro-positive to copper or brass, and in the presence of moisture the contact difference of potential is likely to set up corrosion at terminals. Fuses of aluminium are therefore unsuitable for use in damp situations.

Fusing Current of a Wire.—The current required to fuse a wire of circular cross-section and of a given material is dependent upon (1) diameter, (2) length of wire employed, and (3) the environment and position of fuse. The curves in Figure 271 show the relation between diameter and fusing current for copper, tin, and aluminium wires for a given length. The variation, with the length between the terminals, of the fusing current of a No. 25 S.W.G. tin wire is shown in Figure 272. For lengths between the points A and B the value of the fusing current is high, due to radiation from the comparatively large surfaces of the terminals. As the fuse is

lengthened the heat from the central portions is not thus dissipated, and the fusing current is appreciably reduced.

The less the length of wire the greater will be the influence of the terminals, but wire mav selected of a sufficient length to be independent of the cooling effect of the terminals, as is shown by the approaching the axis of abscissæ asymtotically.

The fusing current of a wire is also affected by its position and the nature

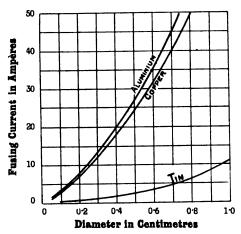


FIG. 271.—Relation between fusing current and diameter of wire.

of the terminals. The effect of a fuse being in a horizontal position instead of in a vertical one is to increase the fusing current by about 6 per cent. in wires

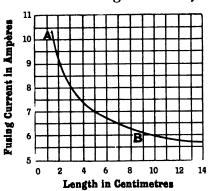


FIG. 272.—Relation between fusing current and length of wire for No. 25 S.W.G. tin.

of 40 to 37 S.W.G. and 4 per cent. in wires of larger gauge. The more massive the terminals the greater will be their effect in dissipating the heat, but for wires having lengths of 5 centimetres and upwards the effect of the terminals may be neglected.

From the curves in Figure 271 connecting the fusing current with diameter of wire it will be

observed that the curve is not a linear function, so that the fusing current is expressed by an equation of the order

where d is the diameter of wire in centimetres. The

values of A and n for different materials under various conditions have been investigated by Professor Schwartz and W. H. James,\* and are set forth in Table XVI., the values holding good for wire clamped in such a manner that it is free in air from terminal to terminal.

# TABLE XVI FUSING CONSTANTS

Particulars of Fuse.	Range on S.W.G.	Range of Fusing Currents.	Index n.	Con- stant A.
TINNED COPPER—				1
Lengths of 5 centimetres and upwards, Horizontal Lengths of 15 centimetres	47 to 33	I to IO	1.195	821
and upwards, Horizontal . Lengths of 5 centimetres and	33 to 18	10 to 100	1.403	1768
upwards, Vertical .  Lengths of 15 centimetres	47 to 33	1 to 10	1.195	775
and upwards, Vertical .  Lengths of 10 centimetres,	33 to 18	10 to 100	1.403	1680
Horizontal with large ter- minals Lengths of 10 centimetres,	33 to 18	10 to 100	1.586	2980
Vertical with large ter- minals	33 to 18	10 to 100	1.586	2844
TIN— Lengths of 8 centimetres and				1
upwards, Horizontal.  Lengths of 15 centimetres	43 to 20	1 to 10	1.131	146
and upwards, Horizontal.	20 to 7	10 to 80	1.32	239
ALUMINIUM— Lengths of 10 centimetres				
and upwards, Horizontal.	42 to 22	3 to 45	1.461	2188

Fuses for circuits carrying 200 ampères or more are often made from sheet metal, as less material is necessary owing to the relatively greater radiating surface. The fusing current C is a function of the breadth b and the thickness t, and with lengths of 13 centimetres or more

<sup>\*</sup> Journal of the Institution of Electrical Engineers, vol. xxxv. p. 416 (1905).

the above-mentioned investigators have shown that the fusing current for lead, copper, and aluminium may be calculated from the following expressions:

Lead  $C = 407 t^{.74} (b+0.04)$ , Copper C = 6280 b (t+0.009), Aluminium C = 15000 (b+0.09) (t+0.006), b and t being expressed in centimetres.

These equations hold good for fuse strips in a horizontal position, but the fusing current is reduced by about 10 per cent. when the strips are placed vertically.

Overload Capacity.—From the foregoing it will be apparent that there may be an indefinite number of fusing currents for any particular wire. The "normal fusing current" of a wire may be defined as the minimum current required to fuse the wire in such a time interval as shall be necessary for the wire to have attained its maximum steady temperature. The "normal carrying capacity" or "rating" of a fuse wire may be defined as the maximum current which the fuse is capable of carrying continuously without deterioration or undue heating. Since the function of a fuse is to protect the whole of the circuit with which it is in series, its fusing current must be such that the safe overload capacity of any individual conductor or piece of apparatus forming the circuit is not exceeded. In general the capacity of a circuit for overload is considerably in excess of the overload capacity of the fuse which protects it.

The fuses protecting motor, generator, or feeder circuits should be selected for 100 per cent. over the normal working full-load current, i.e. a fuse protecting a circuit taking 100 ampères at normal full load should be designed to operate when the current increases to 200 ampères. The fuses will then be able to stand any momentary rise in current likely to occur, and also to protect the component parts of the circuit from overheating. Of course, in certain circuits the apparatus to be protected might be such that the overload capacity of the fuse must not exceed 20 to 30 per cent. of its normal rating. Now it has been shown that if the normal full-load current of a fuse be greater than 50 per cent. of the

normal fusing current, a fuse of copper rapidly deteriorates and so becomes unreliable, so that circuits, in which the fusing current is less than 100 per cent. of the normal current, must be protected with fuses other than of

copper.

Since the rise in temperature to the point of fusion is an integrated effect, the rupturing of a fuse is not instantaneous. Figure 273 shows the relation between the percentage excess over the normal fusing current and the time taken to fuse the wire from a cold state for (1) copper, (2) aluminium, and (3) tin, the normal fusing

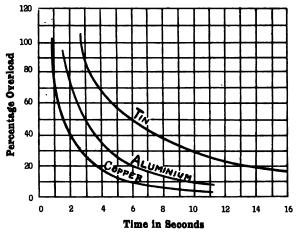


FIG. 273.—Variation in time of fusion with current.

current of each wire being about the same, namely, to ampères. It will be seen that the time of fusion decreases as the current is increased, and that tin is the most sluggish while copper is the quickest in action. As the current is reduced the curves approach the axis of abscissæ asymtotically and the ordinate of the point at which the curve becomes practically horizontal is the value of the current which the fuse will carry continuous without rupture. In the case of a "short circuit" a fuse operates at a much higher current than would be the case if the overload were applied gradually. This is due to the short-circuited current being applied instantaneously; thus when the normal fusing current is reached the fuse

has not had sufficient time to attain its steady temperature corresponding to that current. Again, a fuse melting with the normal fusing current exhibits a greater tendency to arc than when melting with a current three or four times in excess of the normal fusing current. due to the fact that with a small overload the wire will fuse first over a short length at its centre, and an arc will be formed across this small gap. The length of the gap will increase as the ends of the wire are burned back, until the arc finally fails. With a large overload the heating of the entire wire is so rapid that fusion takes place along its entire length, and the wire is completely disrupted from terminal to terminal.

Fusing Current and Length of Break.—The length of break or distance between the terminals of a fuse should be increased with its normal carrying capacity for the following reason. When the rupture of a fuse takes place there will be a self-induced e.m.f. set up in the circuit due to the sudden cessation of current. inductive e.m.f. will be dependent upon the strength of the current at the time of fusion and the time in which the circuit is broken. The inductive pressure rise will largely influence the formation of an arc, so that the length of break must therefore be increased when large currents are to be broken on the fuse.

With fuses for 100 to 250 volt circuits the distance between the terminals of a fuse usually ranges from 7 centimetres with 50-ampère fuses to 11 centimetres with 500-ampère fuses. Again, for 600-volt circuits, and between the same limits of current, the length of fuse ranges from 9 to 15 centimetres. The normal fusing current of a wire should preferably not exceed 100 ampères, and fuses for larger currents should be of strip form or made up of several wires in parallel spaced about 1 centimetre apart.

Construction of Fuse-holders.—As already stated, the melting of a fuse is always accompanied by an electric arc which produces a quantity of hot vapour, the sudden expansion of which tends to scatter the melted metal. Again, it is very desirable that fuses should be easily removable for inspection and renewal, and be capable of being quickly replaced on a live circuit without risk of shock to the operator. These considerations necessitate the fuse being placed in a receptacle forming a removable holder of insulating and incombustible material.

Figure 274 illustrates a typical fuse-holder suitable for direct-current circuits up to 600 volts. It consists of a hollow porcelain carrier A of such a design that it can

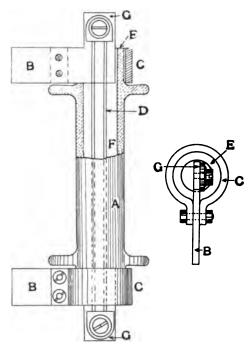


FIG. 274.—Fuse-holder.

be easily handled. The blades B are bolted to the copper bands C, which in turn are clamped to the extremities of the carrier. The fuse D, of either wire strip, or placed in the tube of the holder and clamped to the lugs G, which are one with the blades В. latter fit into contacts which may be of similar design to those shown at E for the switch illustrated in Figure The intense 264. heat generated at the instant of fusion

causes a rapid expansion of air, which escapes at the ends of the tube, and in doing so blows out the arc.

At one time fuse wires were clamped direct to their terminals, but such fuses were liable to be mechanically damaged when being inserted, thus affecting the value of the fusing current. The best practice, and that now invariably adopted for switchboard work, is to solder the ends of the wire to copper blocks B suitably shaped as shown in Figure 275. The blocks supporting the fuse wires W are connected to the lugs G carried by the

blades B (Fig. 274). In enclosing fuse wires in porcelain tubes, precautions should be taken to keep them

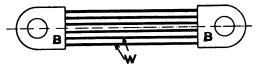


FIG. 275.—Method of fixing fuse wire to blocks.

clear of the porcelain, as this would assist in cooling the wire and thereby increase the fusing current.

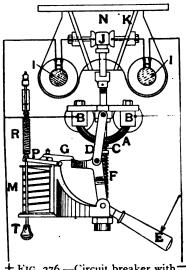
#### CIRCUIT BREAKERS

Excess Current Circuit Breakers.—For central station and heavy-current work generally the fuse has been displaced by the automatic circuit breaker owing to the operating value of the current being more definite with the latter. Also, a circuit breaker has a further advantage in that the continuity of the circuit can be re-established at once after the circuit has been opened by the excess current, whereas the replacement of a fuse occupies an appreciable time. The elimination of this time element is a matter of very great advantage in connection with electric traction work and other applications of motors where momentary excesses of current occur frequently.

Principle.—A circuit breaker in its simplest form consists essentially of a switch which is closed against the action of a strong spring. The switch is kept closed by a latch controlled by a trigger which is operated by a blow from the plunger of a solenoid connected in series with the circuit to be protected. Such circuit breakers are opened when an excessive current passes. As has already been stated, the interruption of the current in an inductive circuit gives rise to an abnormal E.M.F.: hence the opening of a circuit breaker on load will be accompanied by an arc bridging across the points at which the circuit is broken. To protect the metal parts of the switch from the destructive action of the arc, auxiliary carbon contacts are connected in parallel with the main switch contacts, and so arranged that the latter are opened before the auxiliary contacts. The resulting sparking is

thus transferred to the carbon contacts, which are designed so that they can be readily replaced. Certain forms of circuit breakers are provided with magnetic blow-out coils, so that the circuit is broken in a strong magnetic field, and, as has already been explained, the inter-reactions between this field and the current blow out the arc.

Types of Circuit Breakers.—Type 1.—Figure 276 illustrates the principle of construction and diagram of



+ Fig. 276.—Circuit breaker with force magnetic blow-out.

electrical connections for a circuit breaker fitted with a magnetic blow-out coil. The switch proper consists of a large laminated copper contact A, which is pressed against the main contact blocks BB when the circuit closed. breaker is contact A is fixed to, but insulated from, the steel rod C, which can be given a vertical motion of from 4 to 5 centimetres by means of the toggle lever D operated by the insulated handle E. close the circuit is applied handle in the direction of

the arrow, thus bringing the links of the lever into line and pushing up the rod C against the action of a steel spring F. The contact is held in place against the tension of the spring by a latch G, fixed to the armature P of an electro-magnet, engaging with a projection on the lower arm of the lever. The blow-out magnet consists of two iron cores II provided with common pole pieces N and S (the latter has been removed in Figure 276 so as to show the blow-out arrangement).

The coils HH are wound over the cores II, and connected through a carbon plug contact J in parallel with the main contacts, the contact J being enclosed in a fibre box K. The former is fixed to the top of the rod C, so that it lies in the strong magnetic field between the poles

N and S as shown, and is closed or opened according as the main contacts are closed or opened. Owing to the comparatively high resistance of the plug contact J practically no current passes through them while the circuit breaker is closed. The plug is not withdrawn until after the contact A has left the blocks BB. Immediately the switch A is opened the whole of the current passes through the blow-out coils, and the strong magnetic field extinguishes the arc as soon as it is formed at the plug contacts.

The electro-magnet for opening the circuit breaker consists of an iron core wound with a coil M which carries the main current. The armature P of the electro-magnet is attached to the latch G, and is held some distance above the electro-magnet by means of a spring R. When the current passing through the coil M reaches a certain value the armature P is pulled down against the tension of the spring R, thereby releasing the latch G and allowing the switch to open. The current at which the circuit breaker will open depends upon the tension of R, and this can be adjusted over a wide range by means of a thumb-screw. When it is desired to open the circuit breaker the trigger may be tripped by pulling down the rod T which is fixed to the armature P.

Type 2.—A type of circuit breaker provided with auxiliary carbon contacts is illustrated in Figure 277. The jamb brush contacts CC form the switch proper. The terminals A and D are connected to the circuit which has to be protected, and when the switch is closed a circuit is completed from the main terminal A through the operating solenoid B connecting strap and main contacts CC to the second main terminal D. laminated contact of the switch is bolted to a steel rod N, which works in a bush O fixed to the base of the switch. Inside this bush is a powerful compression spring which acts on N, tending to open the switch. close the circuit breaker the operating handle E is lifted to the position shown dotted, so that the projection E<sup>1</sup> on the handle engages with the projection F<sub>1</sub> on the togglejointed lever F. The toggle joint is thereby straightened, and the laminated contact C is forced against its solid contact blocks with considerable pressure. The switch and toggle lever are held in this position after the handle is released by the roller  $F_2$  engaging with the latch G.

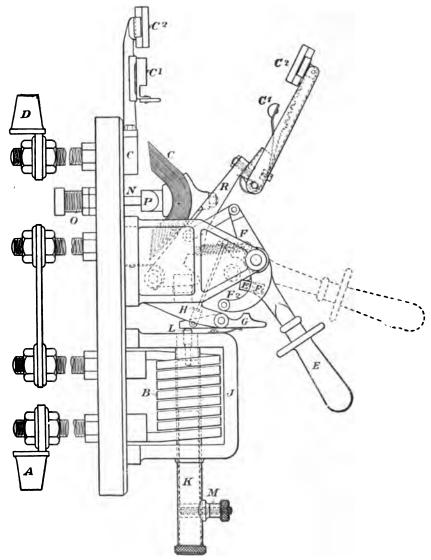


FIG. 277.—Circuit breaker with carbon break.

The electro-magnet for opening the circuit breaker consists of a coil B wound over a brass tube. Inside

the latter is placed an iron core K, which rests on an adjustable stop M, the magnetic circuit of the former being completed through the yoke J. When the current passing through the circuit breaker exceeds a predetermined limit the coil B pulls up the plunger K, which strikes the pin L with sufficient force to cause it to cant the latch G and thereby open the switch. By means of the adjustable stop M the operating current can be varied within wide limits.

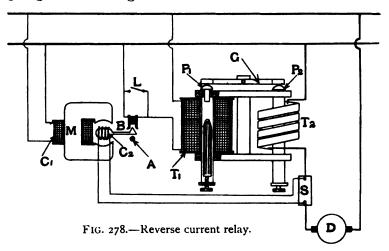
To open the circuit breaker by hand the loose handle E is depressed until the connecting link H tilts the latch G. The auxiliary copper and carbon contacts C<sup>1</sup> and C<sup>2</sup> respectively are connected in parallel with the main contacts CC, and the switch is so designed that the latter is opened before the contacts C<sup>1</sup> or C<sup>2</sup>.

Reverse Current Circuit Breakers.—It was pointed out on page 380 that when two or more dynamos are operated in parallel it is essential to insert, between each dynamo and the bus-bars, an automatic device to open the circuit when a predetermined reverse current flows. Any of the overload circuit breakers already described may be used to operate with reverse currents by connecting the operating solenoid in series with a source of current and a switch which is closed by a relay, thus completing the solenoid circuit and opening the circuit breaker on the passage of a reverse current.

The usual practice, however, is to connect in series with each dynamo a circuit breaker fitted with two tripping coils, one of which operates on the passage of an excess current and the other when a reverse current flows. The reverse current device may be operated either by a relay or direct.

Reverse Current Relay.—The principle of this type is illustrated in Figure 278. The arrangement consists of a moving coil polarised relay, which is in reality a small motor. The field magnet M of the relay is excited by a fine wire coil C<sub>1</sub> which is connected across the dynamo bus-bars. The moving coil C<sub>2</sub> is operated by the difference of potential across a shunt S which is connected in series with the dynamo D. When current flows through the moving coil the latter is subject to

torsion, tending to produce rotation in a clockwise direction, but is prevented from doing so by a contact B carried by the moving coil impinging against a stop A. On the passage of a reverse current, the magnitude of which is determined by the adjustment of a controlling spring, the moving coil rotates in a counter clockwise



direction, and the contact B completes the circuit through the tripping coil  $T_1$  of the circuit breaker. The coil  $T_1$  pulls up its plunger, strikes the pin  $P_1$ , and tilts the latch G, thus breaking the circuit. The coil  $T_2$  is connected in series with the dynamo, and operates the circuit breaker on the passage of an overload current by its plunger striking the pin  $P_2$  and tilting the latch G. The latter performs the same function as the latch G shown in Figure 277.

The trip coil T<sub>1</sub> may be connected across the bus-bars, and constructed with such a factor of safety that even should the bus-bar pressure fall below 75 per cent. of its normal value it will be sufficiently strong to open the circuit breaker. In parallel with the relay may be connected a switch L arranged at a distance from the switchboard, so that by closing it the circuit through T<sub>1</sub> is completed and the circuit breaker thereby opened.

Direct-Acting Reverse Current Release. — Figure 279 illustrates the principle of a direct-acting reverse current release designed by Leonard Andrews. It

consists of two iron cores A<sub>1</sub> and A connected by yokes YY so as to form a closed magnetic circuit. An iron plunger P, fitting loosely into a brass tube as shown, forms the armature of the magnetic circuit. To operate

the circuit breaker the plunger P is pulled up, thus causing a small pin to strike the latch C and thereby operate the circuit breaker. The height of the plunger P can be adjusted by a set-screw.

Over the cores  $A_1$  and A are wound shunt and series coils  $S_H$  and  $S_E$  respectively. The former is connected in parallel with the busbars and the latter in series with the circuit to

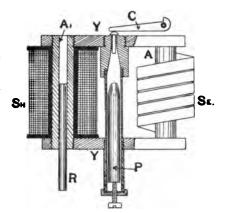


Fig. 279.—Direct-acting reverse current release.

be protected. The series and shunt windings are so connected that under normal conditions—that is to say, when the generator is doing useful work—the fluxes will flow through the field-magnet limbs in series, avoiding the centre path formed by the plunger P and its air-gap.

A feature of this type of release is that it may be used exclusively for reverse currents, or as a combined overload and reverse current device. It will be apparent that if the cross-section of the core A<sub>1</sub> be very much less than that of A a heavy current in the series winding will saturate A<sub>1</sub>, and there will consequently be a considerable magnetic leakage through the air-gap and plunger P which will operate the circuit breaker. If, on the other hand, the core A<sub>1</sub> be of greater cross-sectional area than A the shunt core will provide an easy path for any flux set up by the series winding. There will then be no leakage through the plunger P, and therefore no tendency for this to be attracted with an excess current. Thus with a shunt core larger than the series the release operates only with a reverse current, and will not be affected by a forward current of any magnitude.

When, however, the series core is made the larger the release will operate either by a current in S<sub>E</sub> tending to induce a flux in the closed iron circuit in the opposite direction to the flux induced by S<sub>H</sub>, or by a heavy current in the series winding producing a flux in the same direction as that produced in the shunt winding, but of such a magnitude that the shunt core becomes saturated and the leakage flux through the plunger P attracts the latter; that is, the device will then work as a combined maximum and reverse current release.

In practice the cores of the shunt and series windings are made hollow, and provision is made for the insertion of a solid iron rod R. The latter may be inserted in either the shunt or series coil to produce either a reverse current or a combined maximum and reverse circuit breaker as desired. In the case of the latter the release can be made to operate at any predetermined value of excess current by adjusting the length of the iron core inside the S<sub>E</sub> coil, and by adjusting the height of the movable tripping core P the relay can be set to operate at any desired value of reverse current.

Minimum Current Circuit Breaker.—When a dynamo is used in conjunction with a battery of accumulators for, say, a small lighting plant, the best practice is to connect the dynamo to the battery through an automatic cut-out which will disconnect the dynamo on the charging current falling to a predetermined minimum value. device prevents a reverse current flowing from the battery through the dynamo.

Figure 280 illustrates the principle of construction and diagram of connections of a minimum current cut-It consists of three solenoids. Those marked A and B are fixed, and their cores are connected to the yoke D. The core of the third solenoid C is pivoted at O, and free to move through a small angle in a vertical plane. To the lower end of the core C is fixed a rocking lever L, to the right-hand end of which is fixed a copper fork-shaped connector F. When the core of C is near to A the ends of the connector F dip into the mercury cups  $G_1$  and  $G_2$ .  $G_2$  is connected to one terminal of the cut-out, while G<sub>1</sub> is fixed to the metal bar H. The electrical connections between the battery and the dynamo are indicated by the red lines. There are three terminals  $T_1$ ,  $T_2$ , and  $T_3$ . The positive and negative leads of the dynamo are connected to  $T_2$  and  $T_3$  respectively. The negative pole of the battery is connected to  $T_1$ , and the other pole to  $T_2$  through the switch S. The coil C is connected across  $T_1$  and  $T_2$ , and is therefore energised by the whole number of cells; the difference coil A is connected across  $T_1$  and  $T_3$  so that the current exciting it will depend upon the difference between the dynamo and the battery voltage. Terminal  $T_3$  is connected to

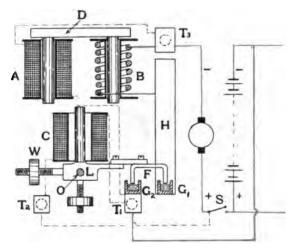


FIG. 280.—Minimum current cut-out.

the bar H through the coil B, which is energised by the current passing between the dynamo and the battery.

The operation of this cut-out or "accumulator switch" is as follows. On closing the switch S the coil C is energised, and its core becomes magnetised. The coil A is excited by a current depending for its direction and magnitude on the difference between the dynamo and the battery voltage. As soon as the former exceeds the latter by about 6 volts the core of C is repelled from A, and F connects the battery to the dynamo through coil B, which is so connected that the charging current confirms the action of coil A and holds the connector firmly in the mercury cups.

On the dynamo voltage falling, as would happen on shutting down the prime mover or in case of accident, the current in B decreases, and whenever the current falls to about zero the connector F is, by the attraction of gravity on the adjustable balance weight W, pulled out

of the cups  $G_1$  and  $G_2$ .

It will be seen, from what has now been said, how the term "accumulator switch" comes to be applied to this device, since it not only opens the circuit on the current falling to a safe minimum, but also prevents the charging circuit being completed until the dynamo pressure exceeds that of the battery. The minimum current at which the cut-out will act can be determined by the adjustment of the weight W.

## LIGHTNING ARRESTERS

When lightning discharges occur in the vicinity of an electrical transmission line there may be an enormous rush of current along the line, due to either of the following causes—(1) electro-static induction; (2) the magnetic effect of the lightning discharge inducing an E.M.F. in the line; or (3) by the lightning discharge actually striking the line on its passage to earth. The resulting increase in the pressure of the line may be of such a magnitude as would pierce the insulation of any electrical apparatus or machinery connected therewith, and transmission lines must be protected against such a contingency. The devices used for this purpose are known as "Lightning Arresters." They are designed to form an easy path to earth, thereby tending to preserve the normal potential of the line.

The general principle of lightning arresters is illustrated in Figure 281, where positive and negative feeders F are connected to bus-bars, marked + and -, and supplied with current from the dynamo D. In series with each feeder is a coil C<sub>1</sub> C<sub>2</sub> consisting of from 10 to 13 turns of bare copper wire. This coil is mounted on an insulating base, and is known either as a "choking coil," "impedance coil," or "kicking coil." The terminal of each coil remote from the bus-bars is

connected to earth (as shown at E) through a small air-

gap G, G, formed between metal rods.

The action of the apparatus is as follows. When a feeder becomes charged by lightning violent surging of current, at enormous potential, is set up, which, if not arrested before reaching the machinery connected to the line, would break down the insulation thereof. pede the progress of such surging currents the choking coils C<sub>1</sub> C<sub>2</sub> are introduced, and their impedance opposes

the flow of current to the bus-bars by offering a much higher resistance to the lightning discharge than earth connection through the gaps G<sub>1</sub> and G<sub>2</sub>. lightning discharge therefore passes to earth through G and G, instead of

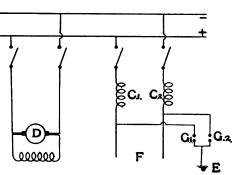


FIG. 281.—Principle of the lightning arrester.

puncturing the insulation of the machinery and controlling apparatus connected to the system.

The bridging of the gaps sets up an electric arc, and under such conditions the generator pressure, though not of sufficient magnitude to start an arc across the gaps, may be of such a value as to be capable of maintaining one started by lightning discharge. These arcs, if allowed to continue, would not only destroy the arrester, but would in many cases permit such an excess flow of current as to overload the generators or other apparatus connected to the line. Provision must therefore be made for the extinguishing of the arc consequent at discharge.

It will now be clear that two conditions are essential to an efficient device for protection against lightning discharges. The lightning arrester must offer less obstruction to high potential discharge in its path to earth than any other part of the circuit, and it must be constructed so as to extinguish the arc that is formed

across the air-gaps. The first of these conditions determines whether the lightning will discharge through the arrester or some other part of the circuit, and the second whether the arrester will extinguish the arc on the circuit or whether it will be destroyed by it. Upon these fundamental principles is based the construction of

all commercial lightning arresters.

Although the reactance coils (C<sub>1</sub> C<sub>2</sub>, Figure 281) act to choke a sudden increase of voltage, as in the case of lightning, it does not prevent the gradual building up of the static potential, which may be the cause of a discharge as dangerous to insulation as the direct discharge of lightning. On this account the spark-gap resistance must be considerably less than the insulation resistance of the machinery and apparatus protected. For transmission lines the spark-gap must be adjusted to such a length that the normal pressure of the generators is insufficient to bridge it, and over which the lightning may discharge without allowing the potential between the line and earth to increase to an unsafe value ranging. say, from 100 to 200 per cent. of the normal line pressure.

Examples of Lightning Arresters. — The various types of lightning arresters now used differ from each other in the means employed for extinguishing the arc

formed at the instant of discharge.

Type 1.—Figure 282 illustrates the construction of a lightning arrester in which a magnetic blow-out provides for the immediate extinction of the arc, a method which is invariably adopted for lightning arresters connected to direct-current circuits. The spark-gap G is formed between the ends of two short brass rods B<sub>1</sub> and B<sub>2</sub>. The length of the spark-gap may be adjusted when necessary. The rod B<sub>1</sub> is connected to the line terminal L, and B<sub>2</sub> to the earthed terminal E through a carbon rod C, which forms a high non-inductive resistance to limit the discharge current. The magnet coil M of the magnetic blow-out is connected in parallel with a part of the non-inductive resistance C, and wound on an iron core. From the latter there projects the pole pieces N and S, which are arranged so that the arc formed at G

is in a strong magnetic field and is thereby extinguished. The arrester is enclosed in a porcelain box, the cover of which has a small hole in it opposite the gap G, through which the arc is blown. The hole also allows the hot vapour to escape to atmosphere. The electrical connections are indicated by the chain-dotted lines.

Type 2.—Another type of lightning arrester is illustrated in Figure 283. It consists of an air-gap G formed between carbon rods B<sub>1</sub> and B<sub>2</sub>. B<sub>1</sub> is connected to the line terminal L, and B<sub>2</sub> to the earth terminal E

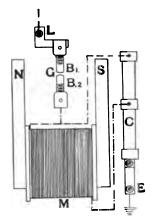


FIG. 282.—Lightning arrester.

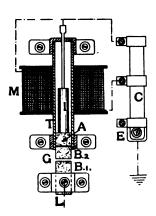


FIG. 283.—Lightning arrester.

through a carbon contact A, iron core I, and the resistance rod C, which forms a high non-inductive resistance. The core I is fixed to A, and placed inside a brass tube T, so that the lower end of A rests on B<sub>2</sub>. Over the tube T is wound a magnetising coil M, which is connected in shunt across a portion of the resistance C. At the instant of discharge a current flows from L to E by bridging the gap G. The arc formed is extinguished by the coil M becoming energised, pulling up the iron core I, and breaking the contact between B<sub>2</sub> and A. The coil M also acts as a magnetic blow-out, and immediately extinguishes the arc formed at G, on accomplishment of which the core I falls back into place, thus resetting the arrester.

Method of Earthing Lightning Arresters. - The

connections from the line to the arrester and from the arrester to earth should be as free from angles and bends as possible, in order to have an arrester circuit of minimum inductance. Where turns are absolutely necessary the wire should never be bent at an angle, but in a curve of long radius. The wire forming the earth connection should not be smaller than No. 8 S.W.G. In such situations, as a wire would be liable to mechanical injury, it is sometimes expedient to substitute it by a length of iron pipe. The connection between the wire and the pipe should be made by soldering the former to the top of a plug, screwed into the pipe. The wire must on no account pass through the pipe, or its reactance when surrounded by iron would impede the discharge through the arrester.

The earth wire should be connected to a copper plate having a thickness of about 2 millimetres and a surface of at least 120 square centimetres. The earth plate should be buried in damp soil in a bed of powdered coke or broken carbons and the wire should form contact with the plate for at least 60 centimetres, being

carefully soldered or riveted.

## Principles of Switchboard Design

Having now described in detail the several pieces of apparatus requisite for the due protection and control of electrical machines, etc., attention will be directed to a consideration of the usual methods of disposing and arranging such apparatus. For convenience in manipulation it is necessary that the several parts be assembled as compactly as is consistent with electrical security; this end is best attained by disposing the parts upon an incombustible board or panel. Such boards or panels, taking a variety of forms depending upon the nature of the currents and pressures to be dealt with, are called "switchboards."

The primary object of a generating station switchboard is to collect the current from the generators and direct it into the conductors, and so to the points of utilisation. The switch-gear and instruments necessary for controlling the output of the generators consists essentially of the following:

- 1. Rheostats for regulating the pressure generated.
- 2. Switches for enabling individual generators to be connected to the bus-bars.
- 3. Cut-outs for protecting the generators and mains.
- 4. Instruments for measuring the output of the generators, the power supplied to the feeders, and the pressure at which it is supplied.

Switchboards should be erected so that every part is easily accessible. They should also be placed in such a position that the operator commands a view of the machines controlled. To this end switchboards in stations having several generating sets are usually erected on an elevated fireproof platform.

It is essential that a switchboard be constructed as far as possible of incombustible material, and for this reason the panels are made of slate or marble slabs. Being the less expensive, slate is the more often used. Suitable frames for supporting the panels are usually made from T and L section iron. In bolting the panels to these frames care must be taken to ensure efficient insulation between them. This is often accomplished by bushing the holes in the panels through which the bolts pass with vulcanite, and by inserting rubber washers between the panels and the frame.

The disposition of the switch-gear and instruments should be such that the function of each part is clear without reference to diagrams or descriptions; in fact, every switchboard should be so designed that, as far as possible, it is its own diagram of connections. Principally in order to fulfil this requirement, switchboards are now constructed on the "panel" system; in which all the switch-gear and measuring instruments pertaining to one machine or one feeder are kept together on a single panel. This system also facilitates extensions as the number of generators and feeders require to be increased.

For interconnecting the controlling apparatus and instruments bare copper strip or rod should be used in

preference to insulated cable, as the dielectric of the latter is usually highly inflammable. Every interconnection should be run as straight between its terminals as possible, and conductors between which there exists a large difference of potential should be kept well apart. The bus-bars themselves are supported either on, but insulated from, angle iron brackets fixed to the framework, or on porcelain pillars bolted to the switchboard panels. The former method is better, as individual panels can then be removed without disturbing the bus-bars.

Circuit breakers, if possible, should be placed at the top of the panels, so that in the event of their opening when abnormal conditions arise there is no apparatus above them to sustain possible injury; also, they are then high enough up to preclude the possibility of injury to an attendant. The indicating instruments are then fixed immediately below the circuit breakers, while switches, rheostats, regulators, and fuses are mounted between the instruments and the bottom of the

panels.

As a rule the multiple contact switches of shunt-regulating rheostats are mounted direct on the panels, and when the resistance boxes are of small dimensions they are fixed to the back. Where this is impracticable the resistance is placed in the most suitable position, and connections from its various terminals made to the contact study of the switch.

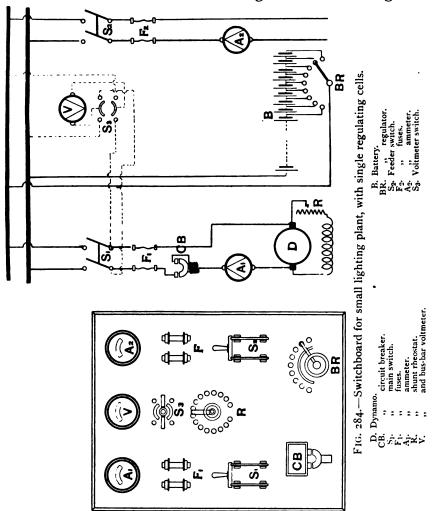
#### Two-Wire System of Distribution

The simplest system of distribution is the "two-wire," in which the power-consuming apparatus is connected between two distributing mains connected to the bus-bars. This system is employed for private house lighting, power installations, and electric traction.

Switchboards for Small Lighting Plants: Arrangement A.—Figure 284 is a diagram of connections and arrangement of switchboard for a small lighting installation consisting of a shunt-wound dynamo D and a battery of secondary cells B. The arrangement is suitable where the dynamo is intended to charge the

cells during the daytime, while in the evening lamps are supplied with current from the battery.

In this and the following switchboard diagrams



positive and negative leads are indicated by red and blue lines respectively.

The dynamo is connected to the bus-bars through an ammeter  $A_1$ , minimum current circuit breaker CB, double-pole fuse  $F_1$ , and double-pole switch  $S_1$ . A regulating

rheostat R is connected in series with the shunt coils of

the dynamo.

One pole of the battery is connected direct to one of the bus-bars, while the other end is arranged with regulating cells controlled by a regulating switch BR, the switch lever of which is connected to the other busbar. The principle of the battery regulating switch has been described on page 145 and illustrated in Figure 78.

The supply mains are connected to the bus-bars through a double-pole switch  $S_2$  and double-pole enclosed fuse  $\tilde{F}_2$ , while an ammeter  $A_2$ , inserted in series with the positive supply main, indicates the current taken by the lamps. The voltmeter V may, by means of the two-way switch  $S_3$ , be made to indicate either the pressure at

the bus-bars or the pressure of the dynamo.

To charge the cells the supply mains are disconnected from the bus-bars by opening the switch S<sub>2</sub>, and with all the regulating cells in circuit the dynamo is run up to speed and adjusted to give a slightly greater pressure than the battery. The switch S<sub>1</sub> is then closed, and if the dynamo voltage be sufficiently in excess of that of the cells the circuit breaker CB closes automatically. The charging current is adjusted to the required value by adjusting the shunt rheostat.

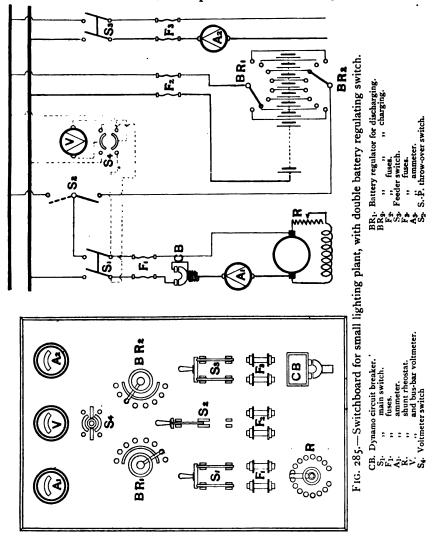
When the battery is supplying current to the lamps the switch S<sub>2</sub> will be closed while S<sub>1</sub> is open, and the E.M.F. across the bus-bars can be regulated as already stated by means of the battery regulating switch BR.

With this arrangement the dynamo should be designed to be capable of generating an E.M.F. about 40 per cent. greater than the normal discharging E.M.F. of the battery. The method of determining the maximum E.M.F. the dynamo is required to generate is set forth in an example

on page 144.

Arrangement B.—In some installations where the current is supplied by accumulators it may not always be convenient to disconnect the supply mains from the source of E.M.F., in which case the battery is provided with charge and discharge regulating switches. The diagram of connections for this arrangement is shown in Figure 285.

The negative terminal of the dynamo is connected to the bus-bars through an ammeter  $A_1$ , minimum current circuit breaker CB, one pole of the fuse  $F_1$ , and main



switch  $S_1$ . The positive terminal is connected through the other pole of the fuse  $F_1$  and switch  $S_1$  to the single-pole throw-over switch  $S_2$ . The upper contact of the latter is connected to the positive bus-bar, and the other

contact to the arm  $BR_2$ , of the battery regulating switch. The latter is provided with two arms; one arm  $BR_1$  is permanently connected to the bus-bars through one pole of the fuse  $F_2$ , so as to maintain a constant bus-bar voltage, and the other arm  $BR_2$  is used for cutting out the regulating cells as they become charged. The negative pole of the battery is connected to the bus-bars through the other pole of  $F_2$ . The supply mains are connected to the bus-bars through an ammeter  $A_2$ , and double-pole

switch and fuse S<sub>3</sub> and F<sub>3</sub> respectively.

To charge the battery the switch S<sub>2</sub> is thrown over to the lower contact and the battery switch BR, adjusted so as to include all the cells in the charging circuit. The dynamo is then connected in parallel with the battery, and its shunt-regulating resistance is adjusted so as to give the desired charging current. The battery discharging switch is employed to regulate the pressure of the supply mains. When charging commences E.M.F. required per cell will be about 2.1 volts, while at the end of charging it will require to be as much as from 2.5 to 2.6 volts; hence to maintain a constant pressure across the supply mains the number of discharging cells must be decreased as the E.M.F. of the battery increases. The number of regulating cells should be such that when the cells are fully charged they are all cut out of the discharging circuit. .

Occasionally it may be required to connect the dynamo direct to the supply mains, in which case the switch S<sub>2</sub> is thrown over to the upper contact. No charge must be given to the battery when the dynamo is thus connected, as the main portion of the battery would

be charged more than the regulating cells.

The voltmeter switch  $S_4$  is in this case also provided with two-ways, so that the voltmeter V can indicate the pressure of either the bus-bars or the dynamo. A switch-board suitable for this installation is also shown.

Arrangement C.—With the arrangement just described it will be seen from the diagram of connections that the total current from the dynamo flows through those regulating cells which are connected between the charge and discharge arms of the regulating switch; and

the generator current must therefore not exceed the normal rate of charge of the battery, otherwise the regulating cells will be charged at an excessive rate. Again, as the current supplied by the generator divides between the load connected to the feeders and the main portion of the battery it follows that, if the load on the feeders be comparatively large, the main portion of the

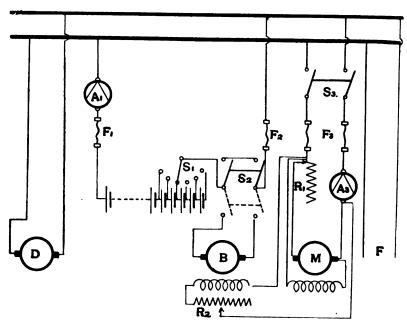


FIG. 286. Switchboard for small lighting plant, with battery and booster.

D. Dynamo.
F. Feeder.
A<sub>1</sub>. Battery ammeter.
A<sub>1</sub>. Battery ammeter.
A<sub>1</sub>. Battery ammeter.
A<sub>1</sub>. Battery ammeter.
A<sub>1</sub>. R<sub>2</sub>. , fuses.
S<sub>1</sub>. , regulating switch.
S<sub>2</sub>. D.-P. throw-over switch.
A<sub>3</sub>. , fuses.
A<sub>3</sub>. , ammeter.

battery will be charged at a very slow rate, and consequently the time required to charge it will be inconveniently long.

These disadvantages may be overcome by adopting an arrangement as shown in Figure 286, where a booster is connected in series with the charging circuit. The generator D and feeders F are connected to the bus-bars through the necessary instruments and switch-gear. The

negative pole of the battery is connected through a fuse  $F_1$  and ammeter  $A_1$  to the negative bus-bar, and positive pole to the corresponding bus-bar by way of the single-regulating switch  $S_1$ , double-pole throw-over switch  $S_2$ , and fuse  $F_2$ . The top contacts of the switch  $S_2$  are connected together, and the armature B of the booster is connected across the lower contacts.

When the switch  $S_2$  is in the lower position the booster armature is connected in series with the bus-bars and increases the charging E.M.F. When the switch is on the top contacts the battery is connected direct to the bus-bars, as will be the case when discharging. The booster is direct coupled to a shunt motor M, which is connected to the bus-bars through a double-pole switch  $S_3$ , double-pole fuse  $F_3$ , ammeter  $A_3$ , and starting resistance  $R_1$ . The field-magnet coils of the booster are connected in parallel with the bus-bars in such a manner that its circuit is only completed when the motor switch  $S_3$  is closed. In series with the booster field coils is connected a regulating resistance  $R_2$ , by means of which the pressure across the battery can be increased as the charge proceeds.

The output of the booster should be equal to the normal rate of charge of the battery, and its maximum voltage equal to the difference between the maximum E.M.F. required to charge the battery and the normal E.M.F. of the bus-bars.

Switchboard for a Power and Lighting Plant.— Figure 287 shows the diagrams of connections and arrangement of switchboard for two compound-wound generators supplying current for lighting and power purposes. The design is suitable for a factory or mining installation having a capacity of from 200 to 500 k.w.

There are two generator panels. The positive terminal of each dynamo is connected to its bus-bar through one pole of the 3-pole switch  $S_1$ , ammeter  $A_1$ , and maximum and reverse current circuit breaker CB. The negative terminal is connected through the switch  $S_1$  to the negative bus-bar as shown. The third or middle pole of the switch serves to connect the negative terminal of the armature to an equalising bus-bar, and for reasons already explained the switch should be designed

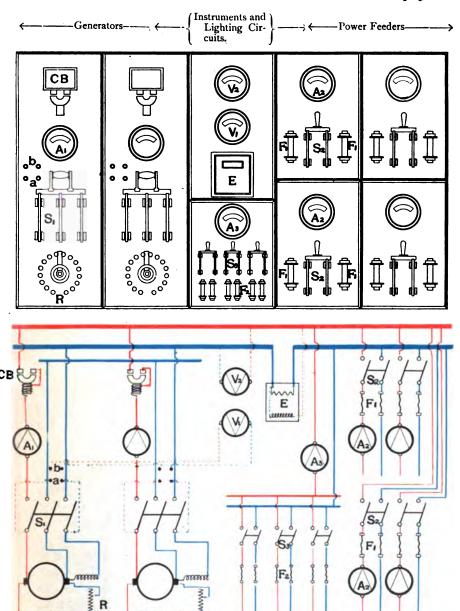


FIG. 287.—Switchboard for factory power and lighting plant.

	Generator	circuit breakers.
$S_1$ .	,,	main switches.
A <sub>1</sub> .	,,	ammeters.
R.	,,	shunt rheostats.

ab.	Voltmeter plug receptacles.
<b>V</b> <sub>2</sub> .	Bus-bar voltmeter.

	Tanal annance and an
E.	Total output meter.
Sn.	Power feeder switches

• •			
A2.	Power fee	eder an	meters.
	Lighting	circuit	switches.
F 2.	,,	,,	fuse.
Δ			ammeter

so that the equalising connection is made first on closing, and broking last on opening. In series with the shunt field coils is a regulating rheostat R.

Each generator panel is provided with voltmeter plugs and receptacles. The receptacles marked a are connected across the positive and negative terminals of each generator, while those marked b are connected to the voltmeter  $V_1$  as shown, the other voltmeter  $V_2$  being permanently connected across the bus-bars. Only one plug is provided, so that  $V_1$  cannot be connected to more than one generator at a time. The voltmeters are

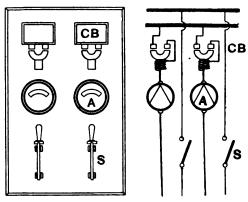


FIG. 288.—Feeder panel for power switchboard.

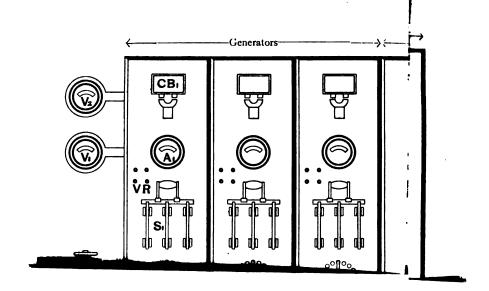
CB. Circuit breaker.

A. Ammeter.

S. Switch.

mounted on the top half of the third panel, together with an energy meter E for measuring the total output of the generators. When it is desired to connect a further generator to the bus-bars its E.M.F. is adjusted until both voltmeters read alike. The main switch is then closed.

In the switchboard illustrated there are four power circuits, each circuit being connected to the bus-bars through an ammeter A<sub>2</sub>, double-pole fuse F<sub>1</sub>, and double-pole switch S<sub>2</sub>. These are mounted on panels four and five, the apparatus belonging to any one circuit occupying one half of a panel. On the lower half of the third panel are mounted three double-pole switches S<sub>3</sub> and three double-pole fuses F, for controlling three lighting circuits,



the ammeter A<sub>3</sub> indicating the total current supplied to the circuits.

In large power installations where the current is conveyed by means of feeders from the switchboard to the centres of distribution the arrangement of feeder circuits would be as shown in Figure 288. The negative lead of each feeder is connected to the positive bus-bar through an ammeter A and maximum current circuit breaker CB, while the positive lead is connected to its bus-bar through the switch S. The arrangement of switchboard shows a feeder panel arranged for two feeders. The generator panels would be similar to that shown in Figure 287.

Traction Generating Station Switchboard.—Figure 289 is a diagram of connections and general arrangement of a traction switchboard. The panels may be grouped as follows—3 generators, 4 feeders, 1 battery and booster,

and I Board of Trade.

The generators are compound wound to give a pressure of 500 to 550 volts between no load and full load. They are connected through the 3-pole main switch S<sub>1</sub>, ammeter A<sub>1</sub>, and circuit breaker CB<sub>1</sub> to the positive and negative bus-bars. The terminal at which the armature and series field coils are joined is connected to the equalising bar EB through the middle pole of the switch S<sub>1</sub>. The shunt coils of the field winding are connected in series with a variable resistance R<sub>1</sub> and field break switch FS<sub>1</sub>. By inserting a four-pronged plug into the receptacles VR the voltmeter V<sub>1</sub> can be connected across any one of the generators. The voltmeter V<sub>2</sub> is permanently connected across the bus-bars.

Each positive feeder is connected to its bus-bar through a choking coil K (which is mounted on the back of the switchboard), wattmeter W, single-pole switch S<sub>2</sub>, ammeter A<sub>2</sub>, and circuit breaker CB<sub>2</sub>. The lightning arrester L is connected to the feeder end of the coil K. In systems of distribution for traction work the rails, except in special cases, are utilised as return leads (see Ra in the figure), and are directly connected to the negative bus-bar, the latter being efficiently

earthed.

The negative generator bus-bar is connected through

an ammeter A<sub>3</sub> to the negative feeder bus-bar.

A battery B worked in conjunction with a "High-field" booster Bo (see Figure 229, page 386) is connected across the bus-bars. Referring to the figure, the negative pole of the battery is connected to the negative bus-bar through an ammeter A<sub>4</sub>, recording ammeter RA<sub>1</sub>, and fuse F. The positive end of the battery is connected to the positive bus-bar through a two-blade throw-over switch S<sub>3</sub> and circuit breaker CB<sub>3</sub>. The top pair of contacts of S<sub>3</sub> are joined by a copper strap, so that when the switch is in the upper position the battery is connected direct to the bus-bars. The booster armature is connected to the lower pair of contacts, so that with the switch in the lower position the battery is connected to the bus-bars through the booster.

The driving motor M of the latter is connected to the supply through an ammeter A<sub>5</sub>, circuit breaker CB<sub>4</sub>, and starting resistance SR provided with a no-voltage release. In series with the field coils of the motor is a

rheostat R<sub>2</sub> for varying its speed.

The exciter armature E is connected in series with the shunt field coils of the booster, together with an ammeter A<sub>6</sub> and field break switch FS<sub>2</sub>. In series with the field of the exciter is a rheostat R<sub>3</sub> to control its voltage. The voltmeter V<sub>3</sub> is connected across the booster armature, and voltmeter V<sub>4</sub> can by means of a two-way switch S<sub>4</sub> be connected across either the battery or exciter. The total current output from the generators is sent partly through the series winding of the booster and partly through a variable diverter D, by adjustment of which a definite current can be passed through the booster series field.

The Board of Trade panel contains the instruments used for making and recording the various tests specified by the Board of Trade in their regulations relating to electric traction. The ammeter  $A_7$  is connected between the +ve bus-bar and the multiple-way switch  $S_5$ , by means of which it can be made to indicate the line leakage of any one feeder. This ammeter has two scales, one reading from 0 to 0.5 ampère, and the other

from 0.5 to 5 ampères. By means of the two-way switch S<sub>n</sub> either of these scales may be used. RV is a voltmeter reading from o to 10 volts for recording the potential drop in the uninsulated return leads. One terminal of the voltmeter is joined to the negative busbar, and the other to the movable arm of the multipleway switch S<sub>7</sub>, the respective contacts of which are in connection with different points on the rails. RA, is a recording ammeter, range o to 5.0 ampères, for recording the total leakage of current from the return leads. is connected in series with either a fusible or magnetic cut-out C, which short-circuits the ammeter in the event of the total leakage current exceeding the scope of its scale. The ammeter A<sub>8</sub>, indicating 0 to 25 ampères, is used to determine the efficiency of the earth connections of the negative bus-bar. Referring to the double-pole throw-over switch S<sub>8</sub>, the middle contacts are connected to the two earth plates EE as shown. The earth recording ammeter RA, is connected to the lower pair of contacts, and normally the switch is left on these contacts, thus keeping RA, in circuit. Connected in series across the upper contacts is the ammeter A<sub>8</sub> and three Lechanché cells. To test the resistance of the earth plates, the switch S<sub>8</sub> is thrown over to the top contacts so as to connect the ammeter and cells in series with the earth plates.

In arranging the switchboard the Board of Trade and battery panels are placed in the centre as shown. The generator and feeder panels are placed on the left-

and right-hand sides respectively.

Limits of 2-Wire System of Distribution for Electric Lighting.—In designing a system of distribution for lighting purposes the following considerations are of prime importance: (1) The current should be supplied at approximately constant pressure to all parts of the system, and (2) the cost of copper in the mains should not exceed the minimum consistent with the former consideration. Figure 290 represents a 2-wire system of distribution in which the distributors A and B are connected in parallel with the feeder F. The feeding centre to which A and B are connected is maintained at

a constant pressure of E volts. Considering the distributor A, suppose 3 consumers to be connected to it at the points marked a, b, and c, and that each consumer's demand is C ampères. Let  $r_1$  be the resistance of the mains between the feeding point and a, and similarly  $r_2$  and  $r_3$  the resistances between ab and bc. The drop in volts between the feeding point and a is  $3Cr_1$ ; and similarly,  $2Cr_2$  and  $Cr_3$  respectively between ab and bc. Thus it

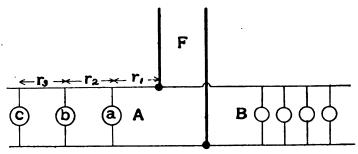


FIG. 290.—Two-wire distribution.

is clear that the pressure cannot be maintained exactly uniform at each of the consumers' terminals, since there will be a loss of pressure between each and the next nearer to the feeding centre.

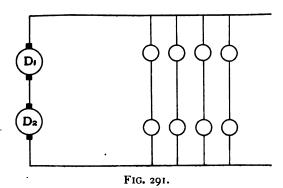
In the chapter on electric lighting attention was directed to the importance of connecting incandescent lamps to circuits in which the pressure could be maintained approximately constant. The Board of Trade regulations relating to electricity supply stipulate that the maximum variation of pressure from that declared shall not exceed ± 4 per cent. The extent of the area which can be efficiently supplied is therefore limited by the difficulties of regulation. The only methods of minimising the percentage pressure variation for a given power demand are by increasing the impressed voltage and thereby reducing the current, or by increasing the section of the conductors. The high cost of copper permits only a very limited recourse to the latter expedient.

One effect of doubling the pressure of a supply system is that the same power is transmitted at half the current,

and consequently a saving in copper is effected. Further, the pressure being doubled, the drop in any distributor may also be doubled without affecting the percentage variation, and thus the extent of the possible radius of

supply is increased 100 per cent.

In the previous diagram the voltage at the feeding centres was equal to E, and if the pressure of supply be doubled by connecting two dynamos  $D_1$  and  $D_2$  in series, as shown in Figure 291, then the same power can be transmitted at half the current; but if the same E volt lamps be still used they will have to be connected two in series across the mains as shown. This system has two inherent drawbacks: first, the lamps require to be



connected to the mains in pairs so that two lamps may be in use when only one is necessary; and second, should the filament of one lamp break the other is immediately extinguished.

The "two-wire" system of distribution for incandescent electric lighting is therefore limited to about 250 volts, this being the maximum pressure for which it has been found possible to commercially develop incandescent lamps.

# THREE-WIRE SYSTEM OF DISTRIBUTION

The inconveniences indicated of connecting two lamps in series across supply mains can, however, be overcome by making use of a third wire M (as shown

in Figure 292), which serves to connect the common terminals of pairs of lamps to the common terminal of the two generators. The addition of this third wire renders it possible to switch in single lamps, and if 2E denote the pressure between the positive and negative mains A and B, then the pressure between either A or B and the lead M is equal to E. This system of distribution was designed independently by Edison and the late Dr. John Hopkinson, and is known as the "three-wire" system of distribution. The positive and negative leads are referred to as the "outer" wires and the third lead M as the middle or neutral wire. When first

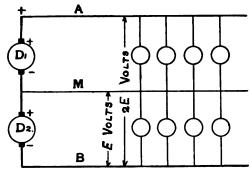


FIG. 292.—Three-wire distribution with the generators connected, two in series.

adopted the voltage between the outers of a 3-wire system ranged from 200 to 220 volts, as at that time carbon filament lamps were only manufactured for pressure up to about 110 volts. With the advent of the 250 - volt incandescent lamp most of the public supply companies in existence at that time doubled their supply pressure, so as to increase the area which could economically be supplied.

Public supply 3-wire systems in Britain are now invariably designed for pressures between the outers

ranging from 400 to 500 volts.

The operation of this system of distribution is as follows. Referring to Figure 292, when the load connected to the positive side is the same as that on the negative, then the entire length of the middle wire, be-

tween the common terminal of the dynamos and the feeding centre, is at the same potential as the former; hence no current will flow in the middle wire, and the system is said to be balancea. Such a condition, however, is ideal, and is not realised in practice. Suppose that the positive side be loaded to the extent of 240 ampères and the negative side has a load of 200 ampères, the out-of-balance current equals 40 ampères and flows along the middle wire. The generator  $D_1$  therefore has to supply 240 ampères, while  $D_2$  supplies only 200. Should the greater load be on the negative side, then the generator  $D_2$  will supply a greater current than  $D_1$  by an amount equal to the out-of-balance current.

It will now be seen that the middle wire has only to carry the out-of-balance current. The apparatus on a 3-wire system should be as equally disposed on each side respectively as possible, so that the current flowing in the middle wire is maintained at the minimum. There is usually no difficulty in arranging that the load on one side is at most never more than 50 per cent. in excess of the other. The usual practice is therefore to make the sectional area of the middle wire equal to half that of each outer.

Saving of Copper by Substitution of 3- for 2-Wire System supplying same Power at same Percentage Loss.— Suppose C ampères at E volts be conveyed to a feeding centre by means of two conductors each of I square centimetres cross-sectional area, with a definite percentage pressure drop. Now, if the pressure of supply be increased to 2E, C ampères could be transmitted to the same feeding centre with the same percentage drop through conductors each of  $\frac{I}{2}$  square centimetres sectional area. But since the pressure is doubled, only half the current will be required to deliver the same power. Hence to carry  $\frac{C}{2}$  ampères at 2 E volts, conductors of only  $\frac{I}{4}$  square centimetres will be needed.

Experience shows that in a 3-wire system a middle wire

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of half the section of that of each outer is ample. Now, adding  $\frac{I}{8}$  required for the middle wire to  $2\left(\frac{I}{4}\right)$  for the

two outers, the sum  $\frac{5}{8}$  I gives the total sectional area of conductor required with a 3-wire system at twice the pressure across the outers of the original 2-wire system. The ratio of copper in the two cases will then be expressed by

Three-wire 
$$=\frac{5}{8}I$$
  $=\frac{5}{16}I$   $=\frac{31.25}{100}$ .

That is, the adoption of the 3-wire system permits of

a saving in copper of nearly 69 per cent.

Use of Balances of 3-Wire System. — When the 3-wire system was first introduced balancing was effected by connecting the generators two in series across the outers, as indicated in the previous figure; but it soon became obvious that greater economy could be secured if single generators of double the voltage were used, and the out-of-balance current dealt with by means of a "balancer set." This had the effect of reducing the number of generators to one-half, thereby securing simplified switch-gear and connections, and higher efficiency.

A balancer set consists of two direct-coupled machines, each connected between an outer and the middle wire, as shown in Figure 293, where B<sub>1</sub> is connected to the positive side and B<sub>2</sub> to the negative. These machines should have as nearly as possible identical characteristic curves. Their fields are usually excited by means of shunt coils, each of which receives its current from the opposite side of the system to that in which the armature is running. For reasons mentioned below this cross-connecting of the balancer fields ensures automatic regulation.

The operation of the balancer set is as follows. If the system be balanced, then the machines run as two motors in series with equal voltages across their armatures and equally excited fields. When the load

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on the positive side exceeds that on the negative the voltage across the former is diminished, thus weakening the field of B<sub>2</sub> and thereby increasing the speed of the set. B<sub>1</sub> therefore generates an E.M.F. which is greater than that across the positive side of the system, and as a result delivers current to it. The current required to drive B<sub>2</sub> as a motor is taken from the negative side, thus equalising the demand of both sides of the system on the generators. If the negative side

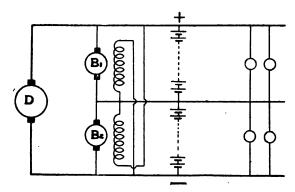


FIG. 293.—Three-wire distribution with balancers and battery.

be loaded to a greater extent than the positive, then B<sub>2</sub> runs as a motor driving B<sub>1</sub> as a generator.

In some cases the balancer machines are compound wound, the series windings being connected in series with the middle wire in such a manner that the field of the machine on the less loaded side is weakened, while that of the other is strengthened. The resulting increased speed and field excitation of the machine on the loaded side causes it to supply the extra current required.

In order to reduce the size of a balancer set it is highly desirable that the load on the system should be so disposed that the out-of-balance current is as small as possible. In practice the latter is found to be usually about 10 per cent. of the total output, so that the rated capacity of each of the machines need not exceed this percentage of the station capacity.

As a rule accumulators disposed in two batteries are used in conjunction with a 3-wire system. The

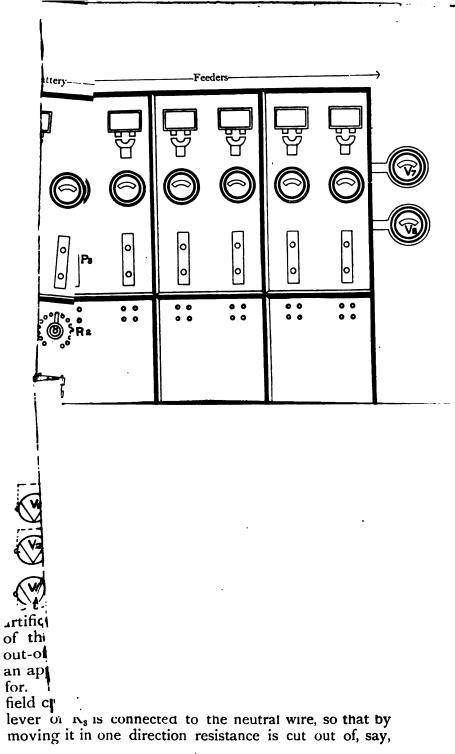
batteries are referred to as the "positive battery" and "negative battery." They act as a stand-by available for instantaneous use in case of emergency, as, for example, at the time of a sudden fog; also in comparatively small supply systems the generators may be shut down during periods of light load, and such load as there is intrusted to the accumulators.

Switchboard for 3-Wire System.—The diagram of connections and arrangement of switchboard for a 3-wire system of distribution is shown in Figure 294. There are three generators. The positive terminal of each is connected to the bus-bar through an ammeter A<sub>1</sub>, maximum and reverse current circuit breaker CB<sub>1</sub>, and plug bus-bar connector P<sub>1</sub>, and the negative terminal through a similar circuit breaker CB<sub>2</sub> and plug bus-bar connector P<sub>3</sub>.

In large supply systems it is usual to provide two or more sets of bus-bars, and to maintain them, if necessary, at different pressures. Long feeders supplying outlying districts would be connected to the bus-bars at the higher pressure; the increased pressure compensating for the increased fall of potential. In the case under consideration there are two sets of bus-bars, and by means of the plug connectors a generator may deliver its supply to either. The voltage of each generator is controlled by means of a rheostat R<sub>1</sub> in series with the shunt field coils. The voltmeters V<sub>1</sub> and V<sub>2</sub> indicate the pressure between either set of bus-bars, and by means of the voltmeter plug receptacles PR<sub>1</sub> any generator may be connected to voltmeter V<sub>3</sub>.

There are 4 positive and 4 negative feeders. Each feeder is connected to the bus-bars through an ammeter A<sub>2</sub>, maximum current circuit breaker CB<sub>3</sub>, and plug connector P<sub>3</sub>, by means of which a feeder may receive its supply from either set of bus-bars. The neutral feeders are connected to the neutral bus-bar, which is earthed through an ammeter RA to record the leakage current from the system. By earthing the middle wire the potential between either outer and the former does not exceed E volts where 2E denotes the pressure

between the outers.



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The positive and negative batteries are each connected to the bus-bars through a centre zero ammeter  $A_3$ , ampère-hour meter AM, battery regulating switch BR, maximum and reverse current circuit breaker  $CB_4$ , two-blade throw-over switch  $S_1$ , and plug-bar connectors. By means of the former the battery may be connected direct to the bus-bars, or have the booster inserted in series with it, as would be the case when the battery is being charged. Each booster field is connected, through a field-break switch FS, in series with a regulating resistance  $R_2$  across a battery as shown. By means of the 2-way switch  $S_2$  the voltmeter  $V_4$  may be connected across either the battery, or battery and booster, terminals.

The boosters may be driven by a direct-coupled shunt-wound motor connected to the supply, but the usual practice is to connect the booster one at each end of the balancer set, *i.e.* there are four machines in line all direct coupled. This arrangement simplifies the controlling apparatus, and experience has shown that the balancers are not affected in the due performance of their primary duties. Such an arrangement is illustrated in the case under consideration.

The machines constituting the balancer set are connected across one set of bus-bars through ammeters  $A_4$ , triple-pole switch  $S_3$ , triple-pole fuse F, and double-pole starting resistance SR, the common contact quadrant of the latter being connected to the neutral bus-bar through the middle pole of  $S_3$  and F, and centre zero ammeter  $A_5$ , to indicate the out-of-balance current. The voltmeters  $V_5$  and  $V_6$  are connected to indicate the pressure of each side of the system respectively.

As it is at the feeding centres that the pressures of the two sides of the system have to be maintained equal, artificial regulation is resorted to, the automatic regulation of the balancer being insufficient. When the load is out-of-balance the current in the middle wire may cause an appreciable pressure drop, which must be compensated for. This is effected by a rheostat R<sub>3</sub> connected in the field circuit of the balancer set as shown. The switch lever of R<sub>3</sub> is connected to the neutral wire, so that by moving it in one direction resistance is cut out of, say,

the generator field, and consequently into the motor field. This causes the generator side to develop a higher voltage at the station than the motor side, thus compensating for the additional drop in the middle wire and the outer carrying the heavier current.

Referring to the arrangement of switchboard, the balancer panel is in the centre, and on the right- and left-hand sides are respectively the positive and negative battery panels. Next to these the generator panels are disposed on one side and the feeder panels on the other. This arrangement facilitates extensions. Each feeder is provided with voltmeter plug receptacles PR<sub>2</sub>, by means of which voltmeter leads or "pilot wires" connected to the feeding centres may be put across either V<sub>7</sub> or V<sub>8</sub>. These voltmeters indicate the pressures at the feeding centres between any outer and the middle wire.

# APPENDIX

# APPENDIX

DETAILS OF COPPER WIRES USED AS ELECTRICAL CONDUCTORS

Metres per Kilogramme.		0.89 1.04 1.19 1.39	1.84 2.12 2.47 2.92 3.50	4.12 6.00 7.20 8.70	10.70 13.60 16.50 26.50 26.2
Kilogrammes per Ohm at 20° C.		8300.0 6170.0 4620.0 3400.0 2540.0	1950.0 1460.0 1075.0 770.0 535.0	385.0 269.0 180.0 127.0 87.0	57.5 35.5 24.0 9.5
	Metres per Ohm at 20° C.	7380.0 6370.0 5500.0 4720.0 4100.0	3600.0 3100.0 2650.0 2245.0 1870.0	1590.0 1320.0 1090.0 915.0 760.0	610.0 485.0 395.0 320.0 250.0
Ohms at 20° C. per Kilometre.		0.1360 0.1580 0.1820 0.2100 0.2450	0.2800 0.3200 0.3750 0.4450 0.5350	0.6300 0.7550 0.920 1.10	1.64 2.05 2.50 3.15 4.00
Cross-section	in Square Centimetres.	1.265 1.090 0.950 0.814 0.705	0.614 0.531 0.456 0.385 0.320	0.274 0.228 0.187 0.157 0.1295	0.105 0.0833 0.0685 0.0546 0.0429
Diameter in Millimetres,	Triple-cotton covered (T.C.C.).	13.20 12.30 11.40 10.65	9.30 8.67 8.05 7.45 6.85	6.30 5.28 6.44 6.85 6.45	4.05 3.65 3.30 2.70
	Double-cotton covered (D.C.C.).	:::::	  7.35 6.75	6.25 5.65 5.15 4.75 4.35	3.95 3.25 3.25 3.25 3.25 3.25 3.25 3.25 3.2
	Bare.	12.70 11.80 11.0 10.15	8.84 8.23 7.62 6.40	5.90 5.40 6.47 70.4	3.65 2.25 2.95 3.4 3.4
	S.W.G. No.	2/0 5/0 5/0 000	80-46	4 NO V®	90125

34.60 42.70 54.00 70.50 96.10	139.0 171.0 217.0 283.0 386.0	460.0 555.0 686.0 827.0 1015.0	1203.0 1444.0 1653.0 1900.0 2218.0	2628.0 3145.0 3840.0 4820.0 6170.0	8200.0 9610.0
5.50 3.55 2.23 1.30 0.707	0.340 0.222 0.139 0.0816 0.0442	0.0308 0.0216 0.0139 0.00960 0.00639	0.00454 0.00314 0.00240 0.00181	0.000952 0.000666 0.000442 0.000172	0.0000970
189.0 152.0 120.0 92.0 68.2	47.3 38.4 30.2 23.0 18.0	14.2 11.8 7.95 6.46	5.45 3.3.96 2.96 2.96	2.50 2.09 1.71 1.37 1.05	0.798 0.683
5.30 6.55 8.30 10.50	21.2 26.2 33.1 43.4 58.75	70.5 84.6 105.0 156.0	185.5 220.0 251.0 292.0 338.0	402.0 481.0 587.0 734.0 940.0	1257.0 1470.0
0.0324 0.0264 0.0208 0.01585 0.0117	0.00814 0.00659 0.00520 0.00398 0.00293	0.00245 0.00203 0.001645 0.00136	0.000932 0.000780 0.000685 0.000590	0.000429 0.000357 0.000292 0.000234 0.000182	0.000137
2.38 2.20 1.98 1.75	1.32 1.22 1.11 1.01 0.914	0.862 0.812 0.762 	:::::	:::::	::
2.30 2.10 1.90 1.65	1.220 1.118 1.015 0.915 0.812	0.762 0.710 0.660 0.610	0.559 0.503 0.508 0.482 0.457	:::::	::
2.03 1.83 1.63 1.22	1.017 0.915 0.8125 0.7110	0.5590 0.5080 0.4570 0.4160	0.3460 0.3150 0.2950 0.2740	0.2340 0.2138 0.1930 0.1730 0.1525	0.1320
41 15 17 18	20 21 22 23	25 27 28 28	29 30 33 33	34 35 37 38	40 39

#### **PROBLEMS**

#### CHAPTER I.—UNITS

I. A weight of 60 lbs. is raised vertically through a distance of 110 feet in 30 seconds. Calculate the work done in ergs and the power in watts.

(1)  $8.95 \times 10^{10}$  ergs; (2) 300 watts.

2. Find the horse-power of a motor to work a hoist raising I ton at the rate of 200 feet per minute, if the efficiency of the gearing be 75 per cent.

18 H.P.

3. If the motor driving the hoist mentioned in the last problem has a full-load efficiency of 90 per cent., calculate the current taken from the mains at full load.

65 ampères.

4. A dynamo supplies current to 400 glow lamps, each lamp taking 0.3 of an ampère at 220 volts. Calculate the kilowatts absorbed by the 400 lamps. Also if the lamps are alight for four hours, find the number of Board of Trade units consumed.

# (1) 26.5 K.W.; (2) 106 B.T. units.

5. In the last problem find the horse-power of the engine required to drive the dynamo, assuming the latter to have an efficiency of 90 per cent.

40 H.P.

6. A certain motor, connected to a 500-volt supply, drives a pump which raises 400 gallons of water per minute against a total head of 300 feet. If the combined efficiency at full load be 63 per cent., calculate the current taken by the motor.

[1 gallon of water weighs 10 lbs.]

84 ampères.

7. A motor is required to drive a train of 100,000 kilogrammes along a level track at 50 kilometres per hour. The tractive force required is 7 kilogrammes per 1000 kilogrammes of dead weight. Find the current required at 500 volts if the efficiency of motor and gearing be 70 per cent.

270 ampères.

8. In the last problem find the current taken by the motor when the train moves up an incline of 1 in 100 at the rate of 25 kilometres per hour. Assume the tractive force and efficiency to be the same as before.

330 ampères.

#### CHAPTER II.—FUNDAMENTAL PRINCIPLES

9. A circuit consists of 200 16-c.p. lamps, each lamp taking 4.1 watts per candle when supplied with current at a pressure of 230 volts. If each lead from the dynamo to the lamps has a resistance of 0.23 of an ohm, find the pressure required at the dynamo.

256 volts.

10. In the last problem, if the distance from the dynamo to the lamps be 450 metres, calculate the area of cross-section of cable required. The specific resistance of copper equals  $1.6 \times 10^{-6}$  ohms per centimetre cube.

#### 0.315 square centimetre.

11. Find the area of cross-section of a cable 650 metres long to transmit a maximum power of 100 k.w. at a pressure of 500 volts so that the drop in the cable will not exceed 35 volts.

[The total length of cable=1300 metres, since there must be two leads to transmit the power.]

1.2 square centimetres.

12. Find the diameter of a German silver wire, so that a length of 300 metres may have a resistance of 115 ohms.

[Spec. resce. of German silver =  $30 \times 10^{-6}$  ohms per centimetre cube.]

0.1 centimetre.

13. The field-magnet coils of a shunt-wound dynamo have a resistance of 98 ohms at 15° C. At the end of a six hours' test the resistance of the coils rises to 110 ohms. What is the mean rise of temperature?

Temperature coefficient of copper = 0.0043.

14. An electric water-heater has an efficiency of 81 per cent., and when connected to a 200-volt supply it consumes 1.5 ampères. How long will it take to raise 500 cubic centimetres of water from 19° C. to the boiling-point? One gramme of water may be taken as having a volume of 1 c.c.

11.5 minutes.

15. A water-heating apparatus absorbs 1.5 ampères at 230 volts, and in 9 minutes raises the temperature of 0.4 kilogramme of water from 20° C. to the boiling-point. Find the efficiency of the apparatus.

72 per cent.

16. An electro-plater requires 20 kilogrammes of copper per hour from a copper-depositing vat. What current must be used? E.C.E. for copper=0.000327 gramme per coulomb.

#### 1700 ampères.

17. An ammeter was connected in series with a copper voltmeter and a constant current passed through them. At the end of 20 minutes 19.7 grammes of copper were deposited. The ammeter indicated 52 ampères; was this correct? if not, what was the error in ammeter reading?

#### Ammeter indicated 4 per cent. high.

#### CHAPTER III.-ELECTRO-MAGNETISM

18. A solenoid 20 centimetres long is wound on a brass tube, the internal diameter of which is 8 centimetres, to a depth of 4 centimetres. If the coil carries a current of 0.5 of an ampère, find the number of turns necessary to produce a magnetising force of 100 C.G.S. units at the centre.

3200 turns.

19. An iron ring 4 square centimetres in cross-section, and 48 centimetres in mean circumference, is wound with a coil of 200 turns. If a current of 5.2 ampères produce a flux of 40,000 lines, find the permeability of the iron.

370.

20. Find the current required to produce a magnetic flux of  $2 \times 10^5$  lines in an iron core wound with a coil of 1000 turns. The core is 150 centimetres in length, 20 square centimetres in

cross-section, and has a permeability equal to 1000. The iron circuit is continuous except at a narrow air-gap 2 millimetres wide.

2.8 ampères.

21. A cast-iron ring has a section of 8.5 square centimetres and a length of 80 centimetres. If an air-gap 0.6 centimetre wide be cut in the ring, calculate the ampère-turns required to produce a flux of 50,000 lines in the air-gap. Coefficient of leakage = 1.3; the spreading of the lines of force in the air-gap may be neglected. Permeability of the iron = 1200.

#### 3250 ampère-turns.

22. The armature of a certain dynamo requires a flux of  $4.35 \times 10^6$  lines. If the coefficient of magnetic leakage be 1.25, determine the area of cross-section of the magnet core so that the induction density in the latter may not exceed 14,000 lines per square centimetre.

388 square centimetres.

23. How many watts will be absorbed by a mass of 10,000 cubic centimetres of iron undergoing 50 magnetic cycles per second, the loss per cycle per second per cubic centimetre being 10,000 ergs.

500 watts.

24. The armature laminations of a certain dynamo have a volume of 25,000 cubic centimetres, and are rotated in a magnetic field where B, in the armature core, equals 10,000 lines per square centimetre. From the curve in Fig. 24 calculate the watts absorbed due to hysteresis when the iron goes through 20 complete cycles per second. One cubic centimetre of iron weighs 7.8 grammes.

400 watts.

25. The armature of a 4-pole dynamo, revolving at 600 revolutions per minute, has a volume of 16,000 cubic centimetres of iron laminations. If the induction density B in the core = 12,000 lines per square centimetre, calculate the hysteresis loss in watts from Steinmitz's formula, hysteresis constant for the iron being 0.003.

325 watts.

26. Find the temperature rise of an iron core having a volume of 7500 cubic centimetres which undergoes 35 complete magnetic cycles per second for 35 minutes. The magnetic induction B = 10,000 lines per square centimetre, and

at this induction the loss in ergs per cycle per second per cubic centimetre = 13,000. Assume 60 per cent. of the heat generated is lost by radiation.

9.5° C.

27. The ascending and descending values of B and H for half a hysteresis curve are as follows:

Ascending—				
B = 90	2290	5000	6250	7500
H = I	1.5	2.5	3.5	5
Descending—				
B = 7050	6000	4300	2400	0
H = 3	1.2	o	<b>–</b> 0.5	<b>–</b> 1.1

Plot the curve and find the energy dissipated in ergs per cycle per cubic centimetre.

2350 ergs.

#### CHAPTER IV.—MEASURING INSTRUMENTS

28. A moving - coil soft - iron instrument requires 310 ampère-turns to produce a full scale deflection. It is proposed to use it as a voltmeter reading up to 260 volts. Find the diameter of the copper wire with which the working coil is wound if in series with it is connected a manganin resistance to absorb 220 volts. Mean length of one turn of the coil=14.5 centimetres.

#### Diameter = 0.05 millimetre.

29. The working coil of a moving soft-iron voltmeter has a resistance of 6000 ohms at 20° C. At this temperature it was calibrated, and indicated correctly on 300 volts. Find the percentage error when the temperature of the coil increases to 40° C. The coil is wound with copper wire having a temperature coefficient = 0.0043.

8 per cent.

30. In the last problem, if the resistance of the working coil be reduced to 600 ohms at 20° C. by winding it with the same number of turns of copper wire having a larger sectional area, and in series with it there be connected a manganin resistance of 5400 ohms, find the percentage error when the instrument is connected to 300 volts, the temperature of the working coil having increased to 40° C. Manganin has a zero temperature coefficient.

I per cent.

- 31. The moving coil of a voltmeter has a resistance of 150 ohms, and gives a full scale deflection with a current of 0.02 ampère. Find (1) the extra resistance required for a 100-volt instrument, and (2) the error caused by a rise in temperature of 30° C., assuming the extra resistance not to change with temperature.
  - (1) 4850 ohms; (2) 0.5 per cent.
- 32. A moving-coil voltmeter requires a current of 0.015 of an ampère to produce a full scale deflection. What must its resistance be if it has to indicate up to 300 volts? Also if the error caused by a rise in temperature of 20° C. has not to exceed 0.1 per cent. at maximum reading, how much of the winding must be of manganin, and how much may be copper?

#### Copper, 230 ohms; manganin, 19,770 ohms.

33. Calculate the dimensions of a manganin strip 0.5 millimetre thick to act as a shunt to a moving-coil instrument which gives a full scale deflection with 0.08 of a volt across its terminals. The instrument has to measure currents up to 400 ampères. Allow a radiating surface of 12 square centimetres per watt absorbed by the shunt. Specific resistance of manganin= $43 \times 10^{-6}$  ohms per centimetre cube.

# Breadth = 28.7 centimetres; length = 6.7 centimetres.

34. Determine the size of shunt required for a moving-coil instrument whose control is such that 3 ampère-turns produce a full scale deflection. The instrument has to indicate up to 100 ampères. The moving coil consists of 30 turns of copper wire having a resistance of 0.5 of an ohm, and the shunt is made of manganin.

# Breadth = 7.2 centimetres; length = 4.2 centimetres.

35. An electrolytic meter of the type illustrated in Figures 57 and 58 is to be used on a 200-volt circuit. If  $\frac{1}{100}$  of the main current flows through the electrolyte, determine the internal diameter of the second graduated tube  $T_2$  so that the mercury in this tube will rise to a height of 5 centimetres on 900 Board of Trade units being consumed. Electro-chemical equivalent of the electrolyte=0.001037, and 1 cubic centimetre of mercury weighs 13.6 grammes.

Diameter = 17.7 millimetres.

#### CHAPTER V.—SECONDARY BATTERIES

36. A battery has a discharging E.M.F. of 2.0 volts per cell at start, and gradually falls to 1.80 volts at end of discharge. If the internal resistance of each cell be 0.0005 of an ohm, what number of cells must be used (1) at commencement, and (2) at end of discharge, when they supply current to 800 30-watt lamps the potential across which is maintained constant at 120 volts?

(1) 63 cells; (2) 70 cells.

37. In the previous problem find the maximum E.M.F. of a dynamo required to charge the above cells with a current of 200 ampères. Each cell has an open circuit E.M.F. of 2.45 volts when fully charged, and there are 66 cells in circuit at end of charge. Resistance of leads between the dynamo and the battery = 0.02 of an ohm.

172 volts.

38. The E.M.F. of a certain accumulator was observed to be 2.0 volts on open circuit, but immediately fell to 1.95 volts when connected to an external circuit whose resistance was such that the cell discharged at 100 ampères. What was the internal resistance of the cell?

0.0005 of an ohm.

39. A battery of 110 accumulators is charged with a constant current of 100 ampères for 6.5 hours, the average E.M.F. required to charge each cell being 2.3 volts. The battery is afterwards discharged at 110 ampères for 5 hours, the average discharge E.M.F. being 2 volts per cell. Determine (1) the quantity efficiency and (2) the energy efficiency.

# Quantity efficiency, 85 per cent. Energy efficiency, 73 per cent.

40. A battery consisting of 60 cells has to be charged with a current of 40 ampères from 230-volt supply mains. If the charging E.M.F. per cell at commencement of charge be 2.1 volts, and 2.5 at the end of charge, determine the value of the resistance to be inserted in series between the battery and the supply mains (1) at commencement of charge and (2) at end of charge.

(1) 2.6 ohms; (2) 2.0 ohms.

## CHAPTER VI.—ELECTRIC LIGHTING

41. An incandescent glow lamp is found by a photometer test to give a mean spherical candle-power of 22. If the lamp be intended for use on a 110-volt circuit and the current taken when giving the above candle-power 0.4 of an ampère, determine the commercial efficiency of the lamp,

2 watts per candle.

42. If a particular 16-candle-power lamp costs one shilling, and its life varies with the efficiency as in Table VII., determine the most economical lamp to use when power costs twopence per Board of Trade unit.

## 3 watts per candle lamp.

43. A room has to be illuminated with 20 16-candlepower lamps, which are to be alight for four hours per day. If electrical energy costs fourpence per Board of Trade unit, determine the saving in power effected during one month of thirty days by employing tantalum lamps having an average efficiency of 2.1 watts per candle instead of 4-watt per candle carbon filament lamps.

Saving, 24 shillings.

44. An enclosed type of arc lamp gives its normal illumination when consuming 5 ampères at 80 volts. If it has to be connected to 100-volt supply mains, determine the value of the steadying resistance to be inserted in the lamp circuit.

4 ohms.

45. A hall 40 feet square has to be illuminated with a cluster of incandescent glow lamps placed in the centre and at a height of 14 feet above the floor level. If the farthest corner of the hall requires to be illuminated to an intensity of 0.25 candle-feet, what candle-power of lamps is required?

260 candle-power.

46. Two arc lamps having a mean spherical candle-power of 600 are placed 100 feet apart, and at a height of 20 feet above a roadway. Assuming the lamps to give a uniform distribution of light, determine the illumination in candle-feet at five points. A, B, C, D, and E, situated on the ground level at distances 5, 20, 50, 80, and 95 feet respectively to the right of the left-hand lamp.

Illumination at A and E = 1.36 candle-feet.

 $\vec{D} = 0.057$ 

#### CHAPTER VII.—CONDUCTORS

47. Current is required for a 50-horse-power 460-volt motor whose full-load efficiency is 90 per cent. If a current density of 155 ampères per square centimetre can be permitted, determine the size of cable required between the supply mains and the motor.

19/14 cable.

48. Current is required for a group of 400 110-volt lamps, each lamp taking 44 watts. The lamps are at a distance of 400 metres from the supply mains, the pressure of which is maintained at 126 volts. What size of cable must be used in order that the pressure across the lamps shall not be less than 110 volts?

61/16 cable.

49. A power of 200 k.w. has to be transmitted a distance of 550 metres. If the pressure at the consuming point be maintained at 500 volts, determine the size of cable required so that this power may be transmitted with a maximum loss of 6 per cent.

91/15 cable.

50. Calculate the insulation resistance of I kilometre of cable the di-electric of which is resin oiled paper having a specific resistance at normal temperature of  $3 \times 10^{15}$  ohms per centimetre cube. The conductor of the cable has a diameter of 8 millimetres, and the di-electric is 2 millimetres in thickness.

# 2000 megohms.

51. The insulation resistance of 2 kilometres of cable was found to be 200 megohms. If the conductor of the cable be 6 millimetres in diameter and the insulation 3 millimetres thick, determine the specific resistance of the di-electric.

# $3.6 \times 10^{14}$ ohms per centimetre cube.

52. An aërial transmission line, in which the poles are spaced 40 metres apart, is constructed of 2/0 S.W.G. copper wire. If the minimum temperature in the district is not likely to fall below  $-5^{\circ}$  C., determine the tension to which the wires may be adjusted when the temperature at time of erection is 30° C.

180 kilogrammes.

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## CHAPTER VIII.—THE DYNAMO—ARMATURE WINDINGS

53. The armature of a 4-pole dynamo is required to generate a total pressure of 520 volts when revolving at a speed of 660 kR.P.M. Calculate the magnetic flux per pole required to pass through the armature if the latter has 144 slots with 6 inductors in each slot. The armature is wave-wound.

 $2.7 \times 10^6$  lines.

54. A 6-pole lap-wound armature is required to generate a total E.M.F. of 432 volts when revolving at 360 R.P.M. If the flux per pole entering the armature be 8.0 megalines, calculate the required number of armature inductors.

900.

55. The armature of a 4-pole electro-plating dynamo is driven at 600 R.P.M. and has to generate a total induced E.M.F. of 9.6 volts. If the armature be lap-wound and the flux entering the armature core per pole be  $3 \times 10^6$  lines, find the number of armature inductors. Also show a development of the winding, indicating the position of the poles and brushes. There is one turn per commutator segment.

32 inductors.  $Y_R = 9$ ;  $Y_F = 7$ .

56. A certain 4-pole dynamo, used as a booster, is required to generate a maximum E.M.F. of 31 volts. If the armature be driven at a speed of 660 R.P.M. and the flux per pole entering the armature = 3.1 megalines, calculate the number of inductors required, assuming the armature to be wave-wound. Also show a development of the winding, there being one armature turn per commutator segment.

46 inductors.  $Y_R = II$ ;  $Y_F = II$ .

57. If the armature in the previous example has 25 slots, how many dummy coils are necessary, and how would they be connected?

2 dummy coils.

The first dummy coil connected in parallel with the coil formed by 1 and 12.

The second dummy coil connected in parallel with the coil formed by 23 and 44.

58. Find the number of inductors required for a 6-pole lapwound armature having the following constants:

> Maximum induced E.M.F. = 250 volts.

Magnetic flux in the armature per pole = 6.2 megalines. . = 480 R.P.M.

Armature speed . . Also if the inductors be arranged 6 in a slot with 3 turns per commutator segment, show a development of 4 consecutive winding units.

(I) Inductors = 504.

- (2) Coil I is formed by inductors Nos. 1, 86, 3, 88, 5, and 90 being joined in series in the order given. 1, 3, and 5 are placed in the top of slot No. 1 and 86, 88, and 90 are placed in the bottom of slot No. 15.
- 59. The armature of a 4-pole 500-volt turbo-dynamo is driven at a speed of 1200 R.P.M. From the following data calculate the number of armature inductors, and show a development of seven consecutive turns of the winding.

Flux per pole at full load . . = 10.2 megalines.

Volts drop in armature at full load = 2 per cent. = 10 volts.

Style of winding.  $\cdot \cdot \cdot = lap.$ 

Turns per commutator segment. = I.

(1) Inductors = 248.

(2)  $Y_R = 63$ ;  $Y_F = 61$ .

60. Calculate the approximate diameter of a shaft at any part underneath the armature or commutator of a 500-k.w. generator, the speed of the armature being 100 R.P.M.

34 centimetres.

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# CHAPTER IX.—THE DYNAMO—MAGNETIC CIRCUIT, FIELD COILS, ARMATURE REACTION, AND COMMUTATION

61. At no load a flux of 7.8 megalines per pole has to be sent through the armature of a certain 6-pole dynamo whose coefficient of magnetic leakage is 1.18. From the following data calculate the ampère-turns per pole required to drive this flux through the armature core and teeth, air-gap, and magnet core and yoke.

Armature—Diameter of core = 117 centimetres.

Gross length of core Number of ventilating ducts.

Width of each duct = 30

Width of each duct = 1.25 centimetres.

Radial depth of core below teeth. = 17Length per pole of magnetic path in core = 34

		Air-g		core		900 , 750 .	,
		"		teeth,	(	660,	
		Armature core,			, 2	oo ampèr	e-turns.
Magnetic length	•	•	•	•	•	= 50	"
Cross section.						=400  sq.	"
Magnet Yoke (of	cast s	steel)-				- •	
Magnetic length						= 32.5	,,
Diameter .						= 30	<b>)</b> )
Magnet Core (of c		teel)-	_				
Air-gap—Length						=0.6	**
Polar arc ÷ polar p						=0.7.	
Radial length of t	ooth					= 3.0	,,
Width of slot						= 1.42	,,
Width of tooth at	bott	om				= 0.88	**
Width of tooth at	top			•.		= 1.03  cen	itimetres.
Number of teeth				•		= 150.	

62. If at full load a magnetic flux of 8.8 megalines has to be sent through the armature of the machine mentioned in the previous problem, calculate the ampère-turns required at full load to drive this flux through the magnetic circuit.

,, yoke,

Armature core,	250 amp	ère-turns.
,, teeth,	1200	"
Air-gap, Magnet core,	3300 1180	,,
Magnet core,	1180	,,
" yoke,	1000	,,

700

63. The shunt field winding of a certain 400-k.w. generator has to give 10,400 ampère-turns per pole, the volts per shunt spool being 62.5. The bobbins on which the coils are wound have an axial length of 30 centimetres and are of such dimensions that the internal diameter of the winding is 48 centimetres and the radial depth 4 centimetres. Assuming a space factor of 0.56, determine the size of wire (S.W.G.) with which to wind the coils. Axial length of winding = 23 centimetres.

12 S.W.G.

64. From the following data relating to the shunt field coils of a 250-k.w. generator determine the size of wire with which to wind the shunt coils.

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Ampère-turns per pole . . . = 5800.

Volts per field coil . . . . = 83.

Internal diameter of winding . . = 31 centimetres.

Radial depth of winding . . = 7 , ,  

Space factor (assumed) . . = 0.5.
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65. The brushes of a certain 250-k.w. 6-pole generator are given a brush lead of 5°. From the following data calculate the number of ampère-turns per pole necessary to compensate for the demagnetising ampère-turns of the armature.

Full-load currents . . . =455 ampères. Circuits through the armature . =6.

Total number of inductors . = 1200.

#### 1220 ampère-turns.

66. Assuming four lines of force to be set up per ampère per centimetre of embedded length, and 0.8 per ampère per centimetre of free length, calculate the reactance voltage of an armature having the following constants:

Diameter of commutator . . . = 92 centimetres.

Speed in R.P.M. . . . . . = 320.

Number of commutator segments . = 600.

Length of arc of brush contact . = 1.8 centimetres.

Mean length of one armature turn  $\cdot = 1.8$  centimetres

Effective length of core . = 22.5 ,,

Turns per commutator segment . = 4. Full-load current . . . = 455.

Number of armature circuits. = 6.

4 volts.

## CHAPTER X.—THE DYNAMO—SHUNT RHEOSTATS

67. In a certain dynamo 5300 and 7000 ampère-turns per pole are required at no load and full load respectively. If the dynamo be shunt-wound, determine by aid of the following data the value of the shunt-regulating resistance and the number of steps into which it may be divided. Allow a variation in E.M.F. per step of 4 per cent. of the total range of induced E.M.F. between no load and full load, and assume the working portion of the saturation curve to be approximately a straight line.

Number of turns per shunt coil . . = 3500.

Exciting current at full load . . . = 2 ampères.

Constant voltage across shunt and rheostat

Range of induced E.M.F. between no load and full load . . . = 500-525.

Total resistance of shunt winding . . = 240 ohms.

Total shunt-regulating resistance = 95 ohms. Number of steps = 25, i.e. 3.8 ohms per step.

68. In the previous problem where the regulating resistance has a value of 3.8 ohms per step, if the resistance coils be made of beacon alloy, determine the diameter of wire required, also the length for each section. Maximum field current = 2 ampères.

Diameter = 0.084 centimetre. Nearest S.W.G. No. 21. Length of No. 21 = 280 centimetres.

69. If in Problem 67 the full-load ampère-turns in excess of those required at no load be supplied by a series winding, find the number of series turns per pole. Full-load current=350 ampères.

5 series turns per pole.

#### CHAPTER XI.—MOTORS AND STARTING RESISTANCES

70. The armature core of a certain 4-pole wave-wound machine has 61 slots each containing 20 inductors. If the flux entering the armature per pole be 2.3 megalines, calculate the torque exerted by the armature when it carries a current of 50 ampères.

## 46 kilogramme-metres.

71. The armature of a certain 4-pole wave-wound motor has a diameter of 30 centimetres and is wound with 400 inductors. If the flux in the armature per pole be 4.8 megalines, and the full-load current 40 ampères, calculate the average pull in kilogrammes acting on each inductor at full load.

## 0.42 kilogramme.

72. If the armature of the motor mentioned in the previous problem revolve at 900 R.P.M., determine (1) the horse-power developed by the motor, and (2) the value of the counter *e.m.f.* 

# (I) 26 H.P.; (2) 485 volts.

73. From the following data relating to a 6-pole motor calculate the brake horse-power when the armature carries a current of 400 ampères. Of the total power developed by the motor, 3 per cent. is absorbed in overcoming the friction and iron losses.

Flux entering the armature per pole = 8.0 megalines.

Total number of armature turns . = 600.

Number of armature circuits . . = 6. Speed of armature in R.P.M. . . = 350.

200 B.H.P.

74. A motor is geared to the main axle of travelling crane, the gear ratio between the motor and the axle being 1:4. From the following data calculate the pull exerted at the circumference of the crane wheels when the armature takes a current of 45 ampères. The combined losses due to friction in motor and gearing, and eddy currents and hysteresis in armature, may be taken as being equal to 10 per cent. of the total power developed by the armature.

Number of armature inductors = 824.

Style of winding = 2-circuit.

Flux per pole in armature core = 2.9 megalines.

Diameter of driving wheel = 50 centimetres.

## 126 kilogrammes.

75. The armature of a certain 70-H.P. 250-volt 6-pole motor is wave-wound with 110 turns. At normal working temperature the resistance of the armature winding, brushes, and brush leads equal 0.02 of an ohm, and when running light at 908 R.P.M. with the brushes in the neutral position the armature current was 13.3 ampères. From this data calculate the flux entering the armature per pole.

2.5 megalines.

76. If in Problem 75 the brushes are fixed in the geometrical neutral axis so that the flux entering the armature per pole remains constant at all loads, calculate the speed of the armature at full load assuming the armature full-load current to be 235 ampères.

# 895 R.P.M.

77. A 20-B.H.P. 500-volt motor has to be designed to run at a speed of 600 R.P.M. when fully loaded, and to work at an efficiency of 87 per cent. If the volts drop in the armature has not to exceed 3 per cent. of the full rated pressure, calculate the number of armature inductors, the armature being wave-wound. The motor has 4 poles, and the flux per pole entering the armature equals 2.2 megalines.

# 1104 inductors.

78. A 5-B.H.P. 230-volt motor takes 19 ampères at full load. If the maximum starting current has not to exceed 30 ampères, calculate (1) the number of steps into which the starting resistance must be divided, and (2) the value of the resistance of each step. Resistance of armature brushes and brush leads =0.34 of an ohm.

(1) 7 steps.

<sup>(2) 2.8, 1.8, 1.1, 0.70, 0.47, 0.30,</sup> and 0.19 of an ohm.

79. A 20-B.H.P. 460-volt shunt-wound motor requires a current of 38 ampères when running normally at full load. If the maximum starting current has not to exceed 53 ampères, determine (1) the number of steps required for the starting resistance, and (2) the resistance of each step. The armature resistance = 0.3 of an ohm.

(I) IO steps.

(2) 2.4, 1.8, 1.3, 0.9, 0.6, 0.45, 0.32, 0.24, 0.17, and 0.12 of an ohm.

80. In the starting resistance referred to in Problem 78, determine the size and length of wire required for the resistance 0.7 of an ohm forming the fourth step. The resistance coils are to be made from platinoid wire. It may be assumed that the motor is started in 14 seconds, and that the switch arm is moved uniformly over the contacts.

Size of wire = No. 20 S.W.G. Length of wire = 112 centimetres.

81. The starting resistance in Problem 79 is made of eureka wire, and, assuming the motor is started in 20 seconds, calculate the size and length of wire to form the last step, the resistance being 0.12 of an ohm.

Size of wire = No. 16 S.W.G. Length of wire = 57 centimetres.

# CHAPTER XII.—HEATING, LOSSES, EFFICIENCY, AND TESTING

82. Calculate the resistance at 60° C., volts drop, and watts expended in the winding of an armature having the following constants:

Full-load current . . . = 455 ampères. Mean length of 1 turn . . . = 246 centimetres.

Number of slots . . . = 150. Inductors per slot . . . = 8.

Cross-section of each inductor . =0.25 x 1.2 square centimetre.

Number of armature circuits . = 6.

Resistance = 0.027 of an ohm. Volts drop = 12. Watts expended = 5500. 83. The core of the armature referred to in Problem 82 has the following constants. It is required to predetermine the iron losses by aid of the curve given in Figure 247.

External diame	eter of	lami	inatio	ns.	= 117 ce	ntimetres.	
Internal "	,,		,,		= 77	,,	
Depth of slots					= 3	,,,	
Width of slots	•				= 1.42	**	
Number of slot					= 150.		
Gross length of	core				= 30 cen	timetres.	
Number of ven	tilating	du	cts		= 4.		
Width of each	= 1.25 centimetres.						
Radial depth	of arr	natı	ire c	ore	-		
below toot	h roots				= 17	,,	
Flux per pole							
at full load	l				=8.8 me	galines.	
Magnetic cycle	s per se	econ	ıd.		= 16.		
•	=				550	o watts.	

84. If the armature whose losses have been determined in Problems 82 and 83 has an overall length of 73 centimetres, and revolves at 320 R.P.M., determine by aid of the curves in Figure 248 the approximate temperature rise.

## Temperature rise, 40° C.

85. The armature of a certain 250-k.w. generator is driven at a speed of 320 R.P.M., and the diameter and overall length of its core are 117 and 30 centimetres respectively. Determine the value of the output coefficient.

# Output coefficient = 0.0018.

86. From the following constants regarding the commutator of a certain 250-k.w. generator make an estimation of the total commutator loss.

```
Full-load current . . . = 455 ampères.

Speed of armature . . . = 320 R.P.M.

Diameter of commutator . . = 90 centimetres.

Number of sets of brushes . . = 6.

Number of brushes per set . . = 6.

Width of each brush . . . = 3.3 centimetres.

Length of brush arc . . . = 1.8 ,,

Brush pressure . . . . = 100 grammes per square centimetre.
```

The brushes were in this case of hard graphitic carbon having a contact resistance of 0.2 of an ohm per square centimetre of contact area. Add to calculated losses 15 per cent. for sparking loss.

2300 watts.

87. If the commutator in the previous example has a useful length of 26 centimetres, calculate the approximate temperature rise at full load.

## Temperature rise = 37° C.

88. The shunt field coils of a certain dynamo have a resistance of 80 ohms at 15° C. If at the end of a 6 hours' test the resistance (as measured by a Wheatstone bridge) increases to 94 ohms, what is the mean rise in temperature of the coils?

# Temperature rise, 40° C.

89. From the following data regarding the losses in a 75-k.w. 250-volt generator calculate the efficiency at 25, 50, 75, and 100 per cent. of the full rated output of the machine.

				Output in per Cent. of full rated Output.				
				-25	50	75	100	
Armature iron	loss	(Watts)		1025	1115	1205	1315	
" C²R	,,	, ,,		182	688	1520	2680	
Commutator C <sup>2</sup> R	,,	"		76	220	425	620	
" friction	,,	"		423	423	423	423	
Shunt excitation	,,	,,		1044	1122	1200	1295	
Series excitation	,,	,,		23	92	206	367	
Friction and windage	· ,,	,,	•	501	501	501	501	
Efficiencie	PC 1	er cent	 •	85	90	<b>QI</b> .	91	

90. A 5-B.H.P. 230-volt motor is tested by a prony brake in which the distance  $L_1$  and  $L_2$  (Figure 257) is 60 centimetres. The motor is loaded to such an extent that the current input = 18.3 ampères and the speed = 600 R.P.M. If at this current input the weight (W) and spring balance (S) reading be 9 and 0.6 kilogrammes respectively, calculate (I) the B.H.P. and (2) the efficiency at this particular load.

(1) 4.8 B.H.P.(2) Efficiency, 85 per cent.

91. Two similar 30-B.H.P. 460-volt shunt-wound motors are tested by the Hopkinson method (Figure 258). The current circulating between the two machines is adjusted to 55 ampères, and at this particular load the current taken from the supply mains E was 13 ampères. What is the approximate efficiency of each machine?

Efficiency, 90 per cent.

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